

*LIGO Laboratory / LIGO Scientific Collaboration*

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# RM3 size and astigmatism of AdvVirgo stable cavity

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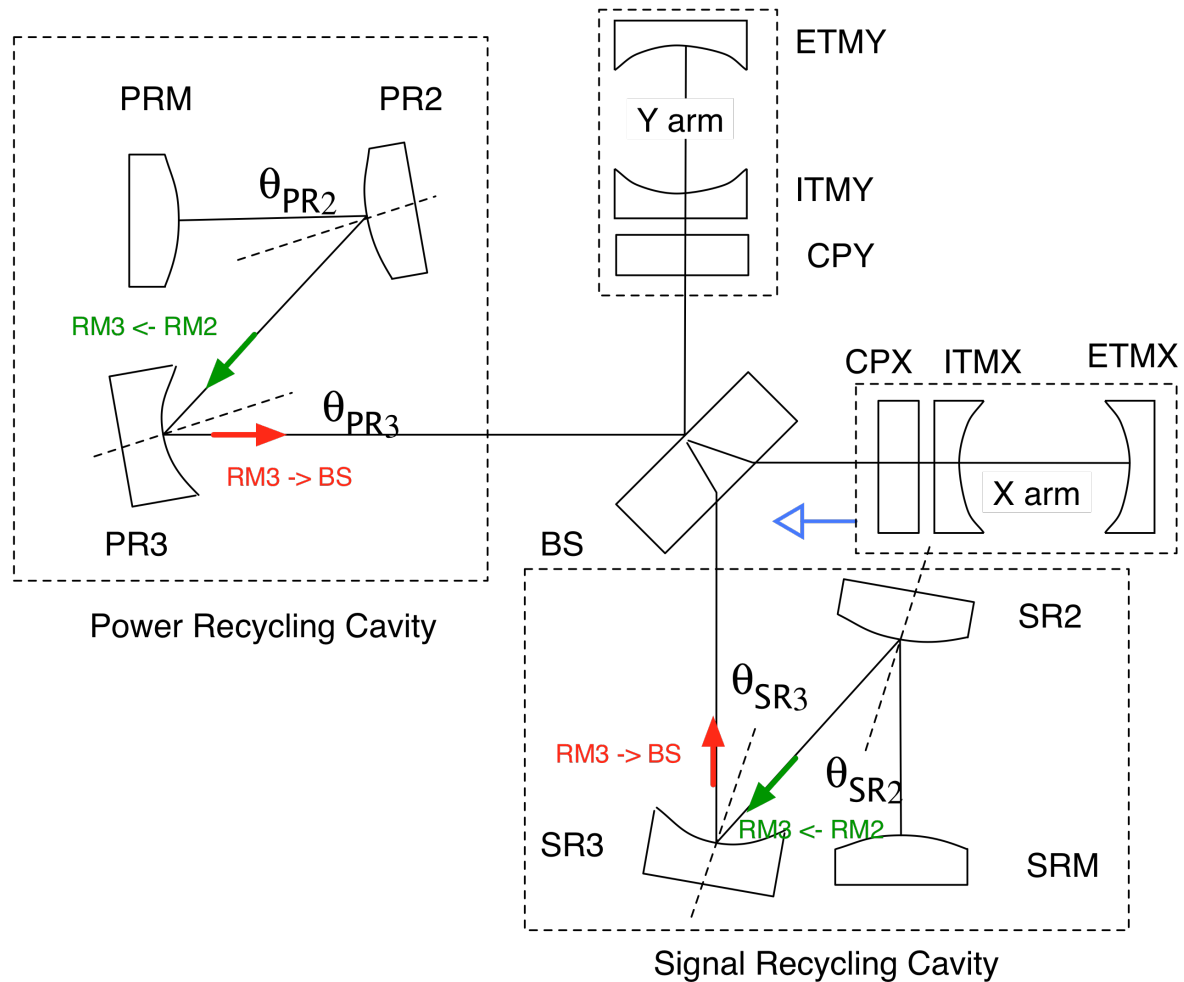
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SIS Stable Coupled Cavity (Power Recycling Cavity and Y-arm, Signal Recycling Cavity and Y-arm) simulation using the following parameters.



Cavity parameters : new Power Recycling ( old PRC ) / SRC

ITM.aperture = 0.35  
 ITM.thickness = 0.2  
 ITM.opt.T = 0.007  
 ITM.opt.R = 1 - ITM.opt.T - 37.5ppm  
 ITM.opt.ROC = 1416

ETM.aperture = 0.35  
 ETM.thickness = 0.2  
 ETM.opt.T = 10ppm  
 ETM.opt.R = 1 - ETM.opt.T - 37.5ppm  
 ETM.opt.ROC = 1646

BS.aperture = 0.55  
BS.thickness = 0.065

RM.aperture = 0.15  
RM.thickness = 0.1  
RM.opt.T = 0.0464 / 0.11  
RM.opt.R = 1 - RM.opt.T  
RM.opt.ROC = -2.853 (-12.26288) / -2.866

MMT2.aperture = 0.15  
MMT2.thickness = 0.1  
MMT2.opt.ROC = -2.853 (-2) / -2.866  
MMT2.incident.theta = 0.9 degree

MMT3.aperture = 0.35  
MMT3.opt.ROC = 22.543 (23.0304) / 21.626  
MMT3.incident.theta = 0.9 degree

FPcav.L0 = 2999.8 (3000)

CCav.RM\_MMT2 = 10.027 (10.5) / 9.556  
CCav.MMT2\_MMT3 = 10.12332322 / 9.65211690 (10.69836864)  
CCav.MMT3\_BS = 10.45 (6) / 9.952  
CCav.BS2ITM = 5.499 (5.55728) / 5.4990

#### Notation of field

RM3->BS : field on RM3 going out toward BS (red line in the figure)

RM3<-RM2 : field on RM3 coming from RM2 (green line in the figure)

#### Case compared

RM3 aperture = 35cm, 33cm, 31cm, 29cm, 27cm

AOI on RM2 and RM3 = 0 and 0.9° for PRC and 1.0° for SRC

PRC – Y arm : inject field from RM

SRC – Y arm : CR is anti resonant in SRC.

Signal sideband is generated by shaking ETM.

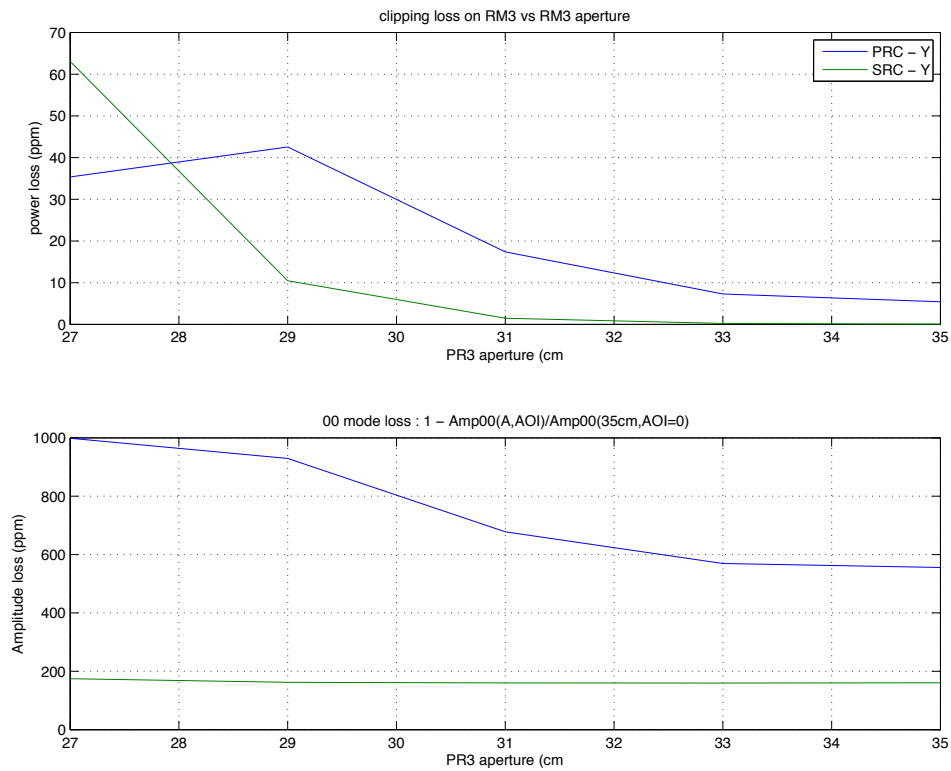
Power in the arm is set to be the same.

## Loss vs aperture (AOI=0.9°)

Top plot :  $1 - \text{Power}(\text{RM3} \rightarrow \text{BS}) / \text{Power}(\text{RM3} \leftarrow \text{RM2})$

Bottom plot :  $1 - \text{Amp00}(\text{RM3 aperture}, \text{AOI}) / \text{Amp00}(35\text{cm}, \text{AOI}=0)$

$\text{Amp00} = \int E(\text{RM3} \rightarrow \text{BS}, \text{aperture}, \text{AOI}) * E(\text{RM3} \rightarrow \text{BS}, \text{aperture}=35\text{cm}, \text{AOI}=0)$



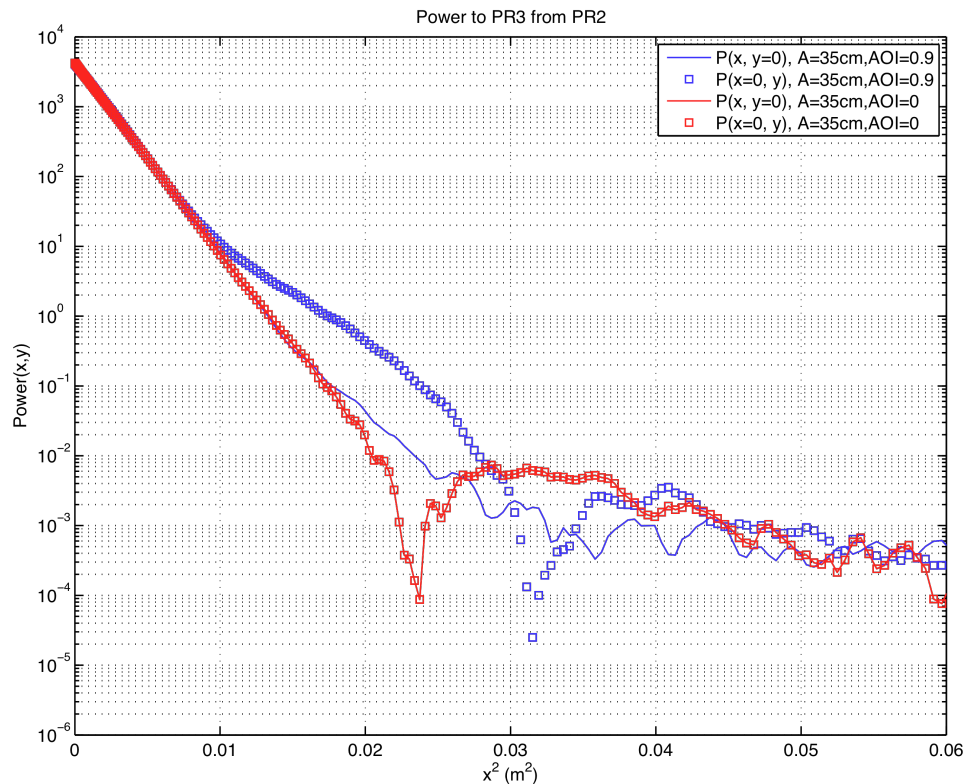
## Effect of finite angle of incidence : Power(RM3 <- RM2)

### PRC – Y arm : new parameter

Comparison of Power distributions with  $\text{AOI} = 0$  and  $\text{AOI} = 0.9^\circ$ , in the x plane (horizontal) and y plane (vertical), with aperture size = 35cm.

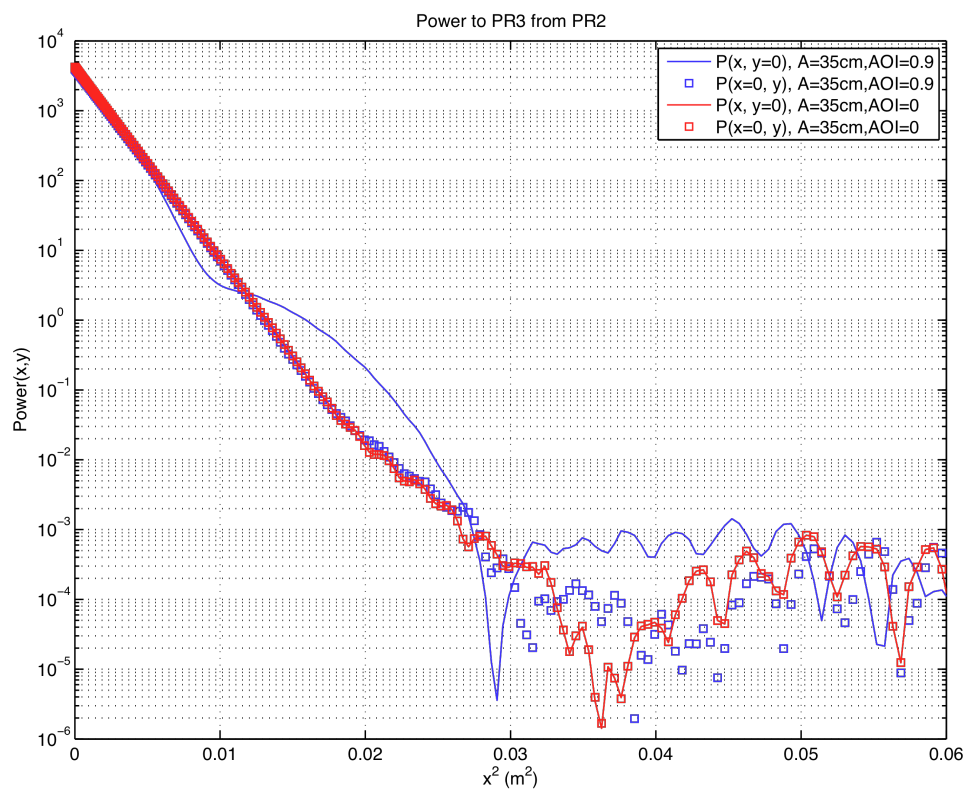
$\text{Log}(\text{power})$  vs  $x^2$ , so a straight line slope means a perfect Gaussian power distribution.  $P(x,y=0)$  is the horizontal distribution in the plane at  $y=0$ , and  $P(x=0,y)$  is the vertical distribution in the plane at  $x=0$ .

With  $\text{AOI}=0$ , the horizontal (red solid) and vertical (red square) distributions are the same. With  $\text{AOI}=0.9^\circ$ , the horizontal distribution (blue solid) is almost the same as no AOI case, but the vertical distribution (blue cross) deviates from the Gaussian shape at around  $x=10\text{cm}$  (0.01 in the plot).



## PRC – Y arm : old parameter

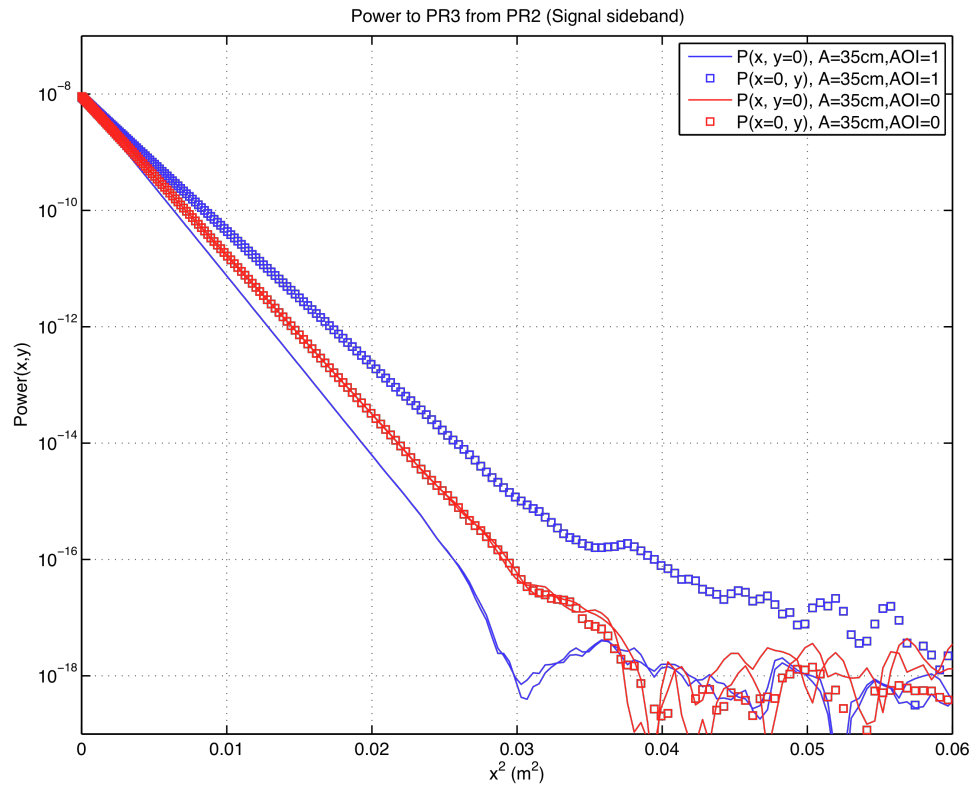
The behavior is different in the configuration using the old parameter set.



## SRC – Y arm

Field structure in the horizontal and vertical planes are the ones in a recycling cavity without AOI, but the ROC(RM2 and RM3) are multiplied or divided by  $\cos(\text{AOI})$ .

The field curvature on RM does not perfectly match with ROC of RM, one direction larger and the other direction smaller.

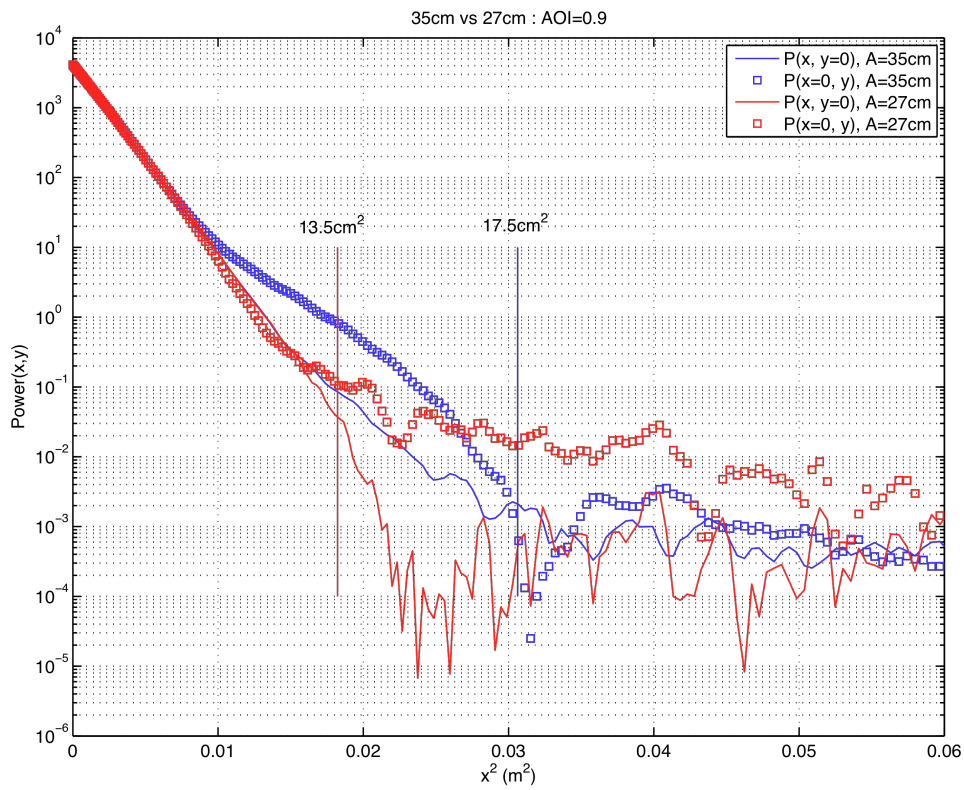


## Effect of different PR3 aperture : Power(RM3 <- RM2)

The following plot compares two cases with aperture 35cm and 27cm.

The horizontal distributions (red and blue solid) do not change much, but the vertical distributions are (red and blue square lines).

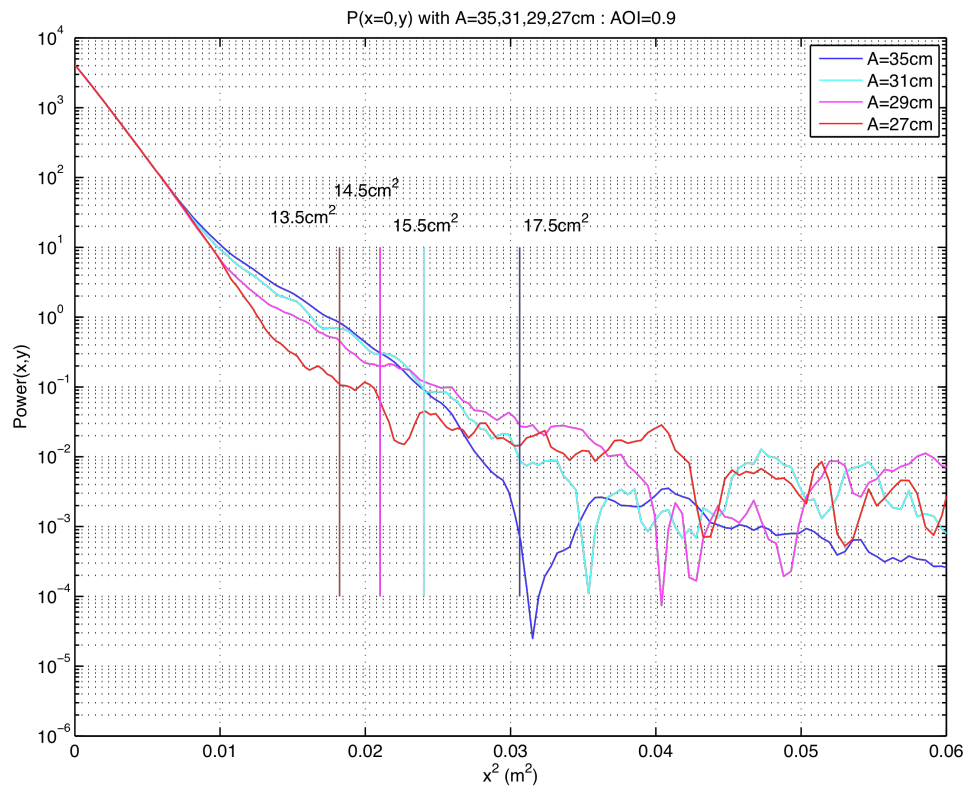
Powers right side of two lines, marking the mirror sizes, are lost.





## Effect of different PR3 aperture : Power(RM3 <- RM2)

The following plot compares the horizontal distributions,  $P(x,y=0)$ , with four apertures.



## Conclusion

Virgo roundtrip loss criteria will be used to impose the aperture limit.