
LIGO Science Reach

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Introduction

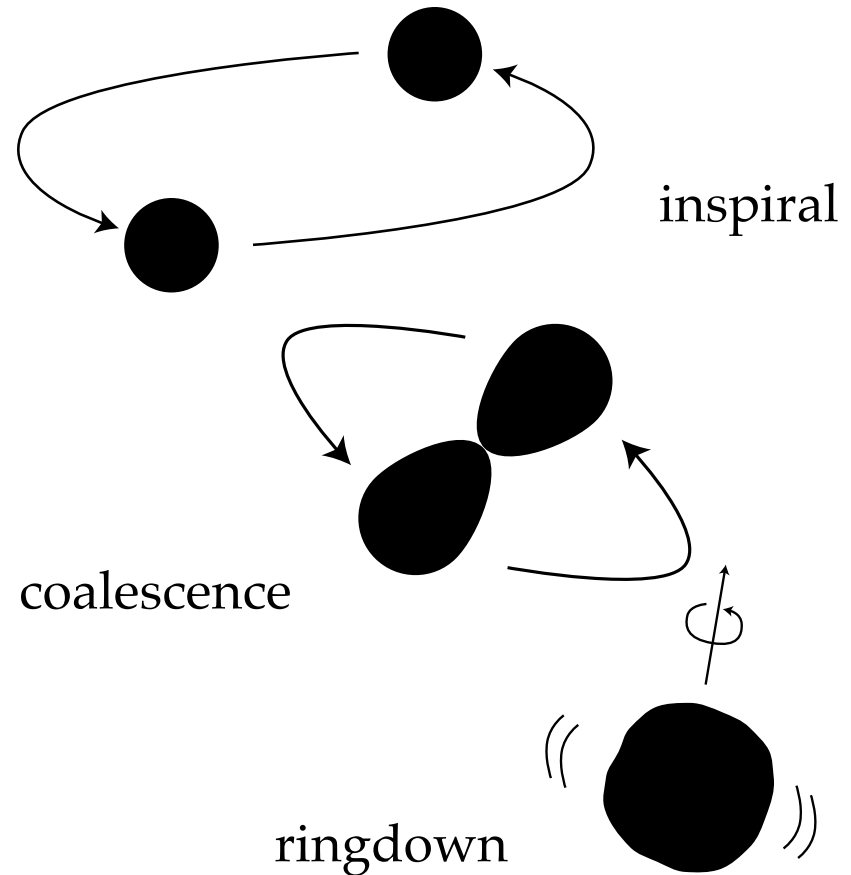
- What is “science reach”?
 - Instrument sensitivity to target science
 - What kind of science, can we expect with first, second generation LIGO instrumentation?
- Conservative approach
 - Focus where speculation can be minimized
 - Miss out on most exciting prospects!
- Outline
 - LIGO I, II baseline recap
 - Compact binary inspiral
 - Stochastic gw signal
 - γ -ray bursts
 - Core-collapse supernovae
 - Summary

LIGO baseline recap

- LIGO I
 - Fixed configuration
 - Peak “sensitivity”
 - $3 - 6 \times 10^{-23} / \text{Hz}^{1/2}$ in 75 – 500 Hz band
- LIGO II
 - Configurable
 - Broad or narrow band operation on a per-IFO basis
 - Peak sensitivity: broadband
 - $1.5 - 3 \times 10^{-24} / \text{Hz}^{1/2}$ in 150 – 600 Hz band
 - Peak sensitivity: narrowband
 - Limited by substrate thermal noise

Binary Inspiral

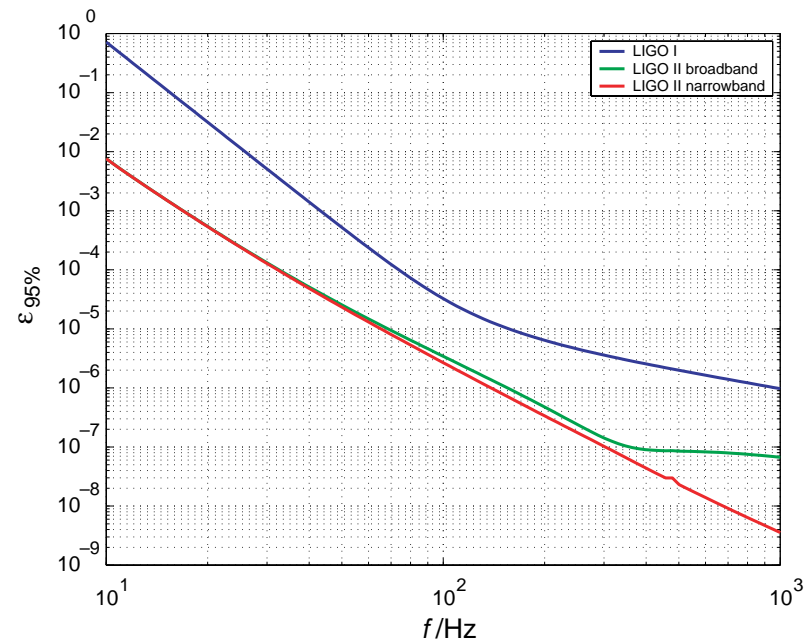
- Reach: Survey volume
 - Distance r such that observed rate is $4\pi r^3 n / 3$
 - Allow for luminosity function, cosmology, etc.
- Parameters
 - $M = 1.4+1.4 M_{\odot}$ binaries
 - $r \sim M^{5/6}$ for $M < 10 M_{\odot}$
 - Expected false rate
 - $< 10^{-4}/y$
 - Corresponds to $S/N \sim 8$
 - $r_{\text{LIGO I}} = 14 \text{ Mpc}$
 - $r_{\text{LIGO II}} = 200 \text{ Mpc}$
 - $x \sim 1.5$ for coherent sum




Periodic Signals

- Focus on pulsars
 - $f_{\text{gw}} = 2f_{\text{pulsar}}$
 - $h \propto \varepsilon = (\Delta I / I)$
- Reach: upper limit on ε
 - 1 yr observation
 - 10 Kpc distance
 - Declination average
 - Significance: 95%
- Theoretical prejudice
 - $\varepsilon < \sim 10^{-6}$
 - From pure Coulomb lattice crust strength

- Observational constraints
 - $\varepsilon < \sim 10^{-8}$ for *old* (recycled) pulsars

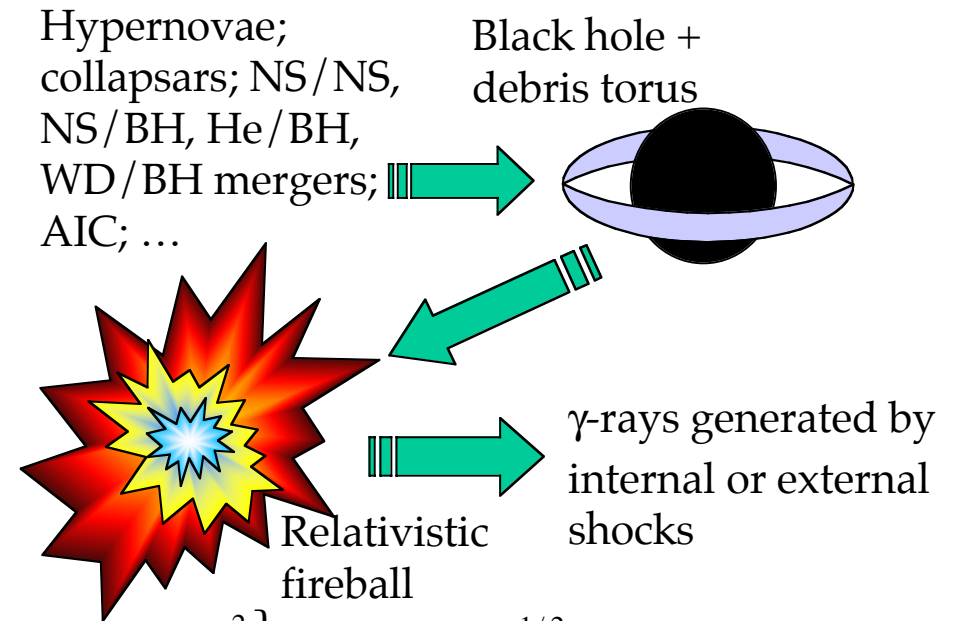


Stochastic Signals

- Single IFO can't separate between signal, noise
 - Reach: Limit on Ω_{GW}
 - GW energy density, as fraction closure density, per log bandwidth
 - 99% significance
 - 1/3 yr observation
 - LIGO I: $3.3 \times 10^{-6} / h^2$
 - LIGO II: $2 \times 10^{-9} / h^2$
- 
- Two detectors respond \sim coherently when $\lambda > d$
 - LHO-LLO: $c/d = 100$ Hz
 - LLO-ALLEGRO: $c/d \gg$ KHz
 - Theoretical prejudice:
 - Inflation: $\Omega_{\text{GW}} \sim 10^{-14}$
 - Cosmic Strings: $\Omega_{\text{GW}} \sim 10^{-11}$
 - In-band observational constraints:
 - N.synthesis: $\Omega_{\text{GW}} \sim 10^{-5}$

γ -ray bursts

- γ -ray burst triggered by formation of $\sim M_{\odot}$ bh
 - Expect grav.-wave burst
- Individual grav.-wave bursts not detectable
 - Distance, amplitude, etc., conspire against
- Look for statistical association:
 - LIGO II bound equiv to $\sim 0.3M_{\odot}$ in grav.-waves at $z = 1/2$



$$h_{\text{Det}}^2 < h_{95\%}^2 = \begin{cases} (1.35 \times 10^{-22})^2 \\ (2.5 \times 10^{-23})^2 \end{cases} \left\{ \begin{array}{l} \left(\frac{T}{0.2\text{s}} \frac{1000}{N_{\text{on}}} \right)^{1/2} \\ \end{array} \right. \begin{array}{l} \text{LIGO I} \\ \text{LIGO II} \end{array}$$

Core-collapse supernovae

- Assume:
 - LIGO II observation of extra-galactic SN
 - Light curve fixes collapse to within 1h
 - LIGO I observation in galactic neighborhood
 - Neutrinos fix collapse to within 1s
 - Waveform unknown
 - Focus on detector-detector x-correlation
 - 1 KHz signal bandwidth
- Reach:
 - Mass fraction ϵ converted to gravitational waves
- LIGO II:
 - $\epsilon_{95\%} < 24\%$ for SN at 15 Mpc
 - Expected rate 3/y
- LIGO I:
 - $\epsilon_{95\%} < 2 \times 10^{-4}$ for SN at 55 Kpc
 - Expected rate 1/30y
- Theoretical prejudice
 - $\epsilon < 10^{-7} - 10^{-8}$

Summary

- LIGO I bounds the possible
 - Bound outside estimates on inspiral rates
 - Upper limits probes prejudice on pulsar crust strength upper bound
 - Improve in-band limit on stochastic GW background
 - Possible physical bound on SN efficiency
- LIGO II challenges theory
 - Observe several NS/NS inspirals per year
 - Measure deformation of nearby pulsars
 - Improve limits on stochastic background
 - Maybe explore γ -ray burst model
 - Physical bound on SN efficiency