



The *STACK-SLIDE* Search

Initial Report: PULG F2F UWM June 2003



Gregory Mendell, Mike Landry
LIGO Hanford Observatory



Initial *STACK-SLIDE* Proposal

- Mendell/Landry at LHO to code stack slide algorithm based on Brady/Creighton gr-qc/9812014
- We are in the very preliminary stages of this project, trying to answer questions like
 - Is anyone else planning on working on this (emailed Creighton/Brady/Riles/Chin)?
 - Is there any known problem with stack slide? Is Hough all we need?
 - Do we need to modify B/C algorithm? Stack slide SFTs, DeFTs, or F-stat?
- Algorithm will be coded under LAL, and search run under LDAS
 - Driver code will be available to all (detailed understanding of LDAS not required)
 - Parallel search; exploit ~THz LDAS computing power
 - Efficient I/O of SFTs, results database (or frame output) inherent in LDAS
- We will have a more complete proposal/progress report at the June F2F
- Code written and working by the August LSC meeting



Definitions

- T_0 = observation time.
- M = number of data segments (number of stacks).
- N = number of data points in one segment.
- N_T = total number of data points in T_0 .
- A = signal amplitude.
- σ = square root variance of the noise.



Coherent Search

$$x = s + n = A \cos(2\pi f t + f_0) + n$$

$$\tilde{x} = DFT(x)$$

$$\tilde{x}^* \tilde{x} = \left(\frac{ANM}{2} \right)^2 + (NMs \pm NMs) + \text{cross-term}$$

$$\langle \tilde{n}^* \tilde{n} \rangle = NMs^2$$

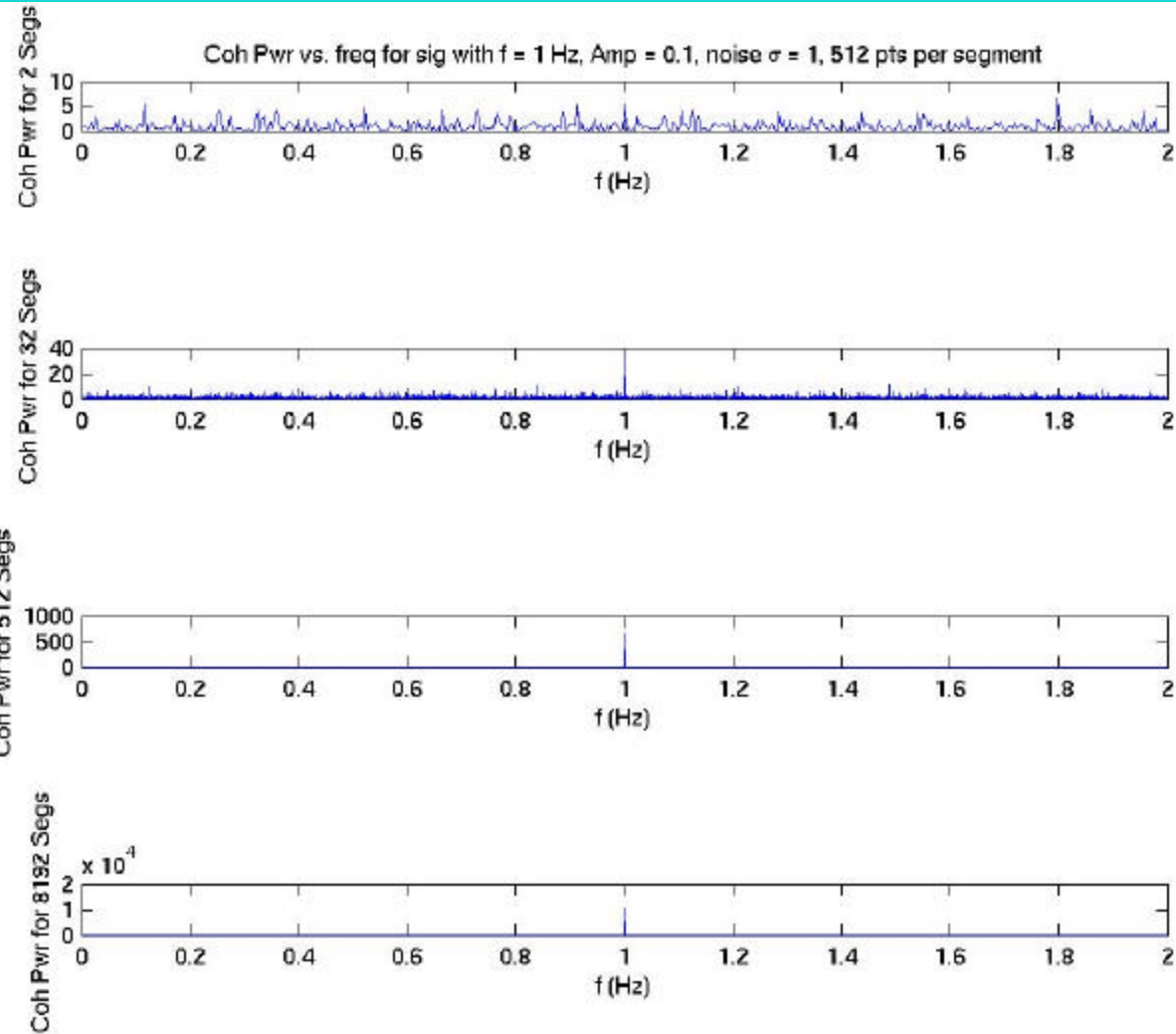
$$\text{For } A^2NM > 4s^2: SNR \sim \sqrt{\tilde{x}^* \tilde{x} / \langle \tilde{n}^* \tilde{n} \rangle} = \frac{A}{2s} \sqrt{NM} = \frac{A}{2s} \sqrt{N_T}$$

$$\text{Detection if: } \frac{A}{2s} \sqrt{NM} \gg 1$$

$$\text{False Alarm Rate: } C_{false} = e^{-\frac{A^2}{4s^2} NM}$$



Coherent Power vs. Freq





STACK-SLIDE Search

$$x = s + n = A \cos(2\pi f t + f_0) + n$$

$$\tilde{x} = DFT(x)$$

One stack: $\tilde{x}^* \tilde{x} = \left(\frac{AN}{2}\right)^2 + (Ns \pm Ns) + \text{cross-term}$

$$\langle \tilde{n}^* \tilde{n} \rangle = Ns^2$$

For $A^2N < s^2$: $SNR \sim (1 \pm 1/\sqrt{M}) + \frac{1}{8} \frac{A^2N}{s^2}$ **(Ave M stacks)**

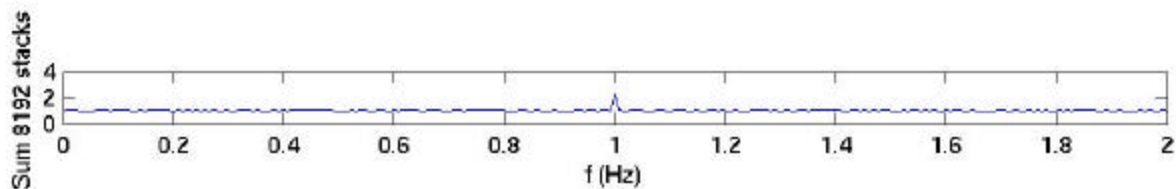
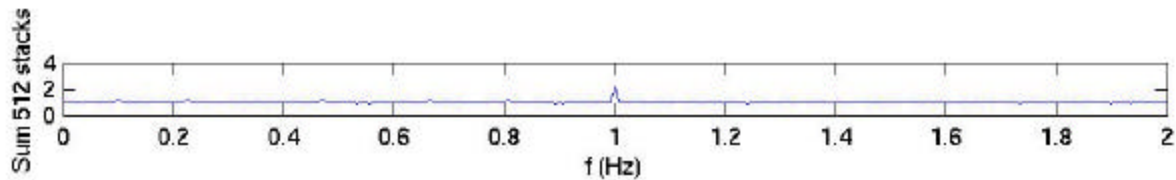
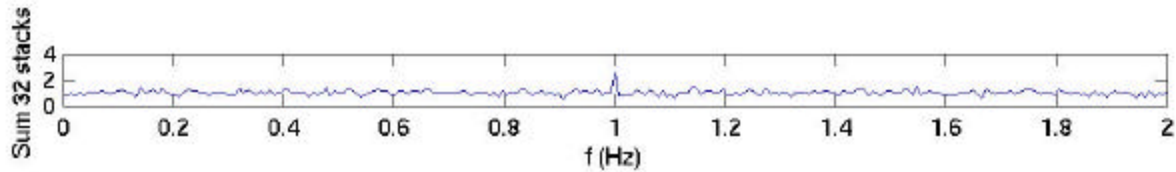
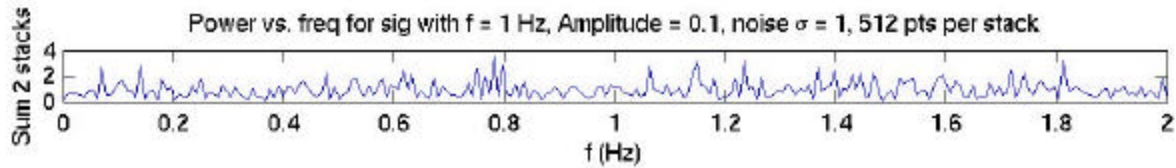
Detection if: $\frac{A}{\sqrt{8s}} \sqrt{NM}^{\frac{1}{4}} \gg 1$

False Alarm Rate: $C_{false} = 1 - \frac{g(M, SNR)}{(M-1)!}$ (Brady/Creighton gr-qc/9812014)

g = Incomplete Gamma Function

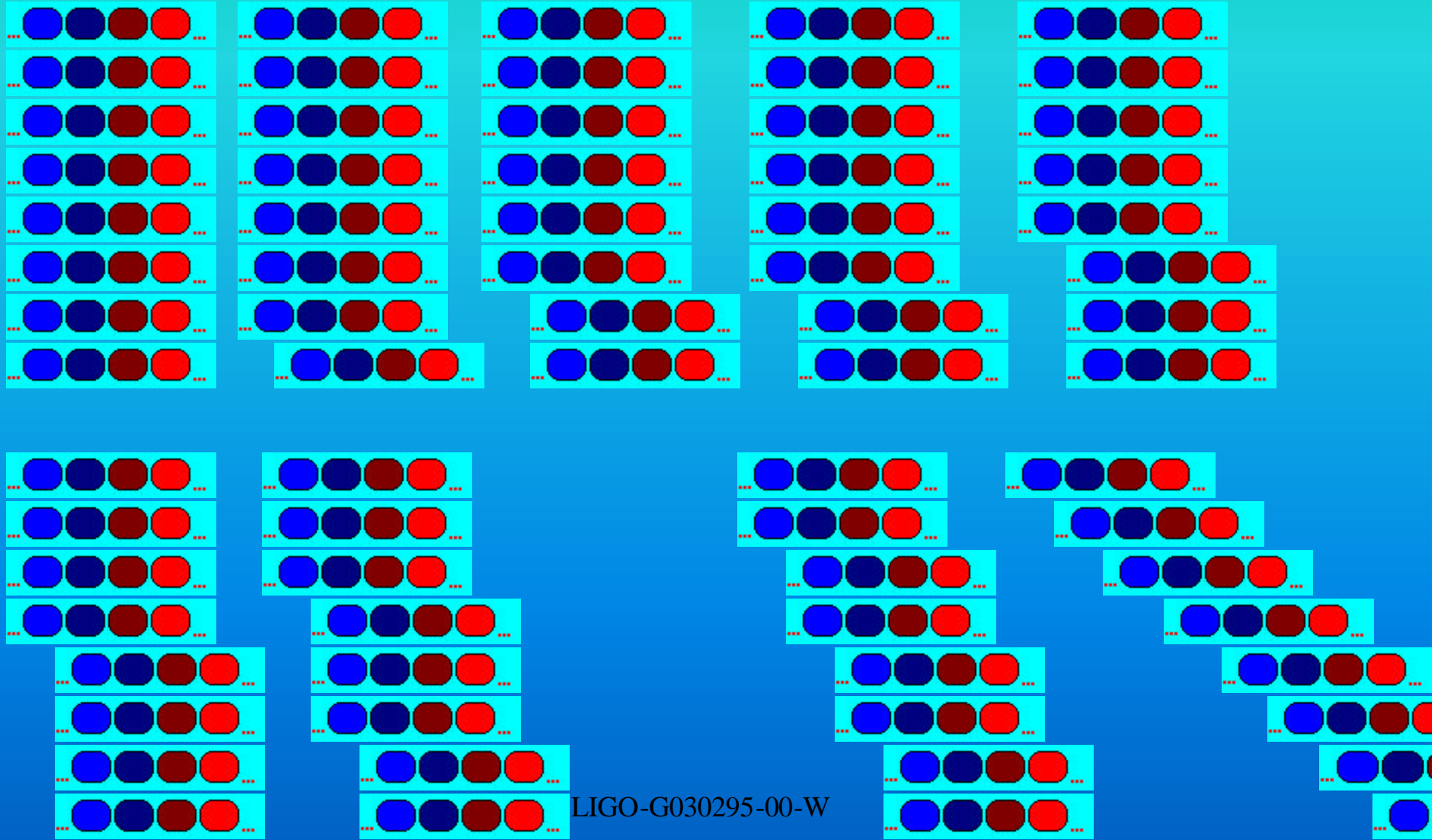


STACK-SLIDE Power vs. Freq





Stacking and Sliding...





Complexity?

Complexity STACK-SLIDE = $O(MN\log_2 N) + O(NM^2)$?

Complexity SFT Coherent Per Sky Position = $O(MN\log_2 N) + O(\mathbf{D}kNM^2)$?

Complexity Coherent FFT Resampled Time Series Per Sky Position = $O(MN\log_2 MN)$?



We are still working to...

- Understand the Algorithm.
- Understand the Computational Complexity.
- Understand the Statistics.



Brady/Creighton algorithm and potential modifications

Resample?
Or use SFTs,
DeFTs, F-stat
From LALDemod

- The algorithm shown in the Flowchart is iterated in a hierarchical approach

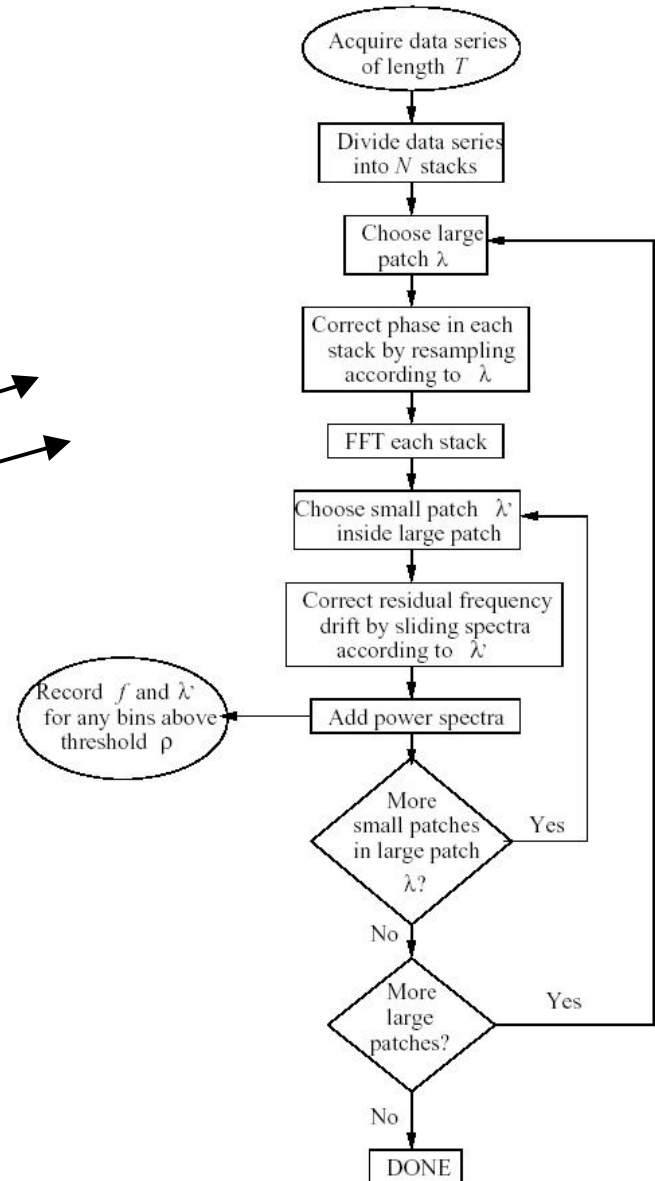


FIG. 1. A flowchart representation of the *stacked slide* algorithm to search for sources of continuous gravitational waves. Notice that the computational cost of sampling the fine grid is reduced by sliding the power spectra, rather than re-computing an FFT for each point on the fine grid.

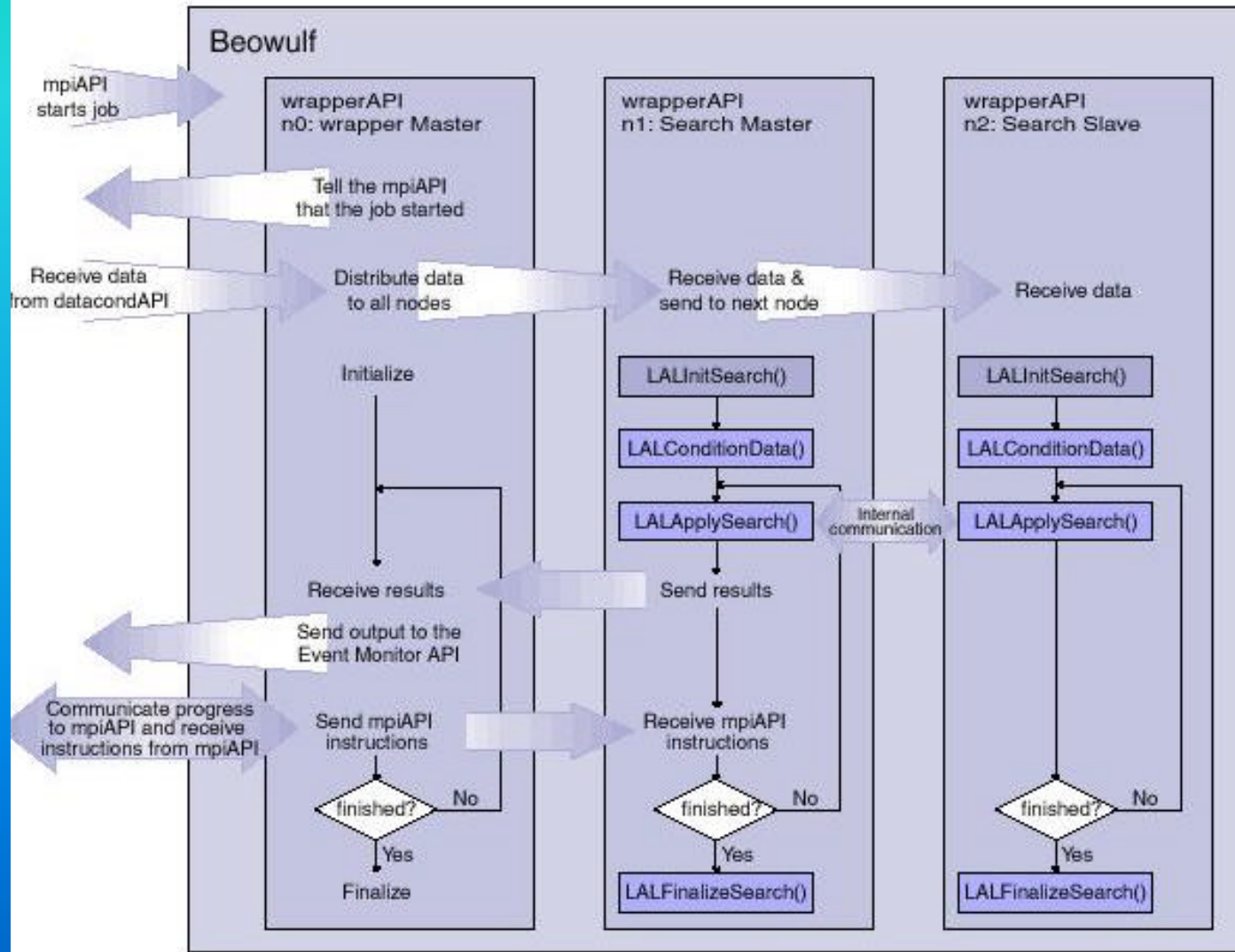


Will Provide LDAS, LAL, & Driver Code

- LDAS code will be based on knownpulsardemod DSO.
- LAL parameter space metric code exists.
- Need LAL STACK-SLIDE function.
- User-friendly driver code that anyone can run.



LDAS Code To Write





Example Driver getFstat

```
Usage: ./getFstat_v1.tclsh <site> <ifo> <start_time> <duration>
<templateFreq0> <band_width> <sft_time> <framecachefile> <templatefile> <outputdatabase>
<outfile> [<run>]
```

Example:

```
./getFstat_v1.tclsh lho H1 729976096 8192 1283.5 2 2048
SFTFrameCache_H1_040203.txt testJ1939.params ldas_tst testFstat.xml run
Starting Thu Jun 12 12:51:54 PDT 2003 LDAS job with LJrun at lho;
User: gmendell; Job id: LDAS-WA890236.
LDAS job succeeded.
Total time to run job = 76 seconds.
```

```
[gmendell@vulcan scripts]$ less testFstat.xml
```

```
...
```

```
<LIGO_LW Name=":data:Container(Vect):Frame">
```

```
<Dim Scale="1.2207031250000000e-04"
```

```
Start="1.2825000000000000e+03" Unit="hz">16388</Dim>
```

```
Name="data" Type="Local">
```

```
2.6003204903121175e+00,2.3834808600241506e+00,2.7261332694330522e+00,...
```

LIGO-G030295-00-W