The background of the slide is a 3D visualization of a gravitational well, represented by a grid of blue lines that curves inward to form a central depression. At the center of this well, two black spheres represent black holes in a binary system, with white arrows indicating their orbital path around each other.

Astrophysics With Few-Hz Gravitational Waves

Cole Miller, University of Maryland

Outline

- The most massive white dwarfs
- Long lead times for telescopes
- Nonzero eccentricities?
- Intermediate-mass black holes

Will focus on binaries; continuous-wave and burst amplitudes are too low.

Will have theorist's optimism and assume lower limit of 1 Hz.

Amplitude of Gravitational Waves

Binary of reduced mass μ , total mass M .
At luminosity distance d , frequency f_{GW} ,
dimensionless strain amplitude is

$$h = 3 \times 10^{-23} (f_{\text{GW}}/1\text{Hz})^{2/3} (M_{\text{ch}}/10 M_{\text{sun}})^{5/3} (100\text{Mpc}/d)$$

where $M_{\text{ch}}^{5/3} = \mu M^{2/3}$ defines the “chirp mass”.

Frequency of Waves

The frequency at the innermost stable circular orbit (ISCO) for a nonrotating hole is

$$f_{\text{GW}}(\text{ISCO}) = 4.4 \times 10^3 \text{ Hz } (M_{\text{sun}}/M)$$

For rotating, up to

$$f_{\text{GW}}(\text{ISCO}) \sim 2 \times 10^4 \text{ Hz } (M_{\text{sun}}/M)$$

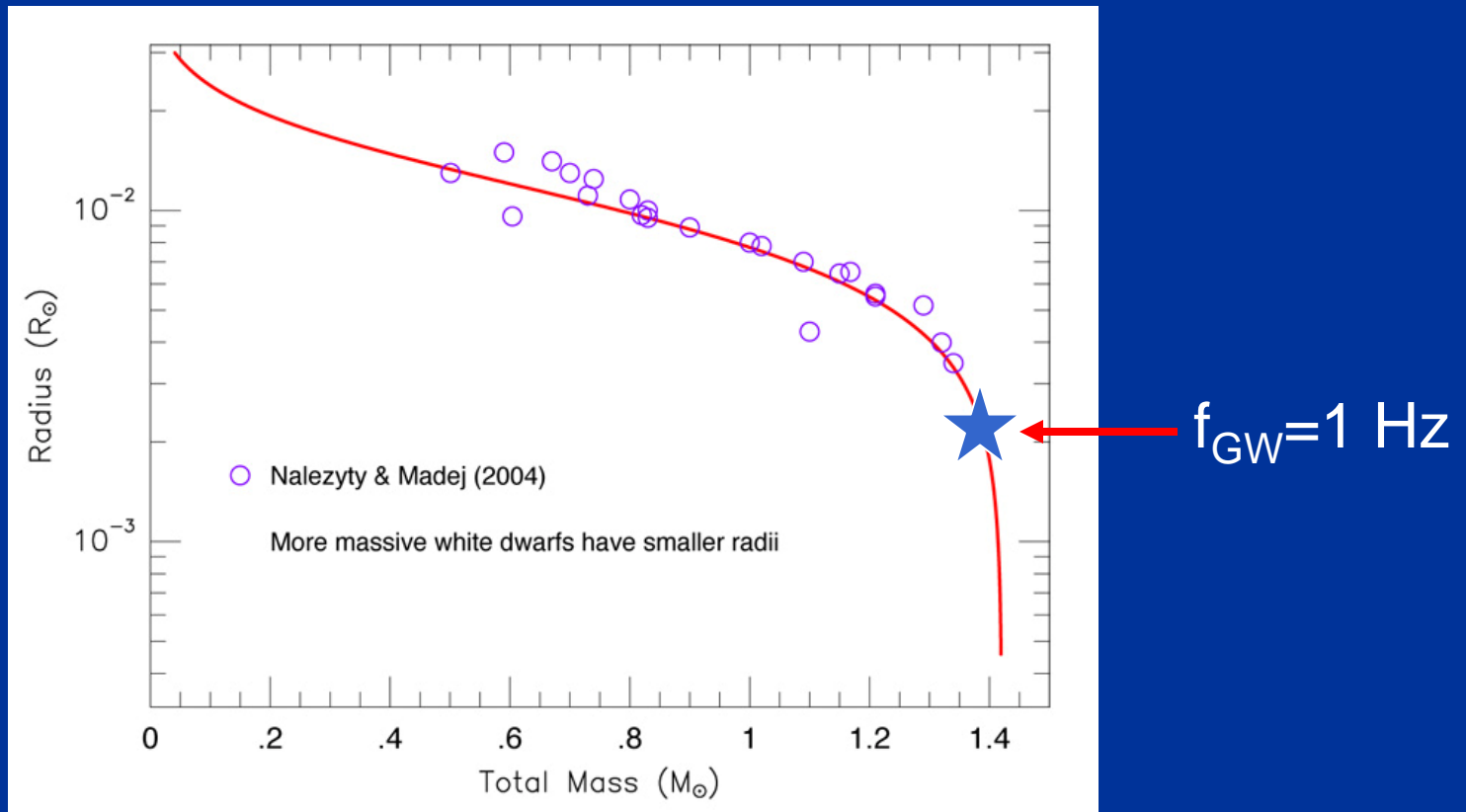
More generally, object of average density ρ has maximum frequency $\sim (G\rho)^{1/2}$

Neutron star: $\sim 2000 \text{ Hz}$

White dwarf: up to $\sim 1 \text{ Hz}$

The Most Massive WD

- $\sim 10^{8-9}$ WD binaries in Milky Way
- Even small fraction with $M \sim 1.4 M_{\text{sun}}$ gives large number; new category of sources



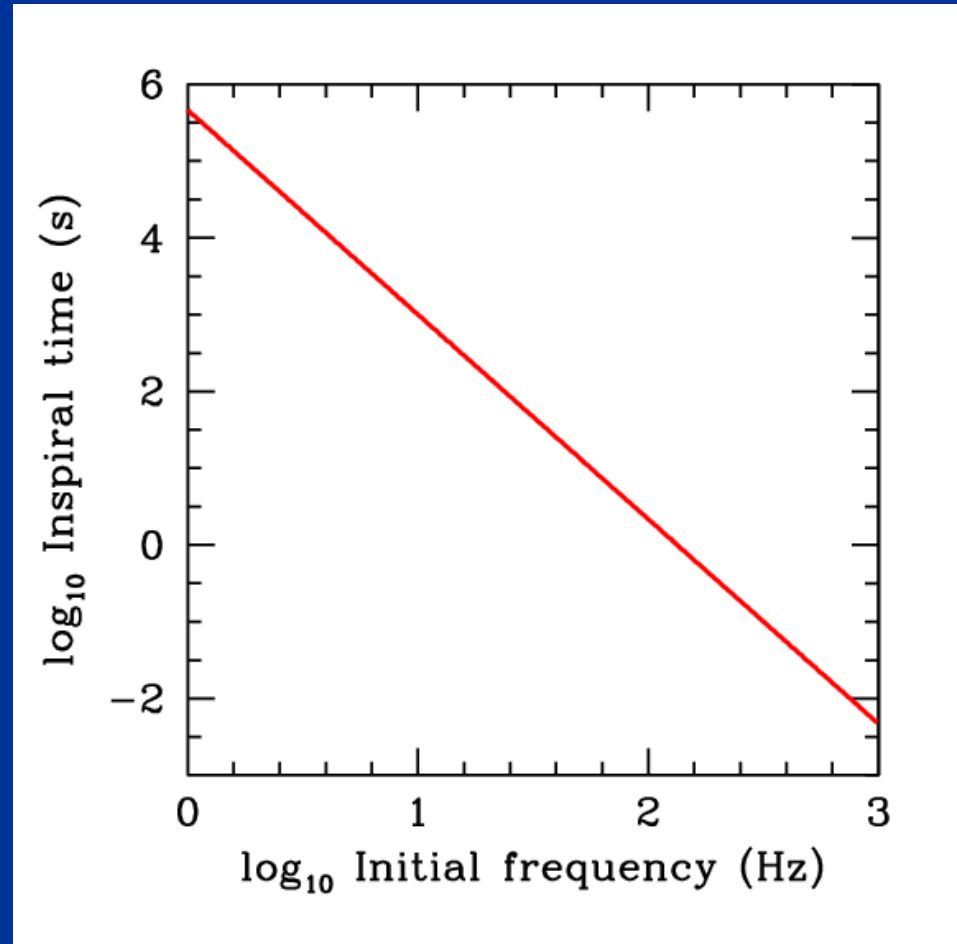
What Can Massive WD Do For You?

- Precise maximum mass depends on composition, other properties
- Massive WD (in binaries with normal stars) thought to be Type Ia SNe progen.
- Mergers would be spectacular but short-lived EM events

How much lead time do we have?

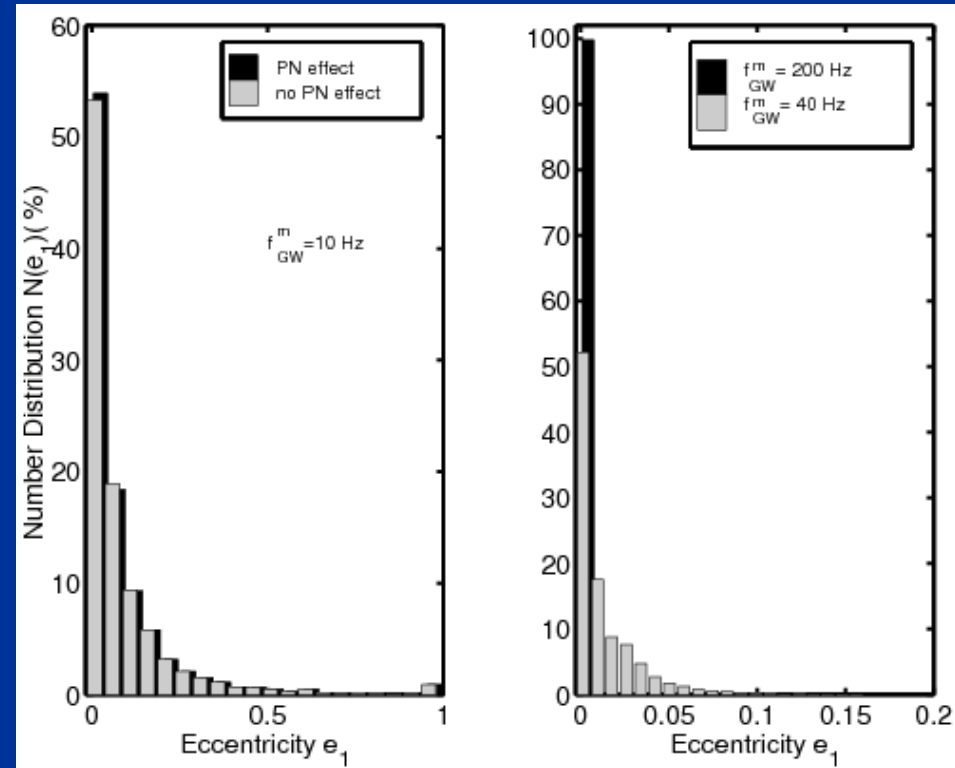
Advance Warning of Merger

- EM counterparts to mergers: lots of info!
Precise localization
Nature of transients
- Time to merger scales as $f_{\text{init}}^{-8/3}$
- At 1 Hz, could be identified days in advance
- Key: how soon could GW be localized?
Rotation of Earth?



Nonzero Eccentricities?

- Usually, think of binary GW as circular **~true for >10 Hz or field binaries**
- Dynamical interactions can change, e.g., Kozai in dense systems
- $e \sim 1/f$ for $e \ll 1$
- Low freq important for inferring dynamic origin



L. Wen 2002

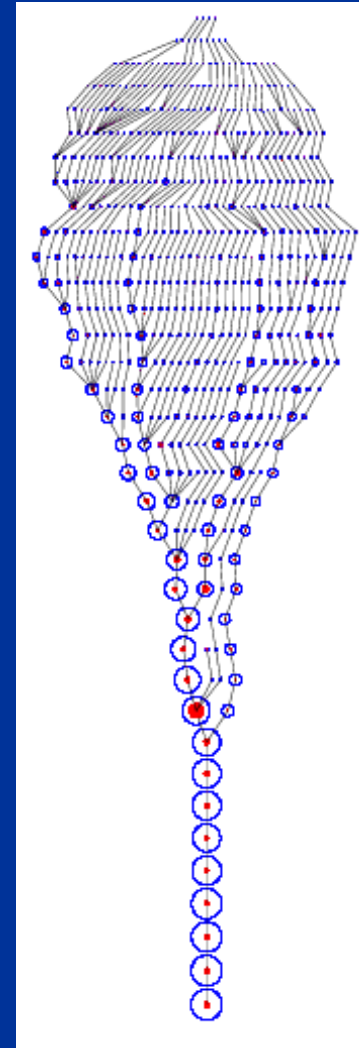
Intermediate-Mass Black Holes

Mass between 10^2 and $10^4 M_{\text{sun}}$

Too massive to have formed from solitary star in current universe, but smaller than standard supermassive black holes.

Context and Connections

- In $z \sim 5-30$ universe, seeds for SMBH
- In local universe, probes of star cluster dynamics
- Potentially unique sources of gravitational waves (ground and space)

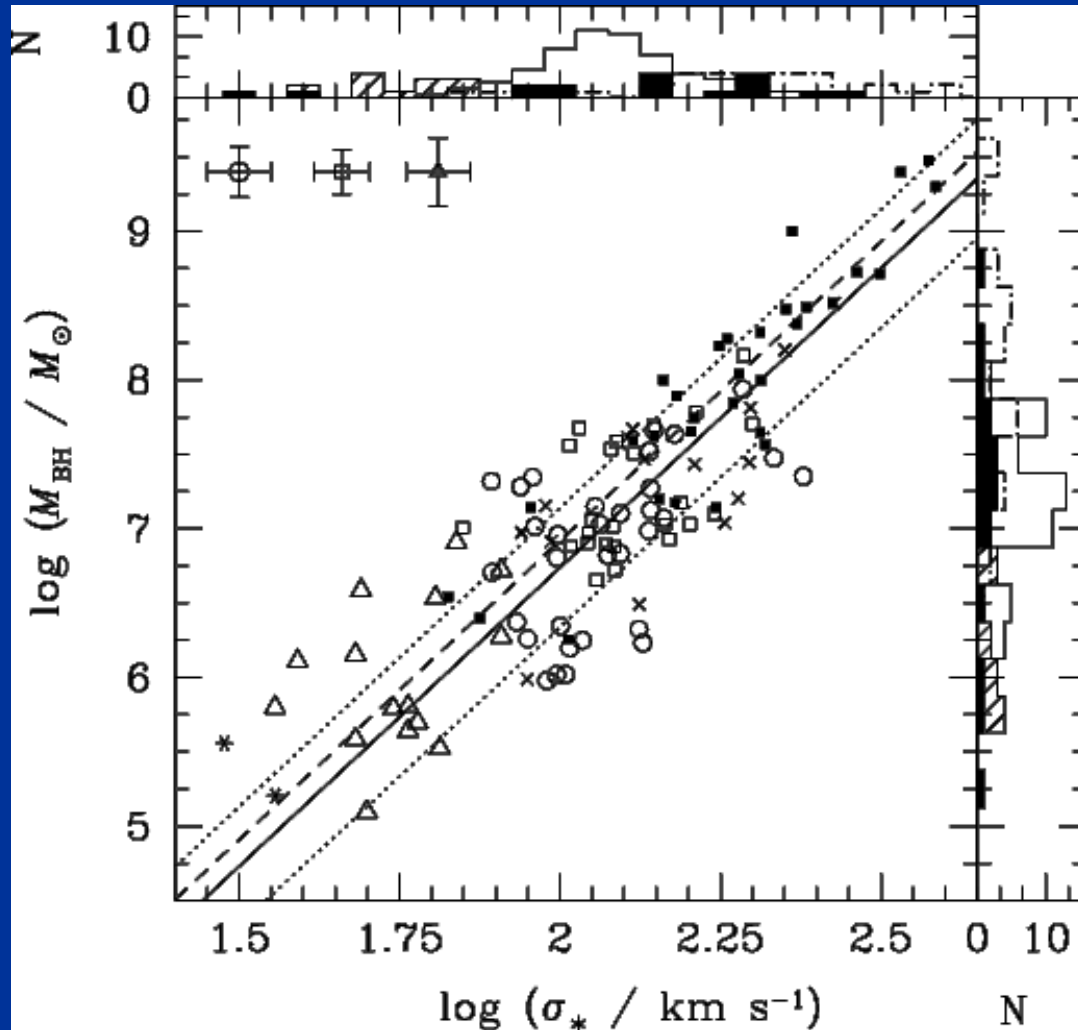


Wechsler et al. 2002

Why Are We Not Sure?

- Stellar-mass ($5-20 M_{\text{sun}}$) and supermassive ($10^6-10^{10} M_{\text{sun}}$) BH are established with certainty
- Why not IMBH ($10^2-10^4 M_{\text{sun}}$)?
- Lack of dynamical evidence
 - Too rare for easy binary observations
 - Too light for easy radius of influence obs
- Attempts being made, but settle for indirect observations in the meantime

Low-Mass SMBH?



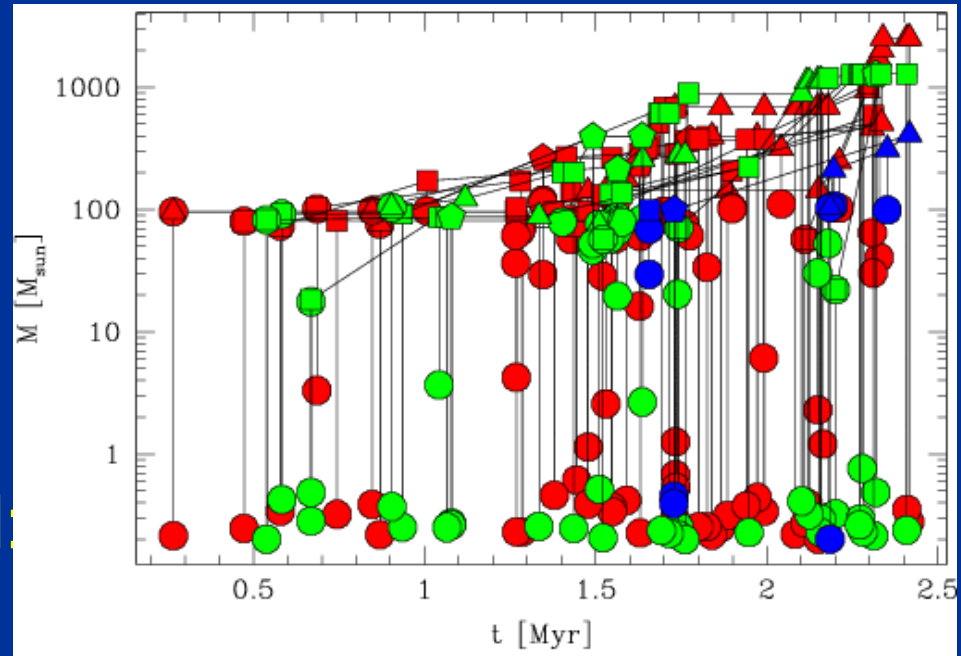
Central massive
black holes

Masses below
 $\sim 10^6 M_{\text{sun}}$ are
inferred indirectly,
but extrapolation
suggests $M \sim 10^4 M_{\text{sun}}$
for numerous small
galaxies

Formation of IMBHs

- Problem: $\sim 10^3 M_{\text{sun}}$ too much for normal star!
- Population III stars
Low Z; weak winds
- Collisions or mergers
Needs dense clusters
Young: collisions Old: three-body

>1 IMBH in single cluster?



Gurkan et al. 2006

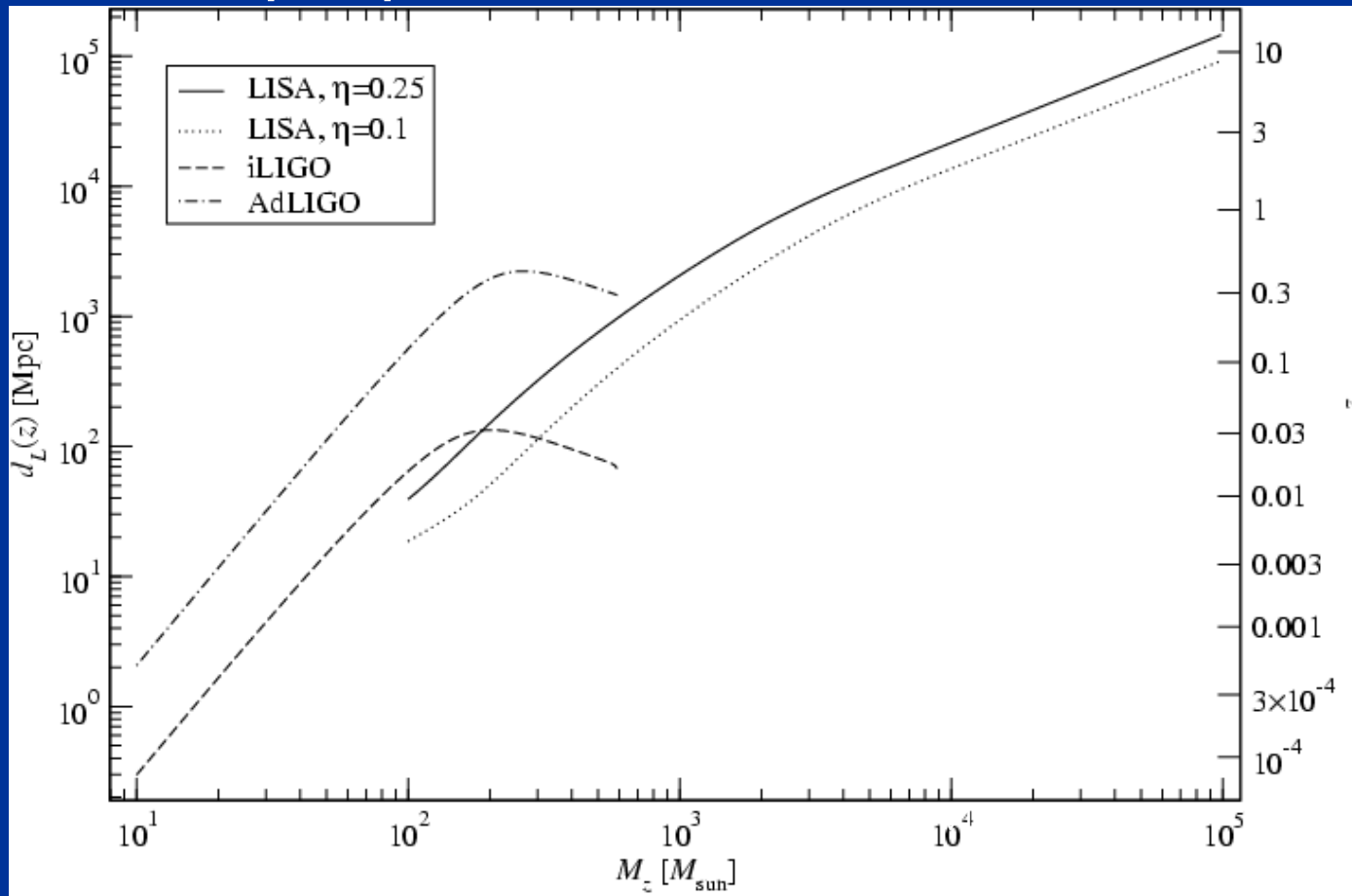
Portegies Zwart & McMillan

Observing GW from IMBH

- Stellar-mass BH with IMBH?
Promising at >1 Hz (Mandel et al. 2008)
- IMBH with IMBH
Plausible with low freq; occur if binary fraction $>10\%$ (Fregeau et al. 2006)

IMBH-IMBH Visibility

- $\sim 1000 M_{\text{sun}}$ binary visible to $z \sim 1$.
- Reasonable rates: few tens per year at >1 Hz
- Unique probe of dense cluster star formation



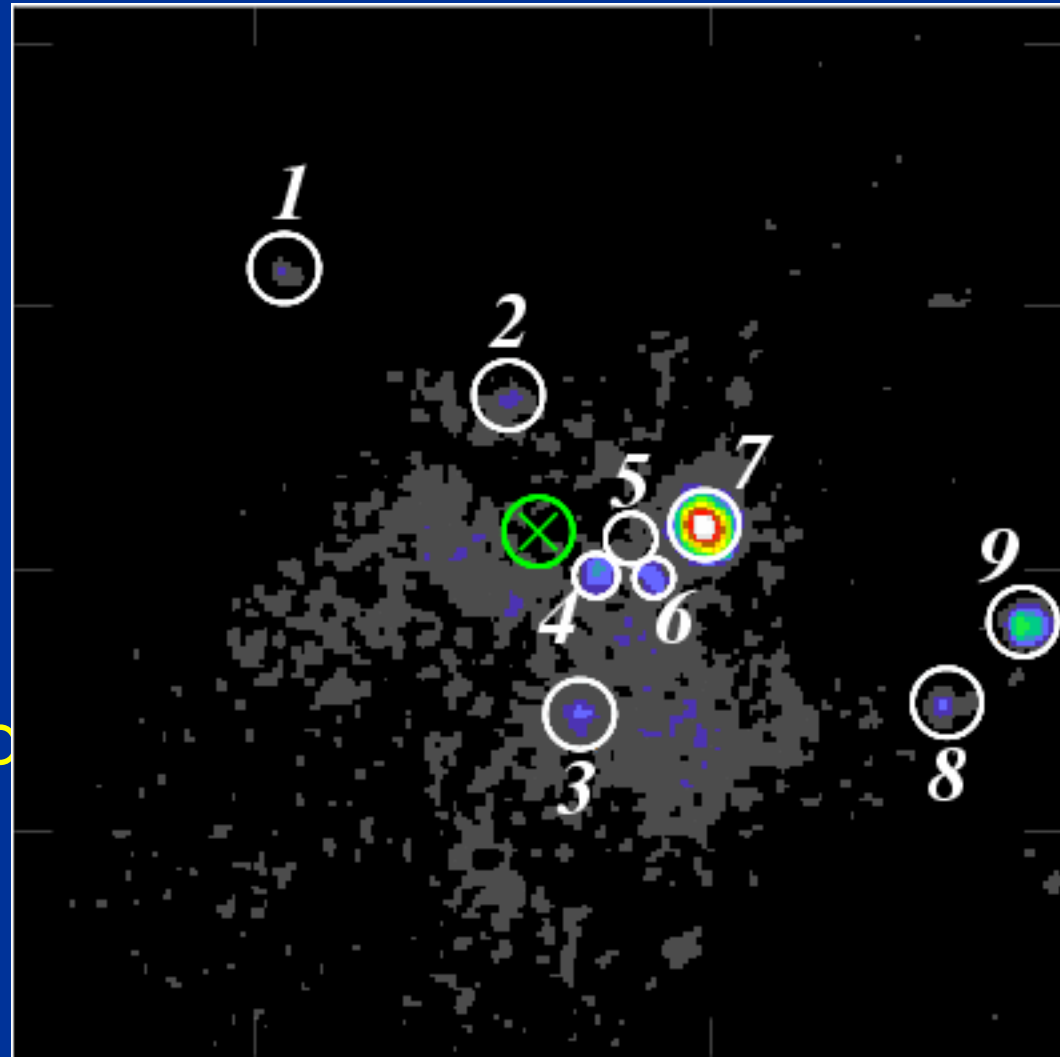
Fregeau et al. 2006

Conclusions

- The ~few Hz range contains qualitatively new sources: heavy WD and IMBH
- Long lead time will allow pointing of large telescopes if the direction can be established to within a few degrees
- Very worth pursuing!

Ultraluminous X-ray Sources

- Ultraluminous X-rays:
Variable
 $L_{\text{iso}} > 10^{39-40}$ erg/s
Some near dense clusters
- Not in galactic centers
Thus, not SMBH; would sink to center
- No dynamical mass measurements yet

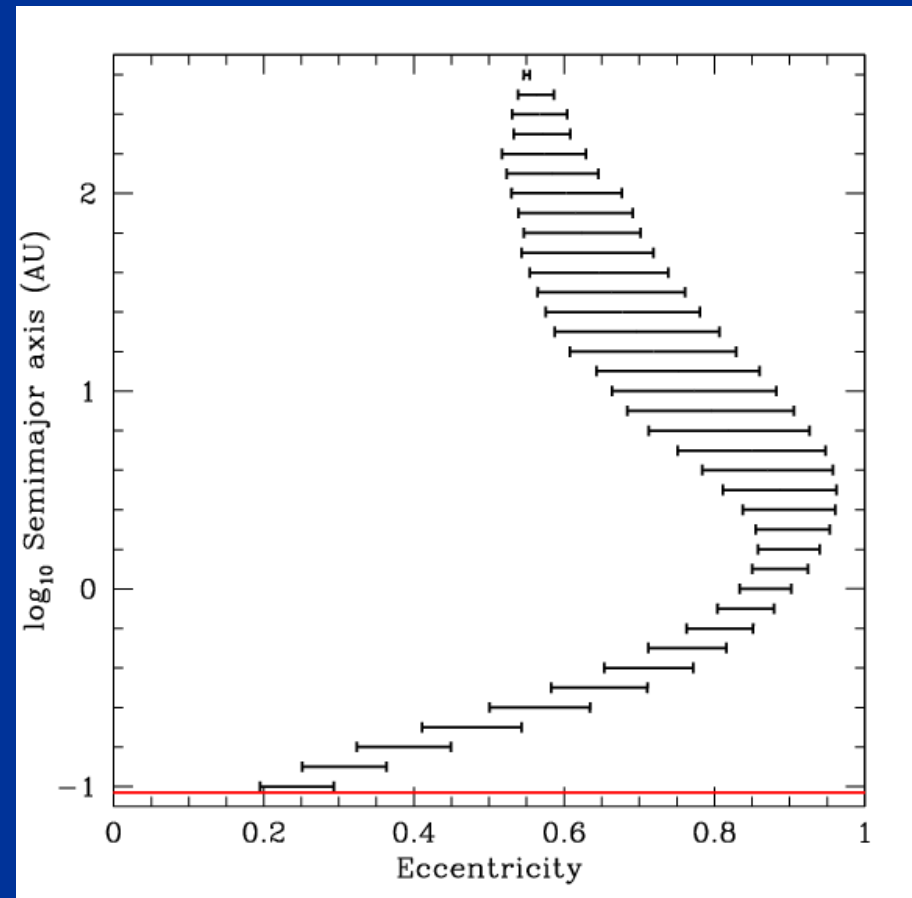


Matsumoto et al. 2000

Properties of Bin IMBH Mergers

- Amaro-Seoane, Miller, and Freitag 2009
- Major results:
 - Cluster stays intact
 - $< 10^8$ yr merger
 - Circular at 1 Hz
- Good probes of clustered star formation

$10^3 M_{\text{sun}} - 10^3 M_{\text{sun}}$ coalescence



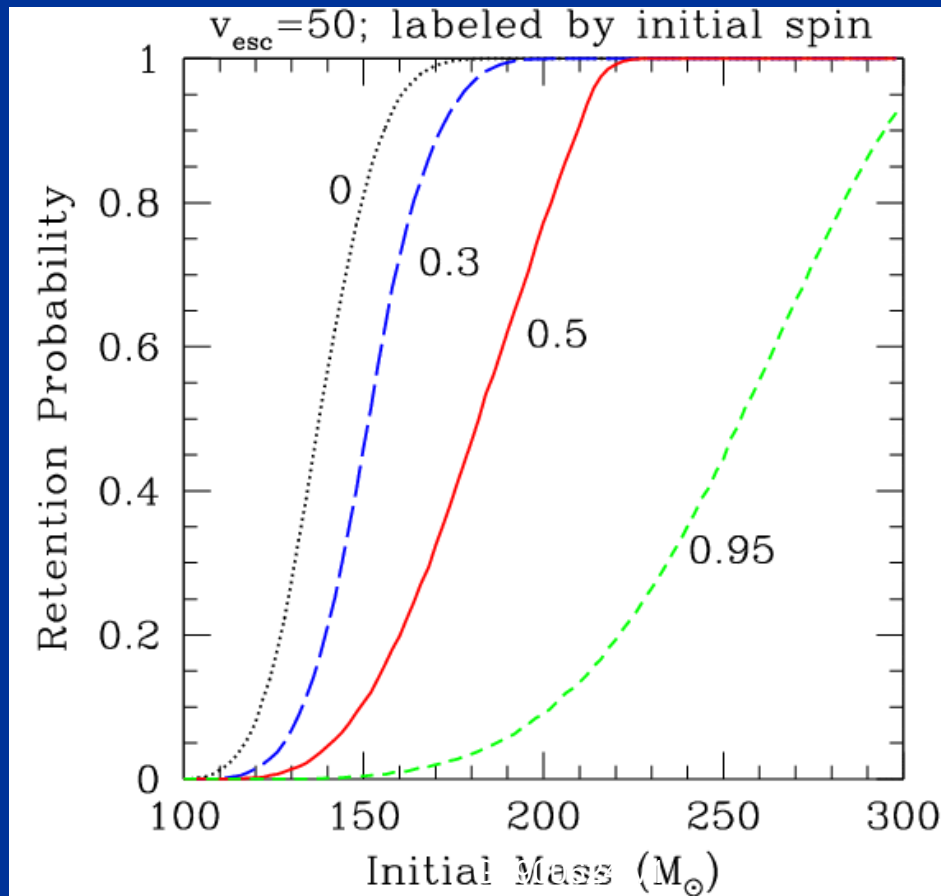
Amaro-Seoane et al. 2009

Competing Ideas

- Beaming (geometrical or relativistic)
King et al.; are spectra, variability okay?
- True super-Eddington accretion
Begelman; interesting idea with many consequences to be worked out.
But no direct evidence that this happens
- All ideas face challenges to explain this unique class of accreting black holes!

Retaining IMBH in Globulars

- Escape speed only ~ 50 km/s or less
- $>300 M_{\text{sun}}$ retained, but IMBH spin crucial

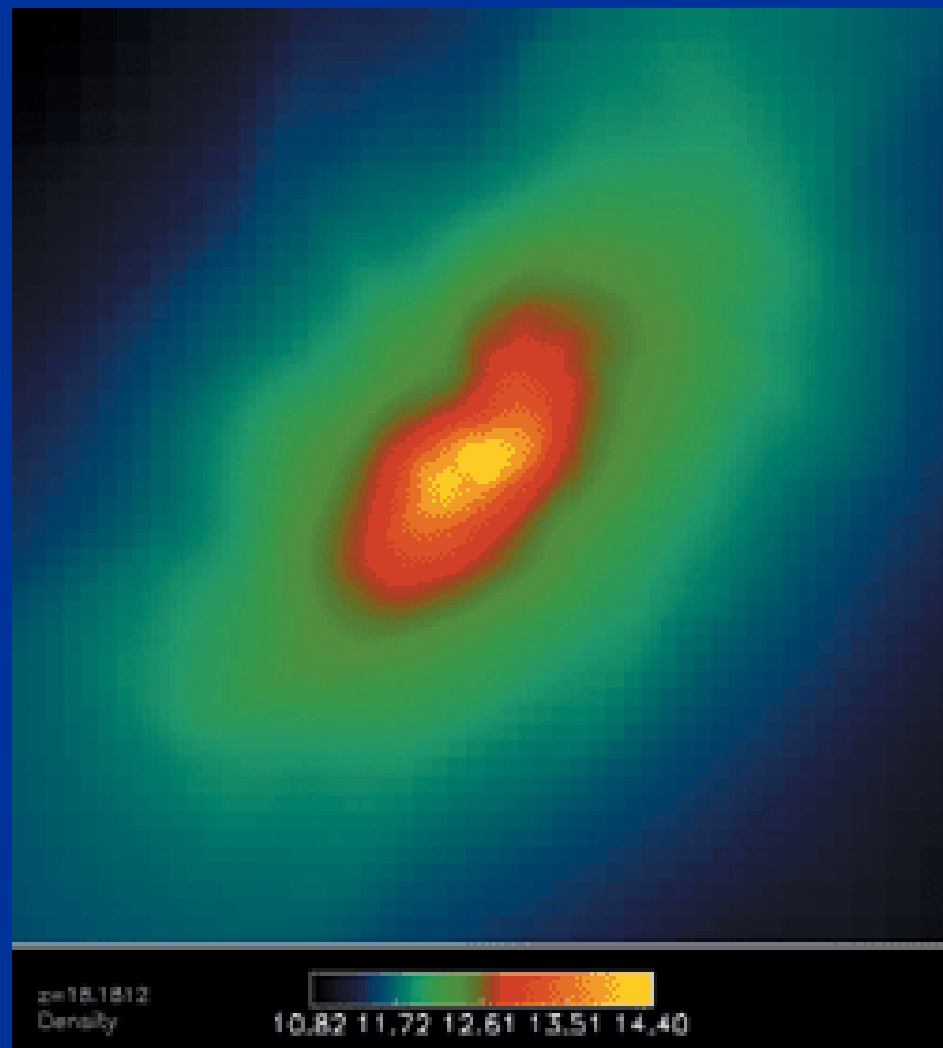


Open Question: IMBH Spin

- Important for dynamics and gravitational wave detection
- Initial collapse: $a/M=0.93$ (\sim MHD limit, e.g., Gammie)?
- Random mergers with giants, MS stars?
Would decrease spins
- Need coupled stellar evolution, bin/single cluster dynamical evolution

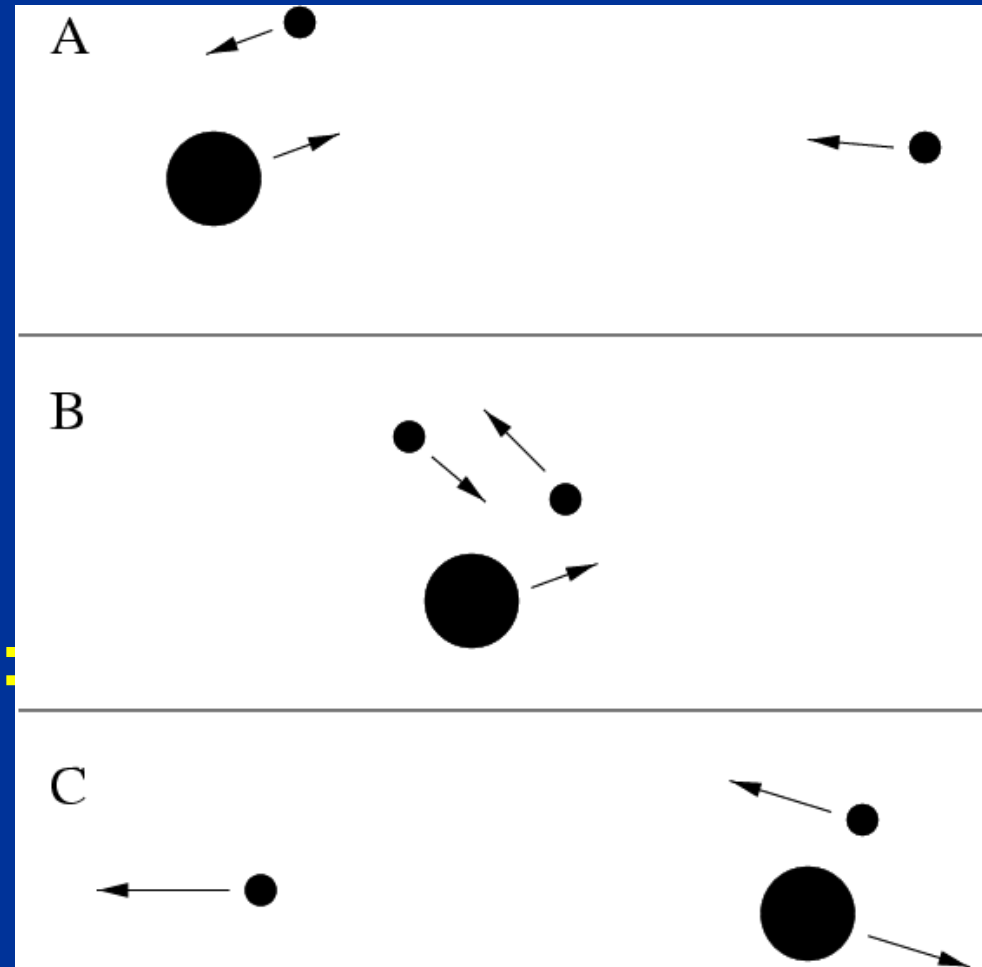
Formation of IMBHs

- Problem: $\sim 10^3 M_{\text{sun}}$ too much from normal star!
- **Population III stars**
Low Z; weak winds
- Collisions or mergers
Needs dense clusters
Young: collisions Old:
three-body



Formation of IMBHs

- Problem: $\sim 10^3 M_{\text{sun}}$ too much from normal star!
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Open Question: Collision Product

- Runaway collisions are promising
- But, how does collision product evolve?
Not a star!
Collisions faster than cooling time
Lumpy; N-body core dynamics?
- When some core collapses, is there a direct collapse or a supernova?
- What is the spin parameter of the IMBH?

Open Question: Super Star Cluster Numbers

- For runaway, need $>10^5 M_{\text{sun}}$, short relaxation time

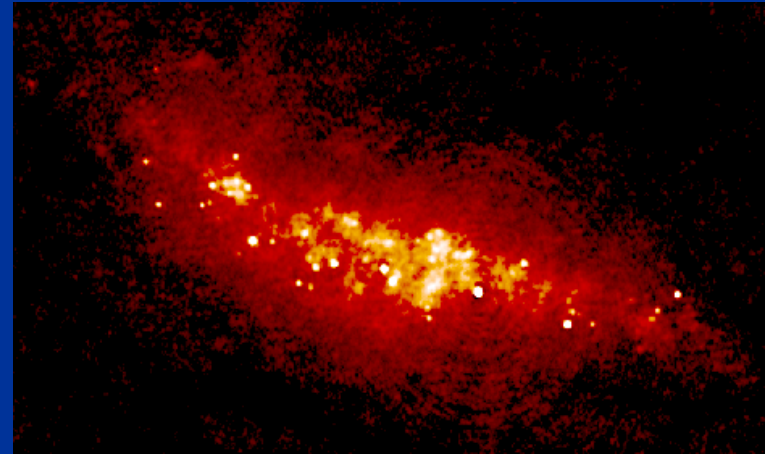
How much star formation is in this mode?

Does it depend on total SFR?

Does it depend on metallicity?

- Could imagine being more important at $z \sim 1$, or $z \sim 20$, than now.

M82



Summary of Formation

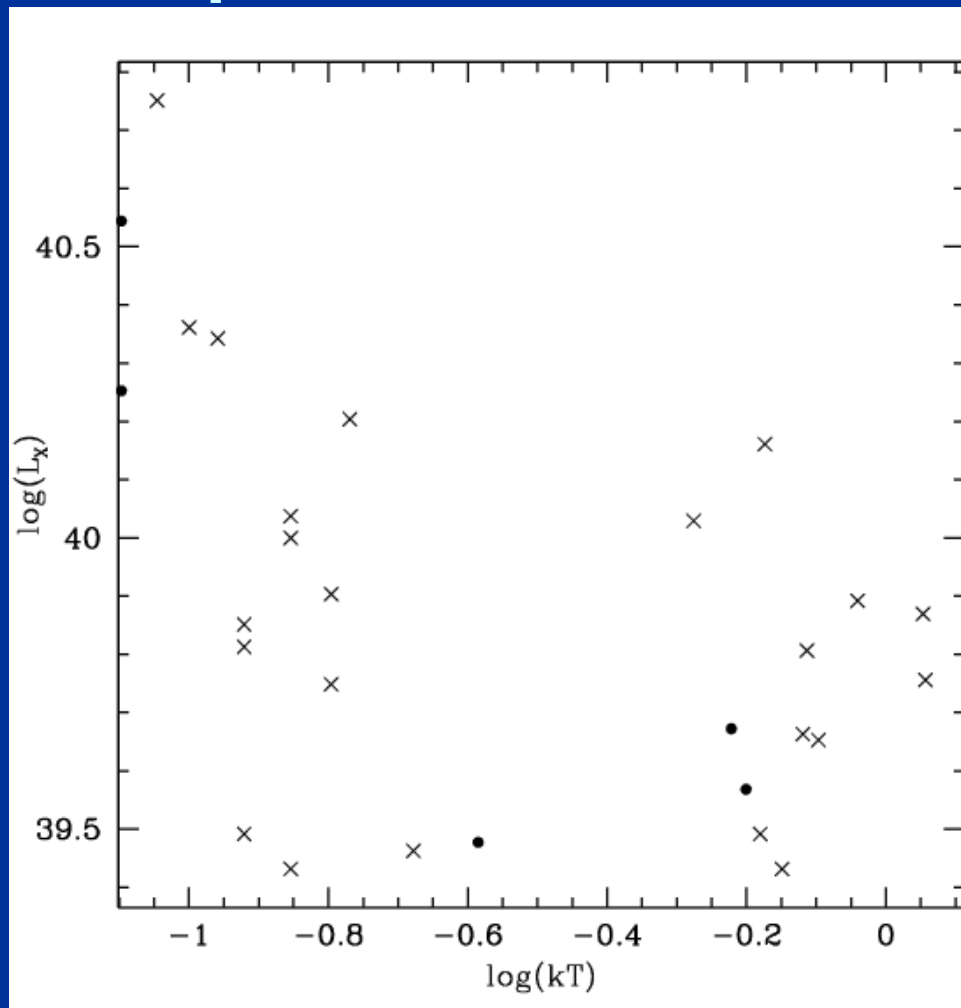
- Modulo open questions, runaway collapse seems reasonable

Then, can have collisionless growth to $\sim 500 M_{\text{sun}}$ (Gultekin et al. 2006)

- Early universe Pop III might have happened
- Seems difficult to avoid IMBH on way to SMBH in most cases
- But what about observations?

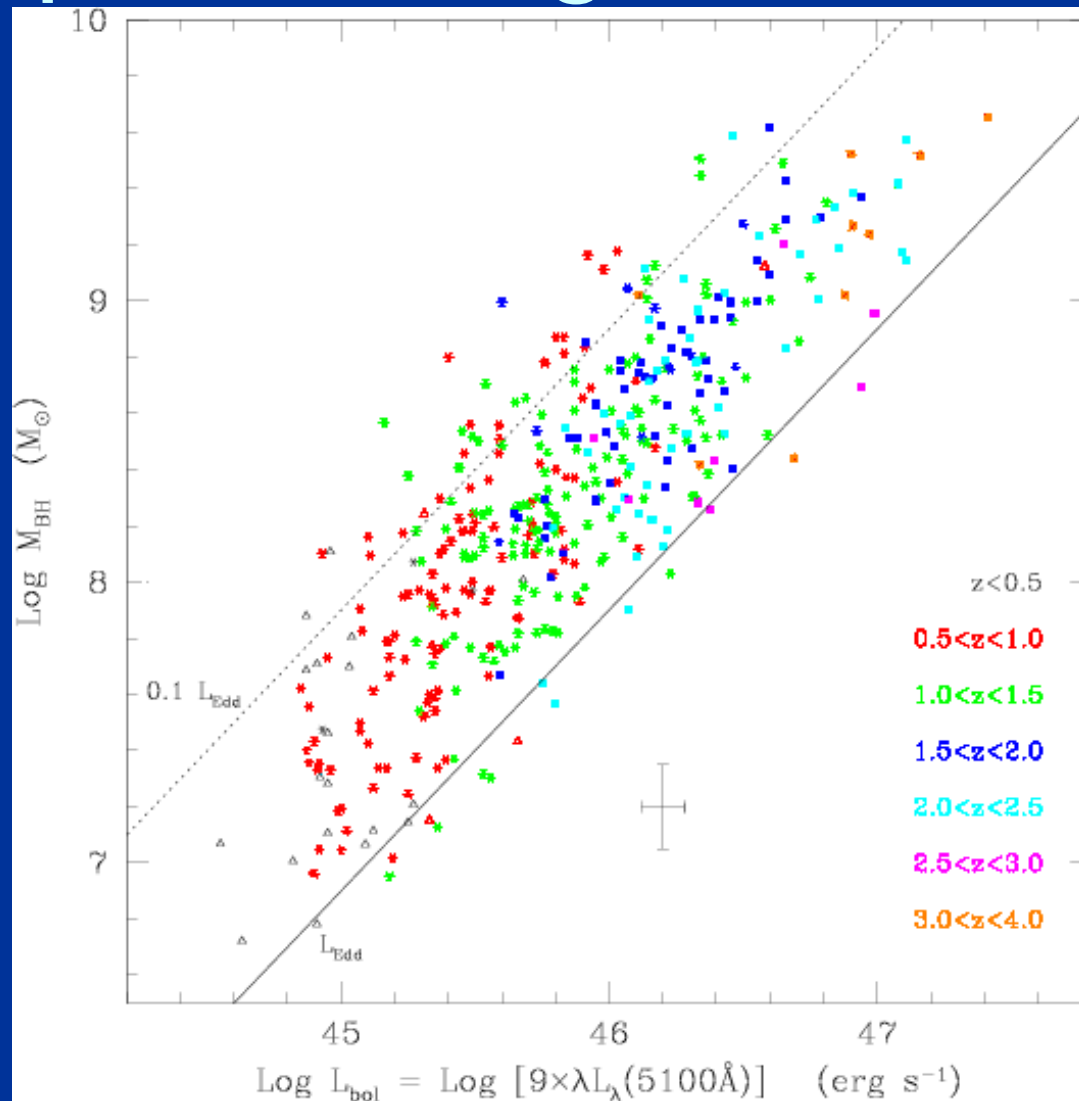
Spectral Properties

- XMM spectra often require two-comp fits
MCD and power law
- Many need cool disk
 $T \sim M^{-1/4}$; high mass?
Some don't; two classes?
- Low temp, high L means large emitting area
- Low L_{opt}/L_X
Not relativistically beamed
- Evidence for new type of object.



Winter et al. 2005

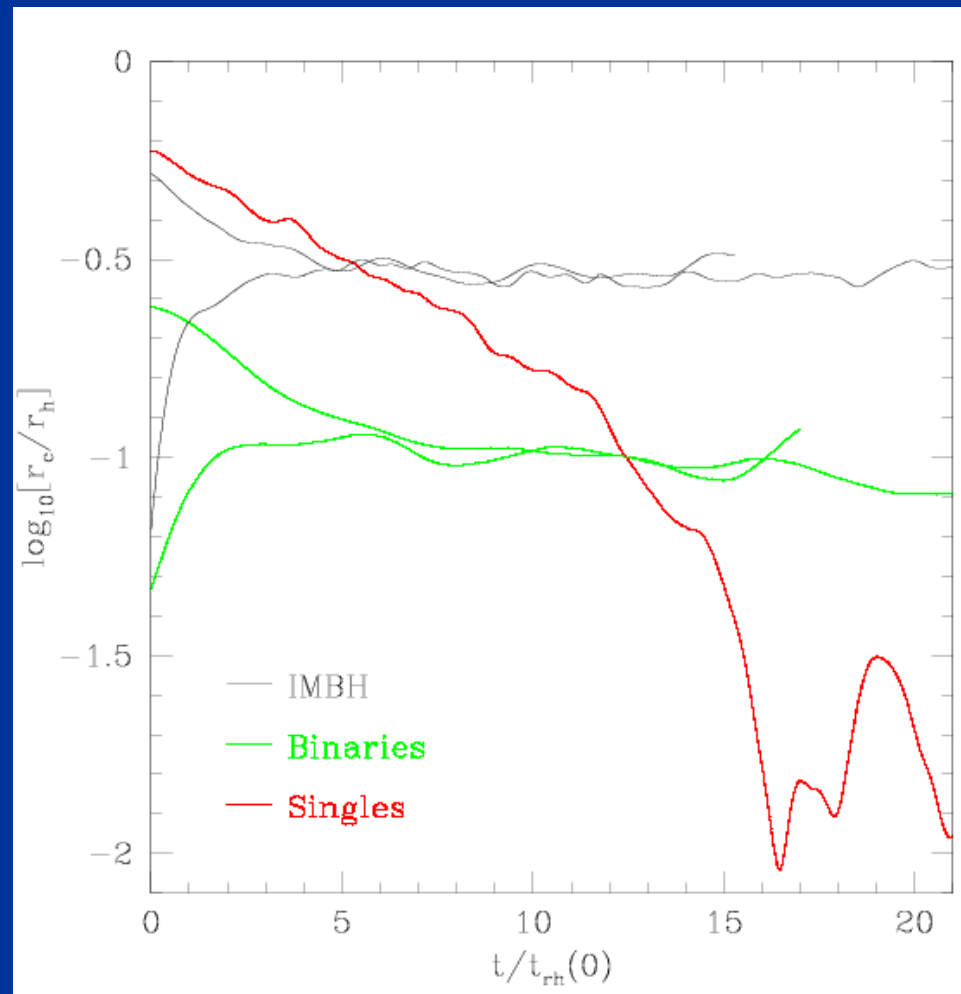
Super-Eddington Emission?



Kollmeier et al. 2006; AGN Eddington ratios
G0900624-v1

Indirect Dynamical Evidence?

- In globular, outer parts expand. Must provide energy.
- Singles are inefficient; need high density.
- Binaries more efficient
- IMBH still more; can lead to high r_c/r_{half}
- Complications must be explored (tidal shocks)



Trenti 2006

Open Question: Mass Function?

- Period, radial velocity of companion would give lower mass limit **One example would establish IMBH**
- Issue: unique identification
**Nearest ULX are few Mpc away!
Even O, B stars are ~24th mag**
- Maybe He II 4686A emission lines?
Some candidates being pursued

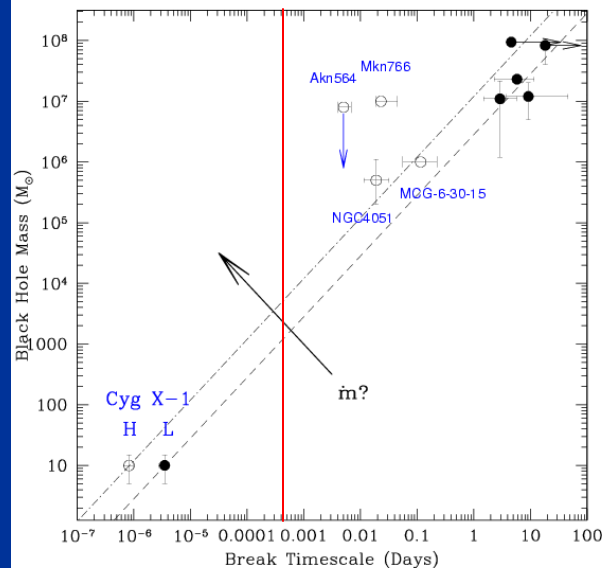
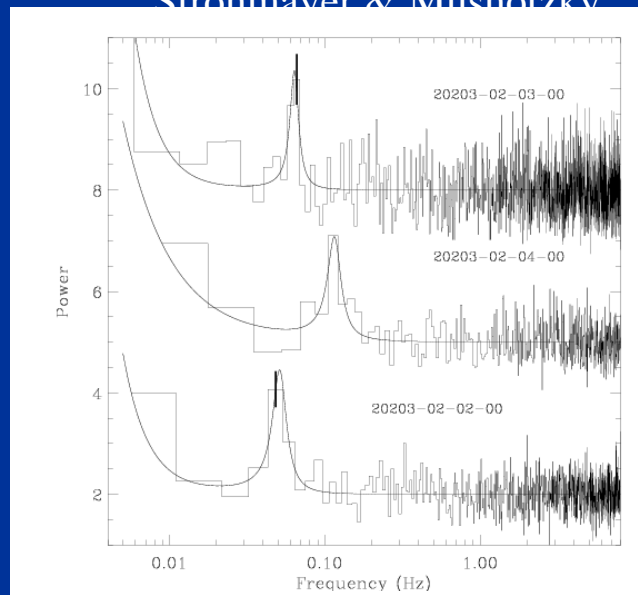
Summary of Observations

- Strong circumstantial evidence
Also timing (QPOs, breaks)
Surrounding nebulae; no strong beaming
- Still missing compelling dynamics
Globular properties are interesting
Work underway for more detailed obs.
comparisons (M. Trenti, MCM, et al.)

Variability

- Expectation: $\text{freq} \sim 1/M$
- No high-frequency power > 1 Hz.
- Definite QPO in one source; maybe two more
- M82 X-1, 26 mHz break
- All consistent with $\sim 10^3 M_{\text{sun}}$, but basic understanding is lacking.
- Why not more QPOs?

Strohmayer & Mushotzky

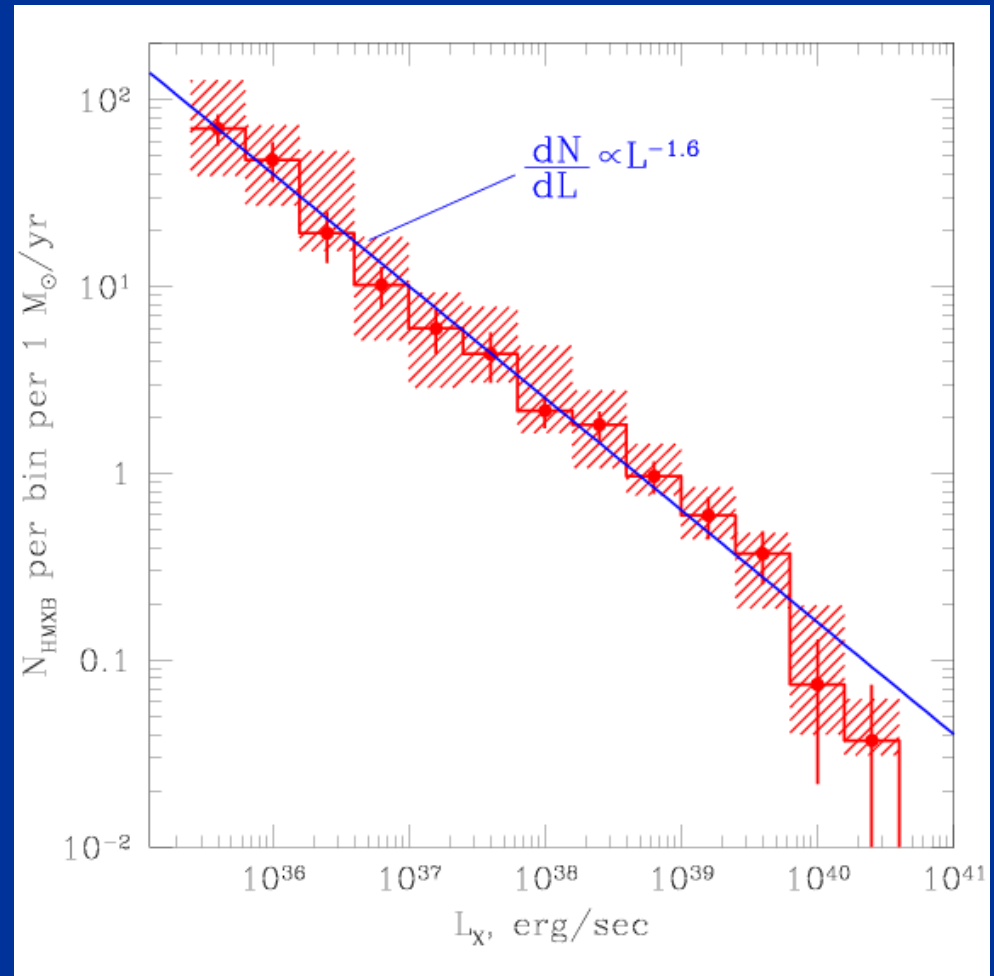


G0900624-v1

McHardy et al. 2004

Lack of Constraint from LF

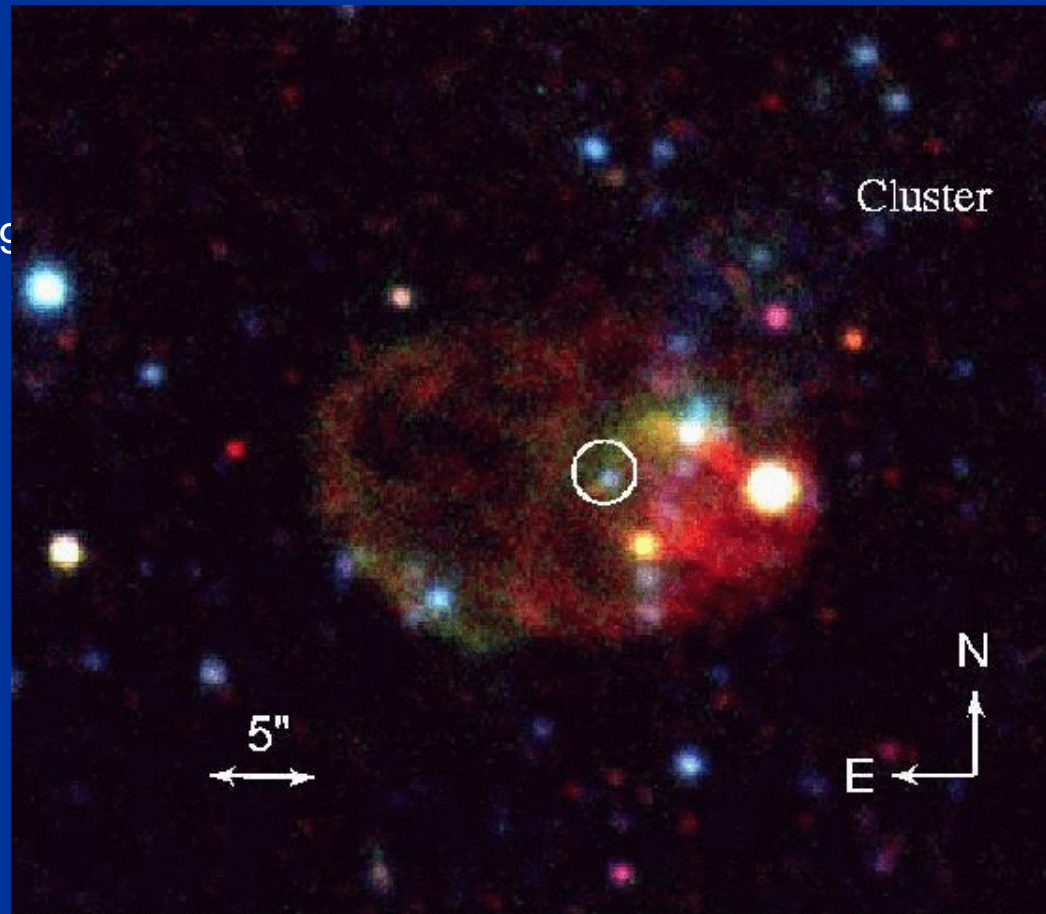
- HMXB LF corrected for star formation rate.
- No break at 10^{39} erg/s, $10 M_{\text{sun}}$ Eddington.
- Evidence against IMBH?
Requires one population?
- No! No break at 10^{38} , either (NS Eddington).
- All models involve new things $>10^{39}$ erg/s; little info.



Gilfanov et al. 2003

Nebulae and Counterparts

- Many ULX in huge (50-800 pc) nebulae
- If beamed, expect $L < 10^{39}$ erg/s, but...
- Few $\times 10^{39}$ erg/s over $\sim 10^6$ years
- O, B stars?
- $P_{\text{orb}} = 62\text{d}$? Kaaret et al.
- He II 4686 emission
300 km/s, NGC 1313?
- P, v_{rad} give mass.



Pakull et al. 2006; NGC 1313 X-2