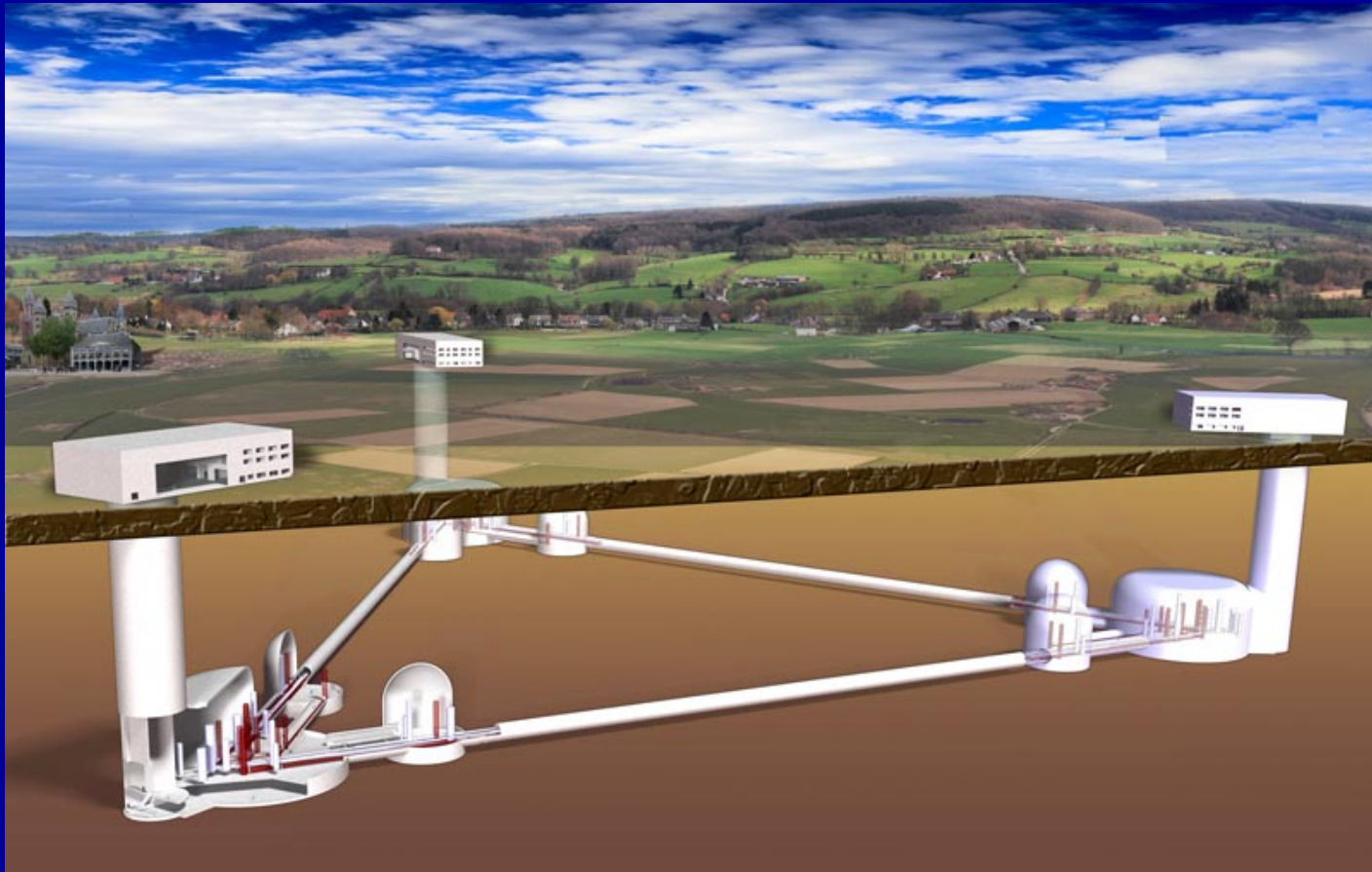


GW sources from a few Hz to a few kHz

Cole Miller, University of Maryland



Outline

- The most massive white dwarfs
- Long lead times for telescopes
- Nonzero eccentricities?
- Intermediate-mass black holes
- High freq: NS masses, radii, and modes
- High freq: SN bursts

Frequency of Waves

Object of average density ρ has maximum frequency $\sim(G\rho)^{1/2}$ for gravitationally bound object

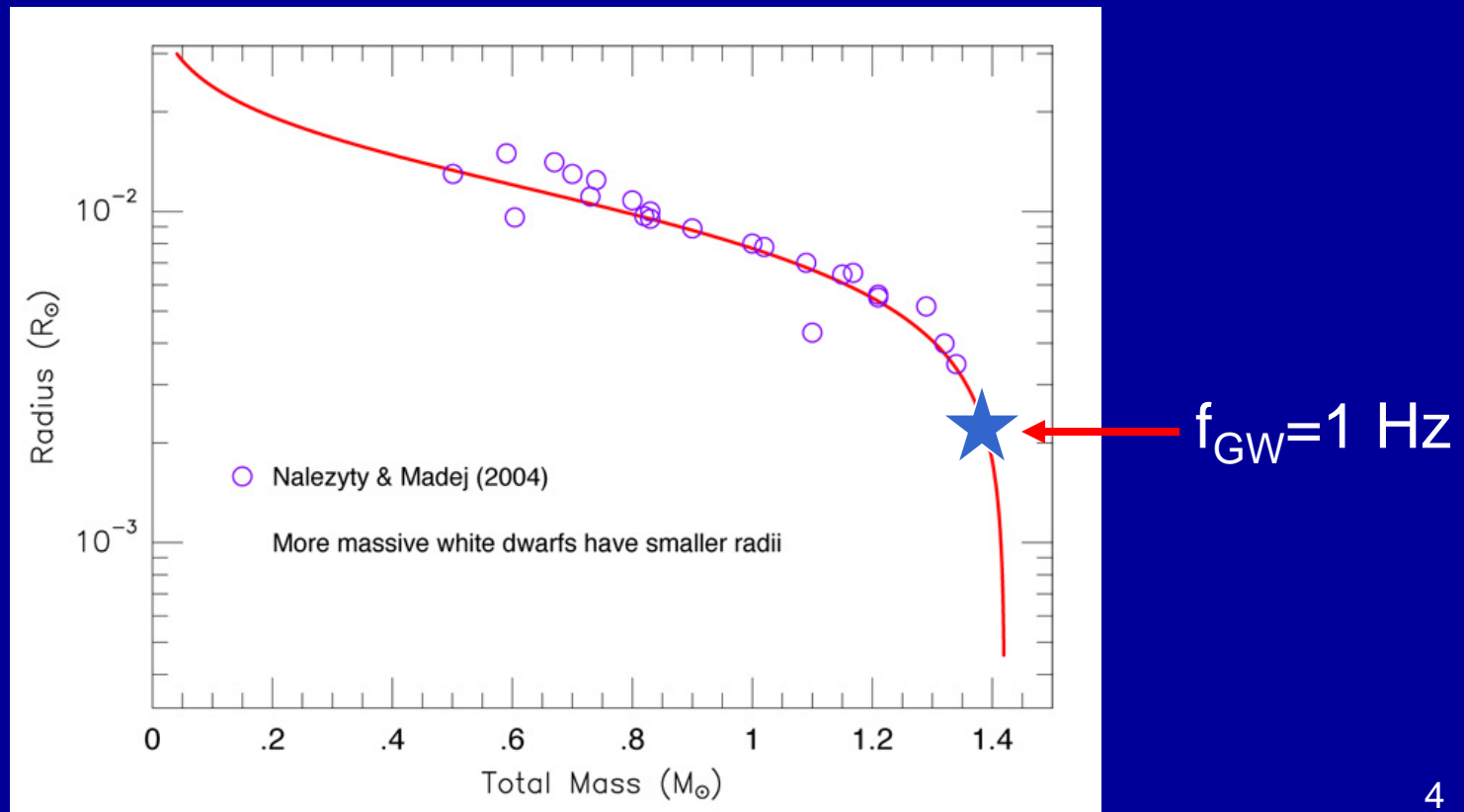
True for orbit, rotation, or full-body pulsation

Neutron star: $\sim 1200\text{-}2000$ Hz

White dwarf: up to ~ 1 Hz (but see later)

The Most Massive WD

- $\sim 10^{8-9}$ WD binaries in Milky Way
- Even small fraction with $M \sim 1.4 M_{\text{sun}}$ gives large number; new category of sources



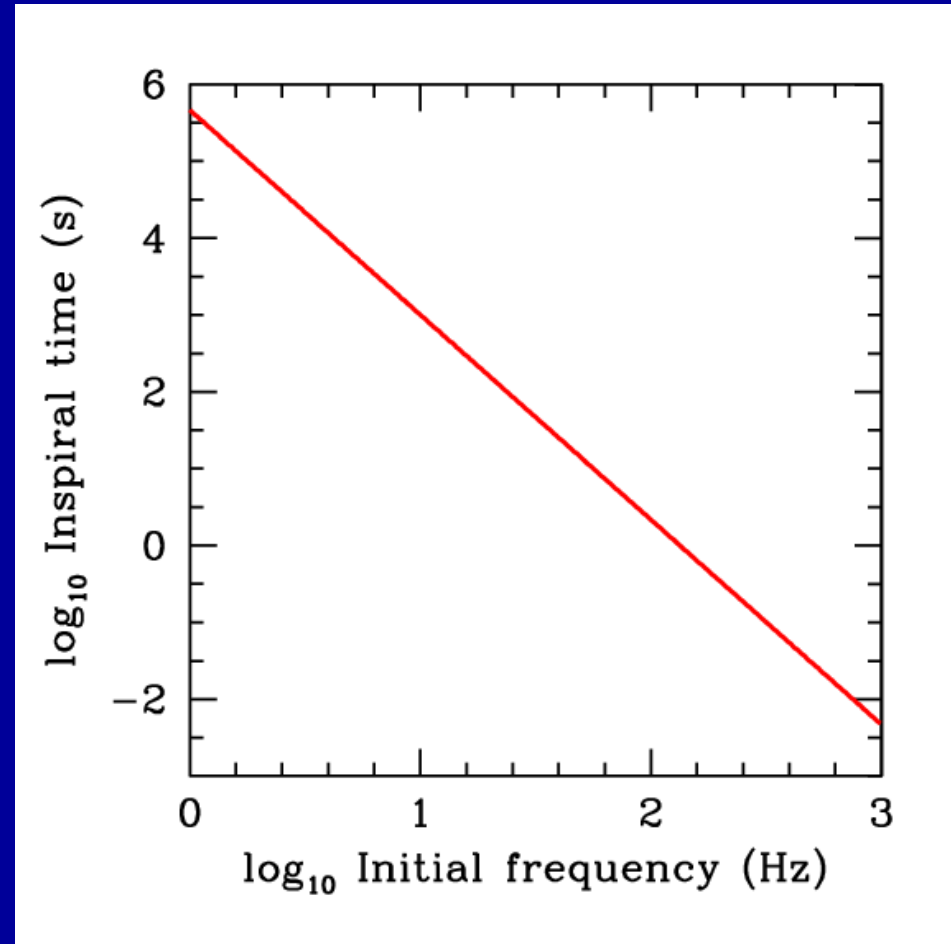
Who Cares About Massive WD?

- Precise maximum mass depends on composition, other properties
- Massive WD (in binaries with normal stars) possible Type Ia SNe progenitors
- Mergers would be spectacular but short-lived EM events

How much lead time do we have?

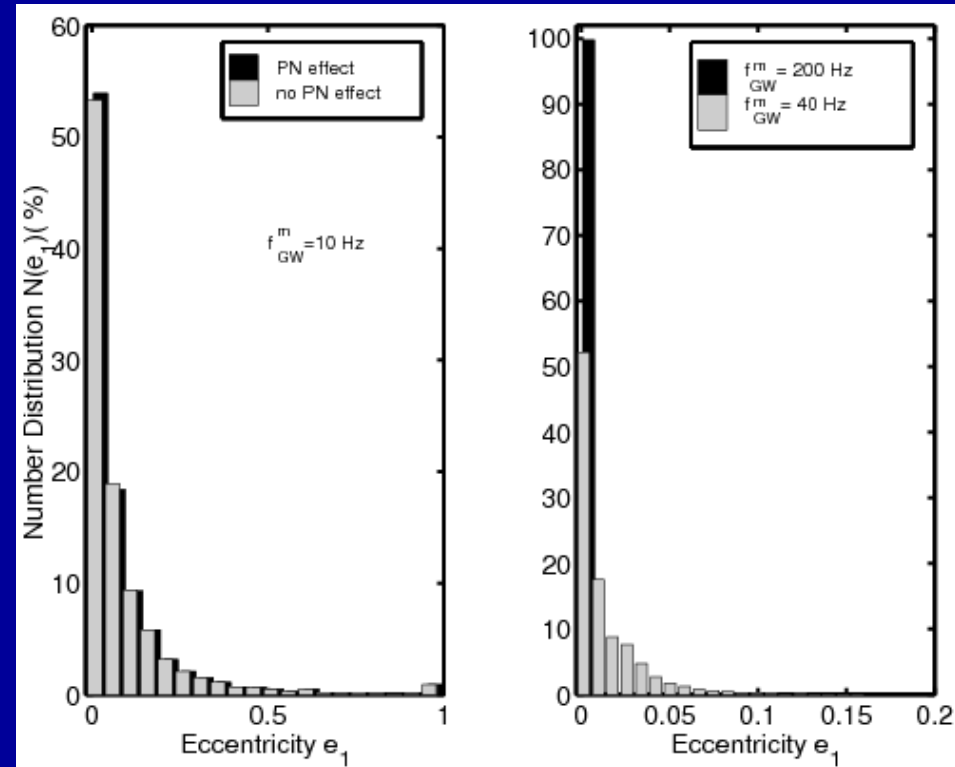
Advance Warning of Merger

- EM counterparts to mergers: lots of info!
Precise localization
Nature of transients
- Time to merger scales as $f_{\text{init}}^{-8/3}$
- At 3 Hz, could be identified hours in advance
- Key: how soon could GW be localized?
Rotation of Earth?



Nonzero Eccentricities?

- Usually, think of binary GW as circular
~true for >10 Hz or field binaries
- Dynamical interactions can change, e.g., Kozai in dense systems
Eccentric Kozai
- $e \sim 1/f$ for $e \ll 1$
- Low freq important for inferring dynamic origin



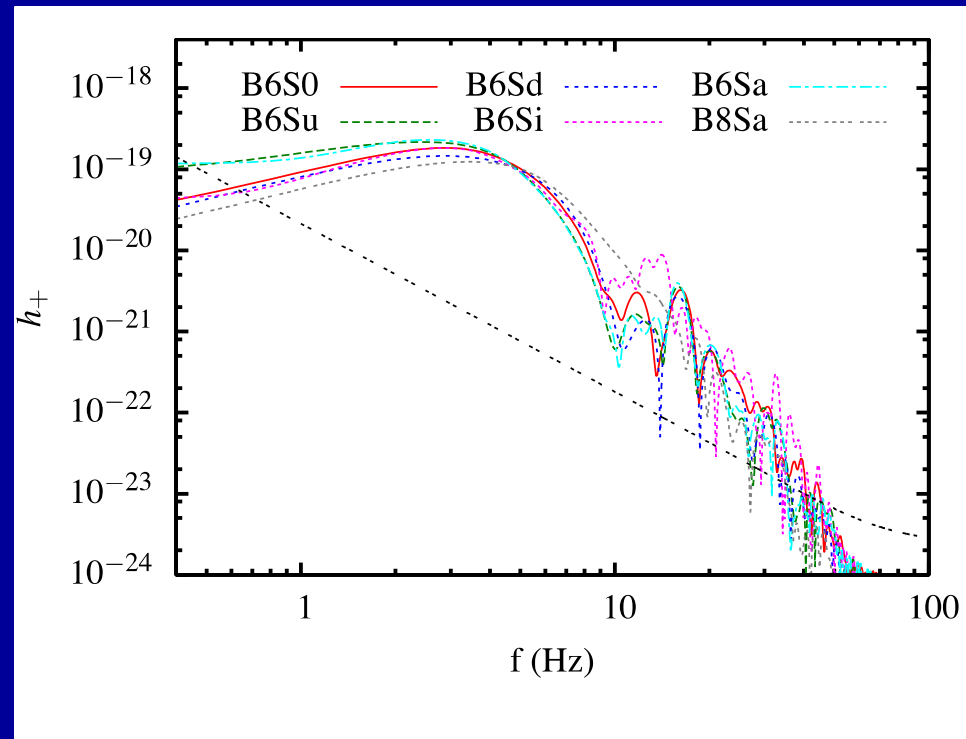
L. Wen 2002

Following Miller & Hamilton 2002

Plunges into IMBHs

Haas et al. 2012

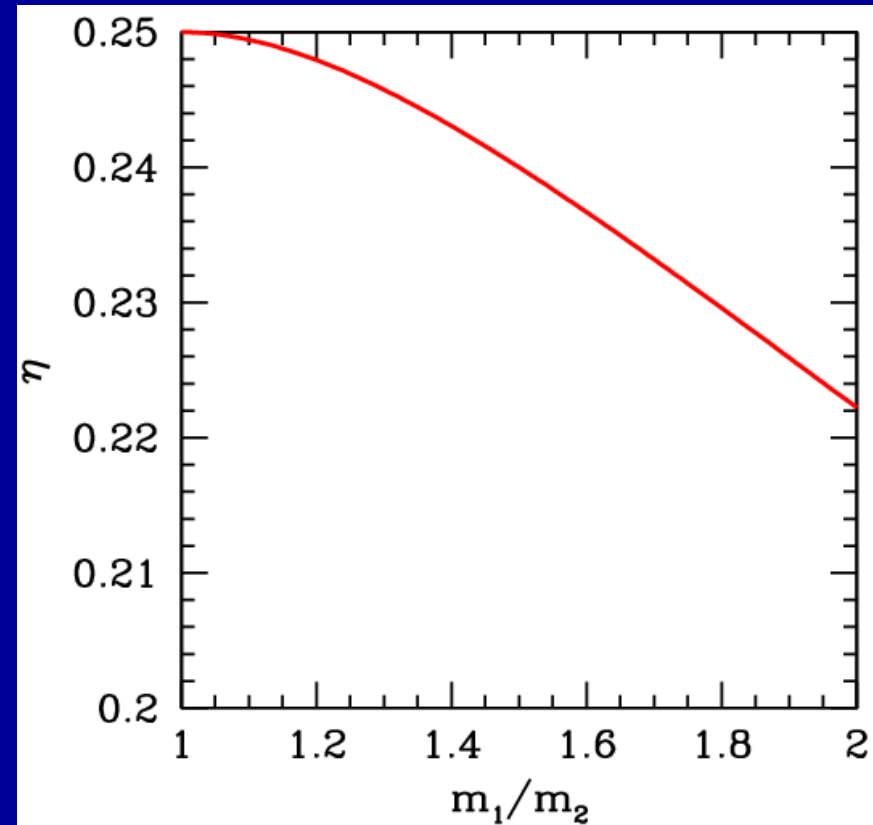
- You can get some leakage to higher freq with plunge
- WD disrupted but bulk moves along same trajectory
- Evidence of IMBH?
This, or IMBH-IMBH, could be first direct proof



$10^3 M_{\text{sun}}$ BH, $1 M_{\text{sun}}$ WD, penetration factors of 6 and 8; assume 20 kpc for distance of source

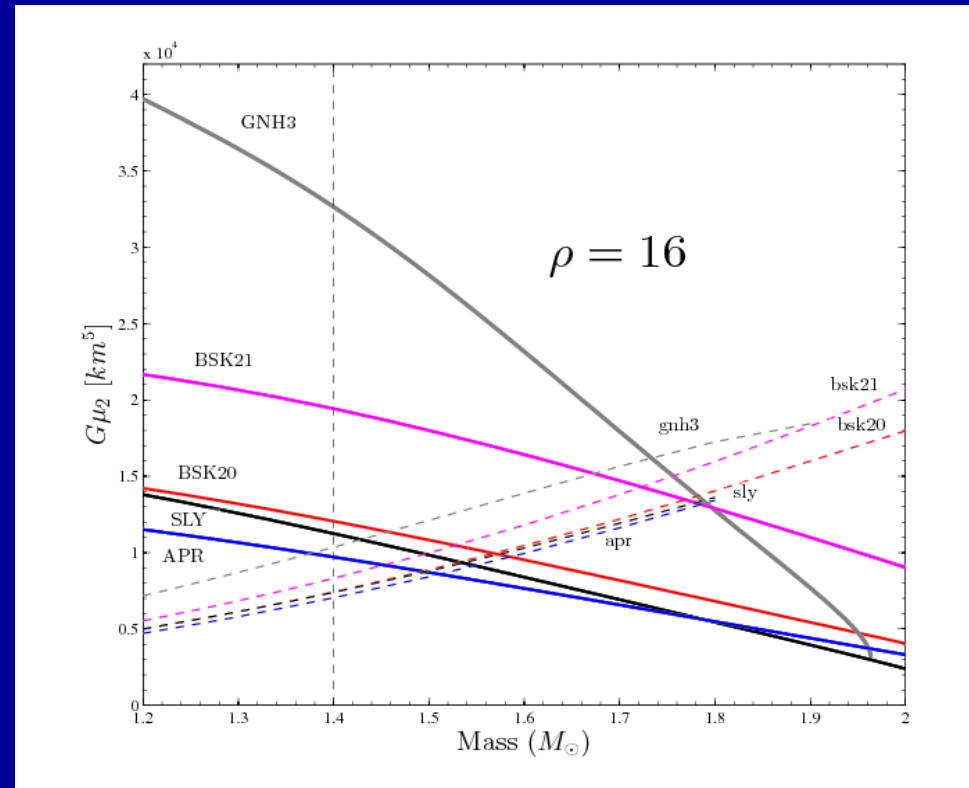
NS and BH masses

- Chirp mass is easy:
 $df/dt \sim \eta M^{5/3} f^{11/3}$
- Getting both masses requires symmetric mass ratio $\eta = m_1 m_2 / M^2$
- Need higher-order, high freq effects in GW
- aLIGO/Virgo at SNR=15:
 $\Delta\eta \sim 0.007$
- Bad for NS-NS; okay for NS-BH, but better high-freq sensitivity is a must!



NS Radius: Phase Accumulation

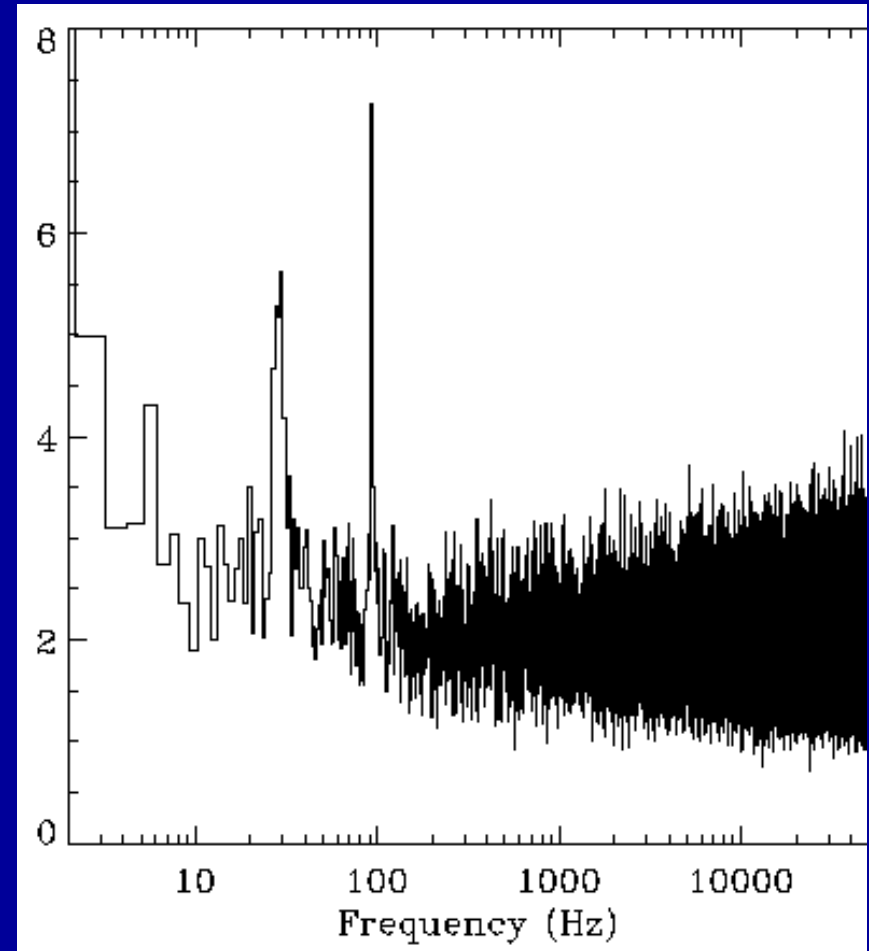
- Radius: key EOS unknown
- Deviation from point mass: accumulated tidal effects
- For aLIGO, can measure tidal param; $\text{SNR} > 30$ can distinguish EOS, barely
- Higher sensitivity at high frequencies would allow fairly precise measurement of tidal parameter, hence radius



Damour et al., arXiv:1203.4352

NS Modes

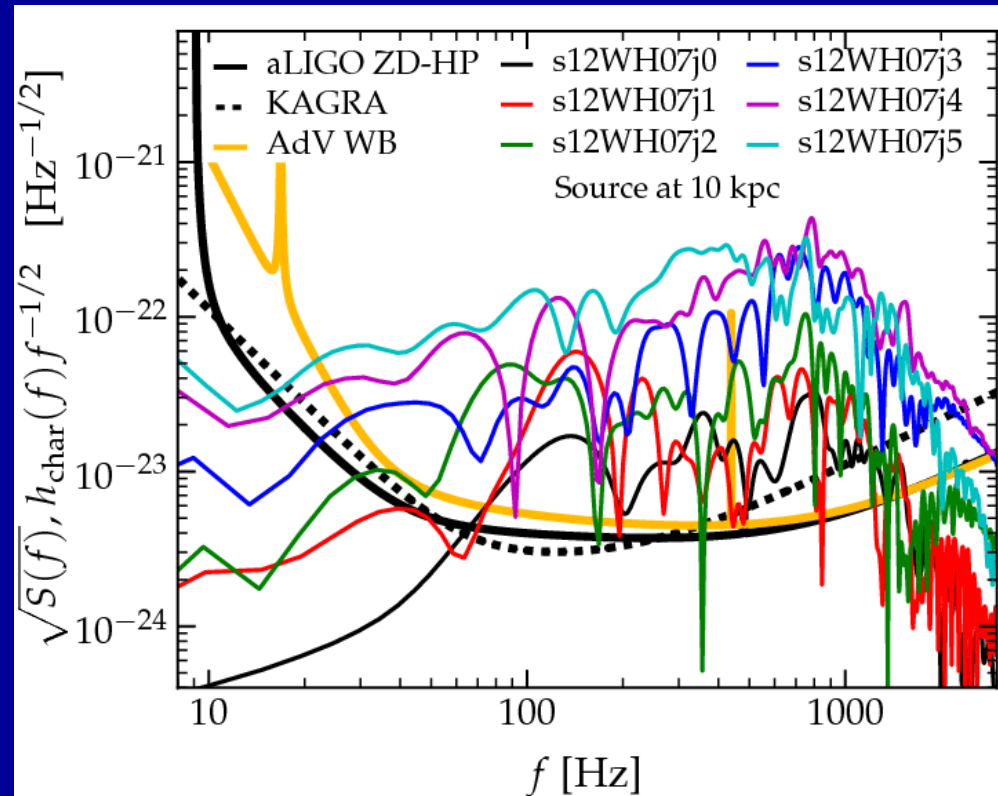
- NS seismology could tell us a lot!
- Indeed, QPOs have been seen
- But...
- Crust has $\sim 1\%$ of M , I ; very weak GW
- If detectable, need huge, transient perturbation at main body freq: ~ 2000 Hz



QPOs from SGR 1806-20 superburst
Strohmayer 2007

GW from Supernovae

- $> \sim 10\%$ chance for MW SN (~ 10 kpc) in decade
- Much uncertainty about mechanism!
- GW (+ ν) will give invaluable info
- High freq are key



Ott et al. 2012

Conclusions

- The ~few Hz range contains qualitatively new sources: heavy WD and IMBH
- Long lead time will allow pointing of large telescopes if the direction can be established to within a few degrees
- The ~few kHz range gives us prospects of unique measurements of NS radius, many measurements of NS mass, and new insights about supernovae

Amplitude of Gravitational Waves

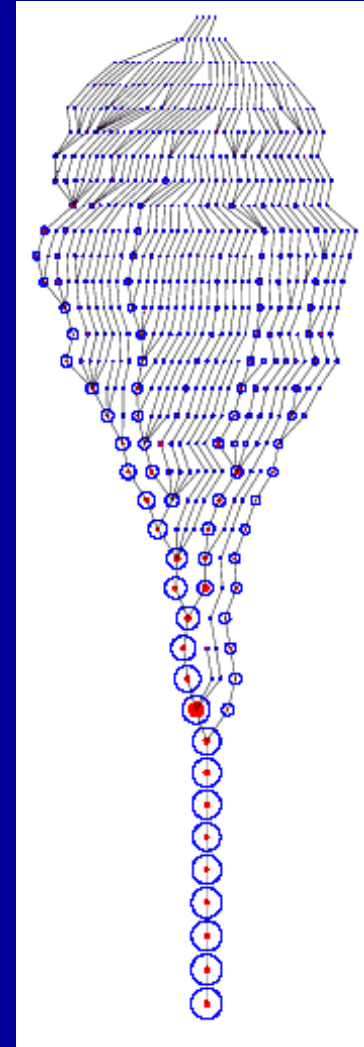
Binary of reduced mass μ , total mass M .
At luminosity distance d , frequency f_{GW} ,
dimensionless strain amplitude is

$$h = 3 \times 10^{-23} (f_{\text{GW}}/1\text{Hz})^{2/3} (M_{\text{ch}}/10 M_{\text{sun}})^{5/3} (100\text{Mpc}/d)$$

where $M_{\text{ch}}^{5/3} = \mu M^{2/3}$ defines the “chirp mass”.

Context and Connections of IMBH

- In $z \sim 5-30$ universe, seeds for SMBH
- In local universe, probes of star cluster dynamics
- Potentially unique sources of gravitational waves (ground and space)



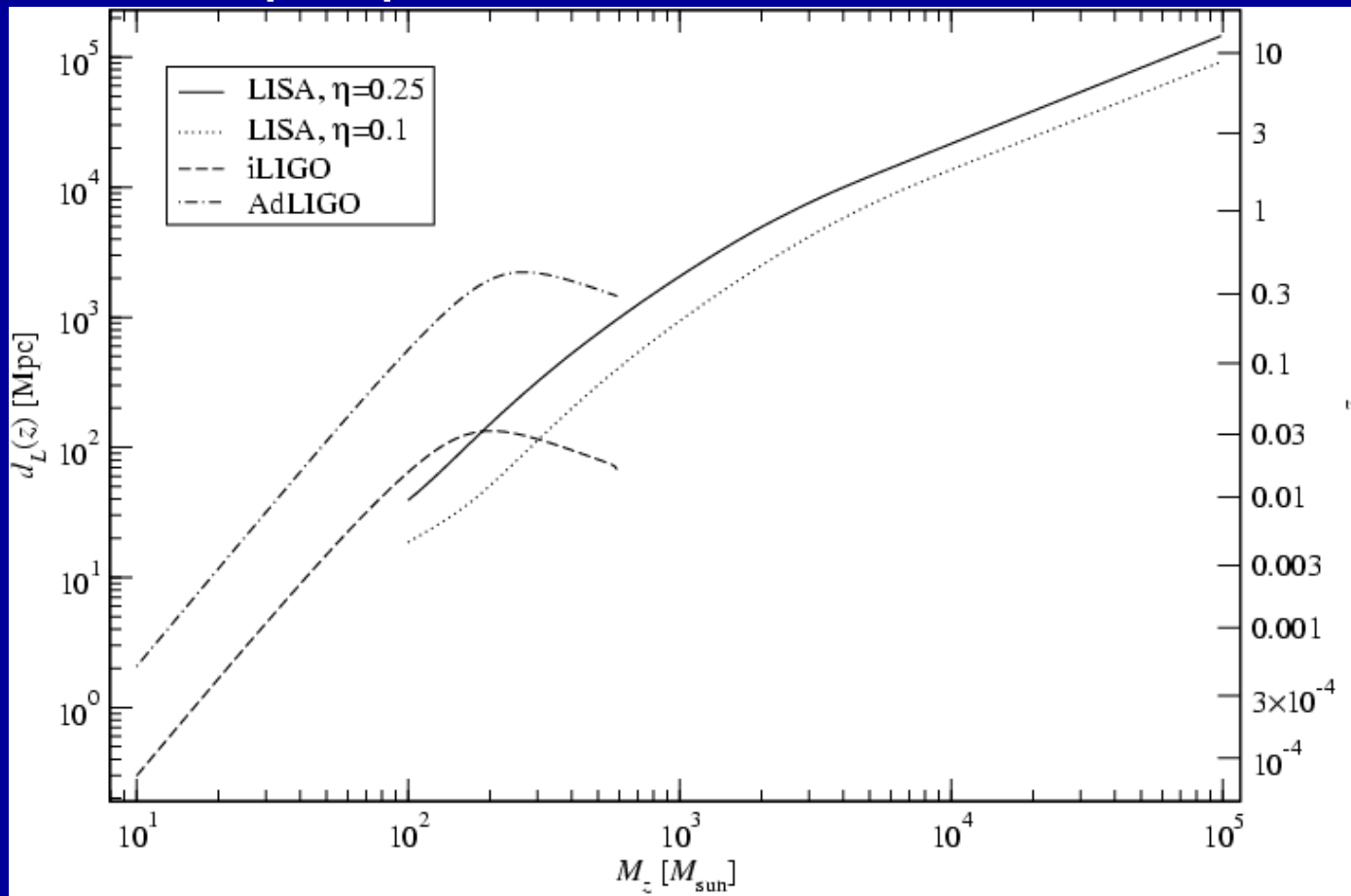
Wechsler et al. 2002

Why Are We Not Sure?

- Stellar-mass ($5-20 M_{\text{sun}}$) and supermassive ($10^6-10^{10} M_{\text{sun}}$) BH are established with certainty
- Why not IMBH ($10^2-10^4 M_{\text{sun}}$)?
- Lack of dynamical evidence
 - Too rare for easy binary observations
 - Too light for easy radius of influence obs
- Attempts being made, but settle for indirect observations in the meantime

IMBH-IMBH Visibility

- $\sim 1000 M_{\text{sun}}$ binary visible to $z \sim 1$.
- Reasonable rates: few tens per year at >1 Hz
- Unique probe of dense cluster star formation

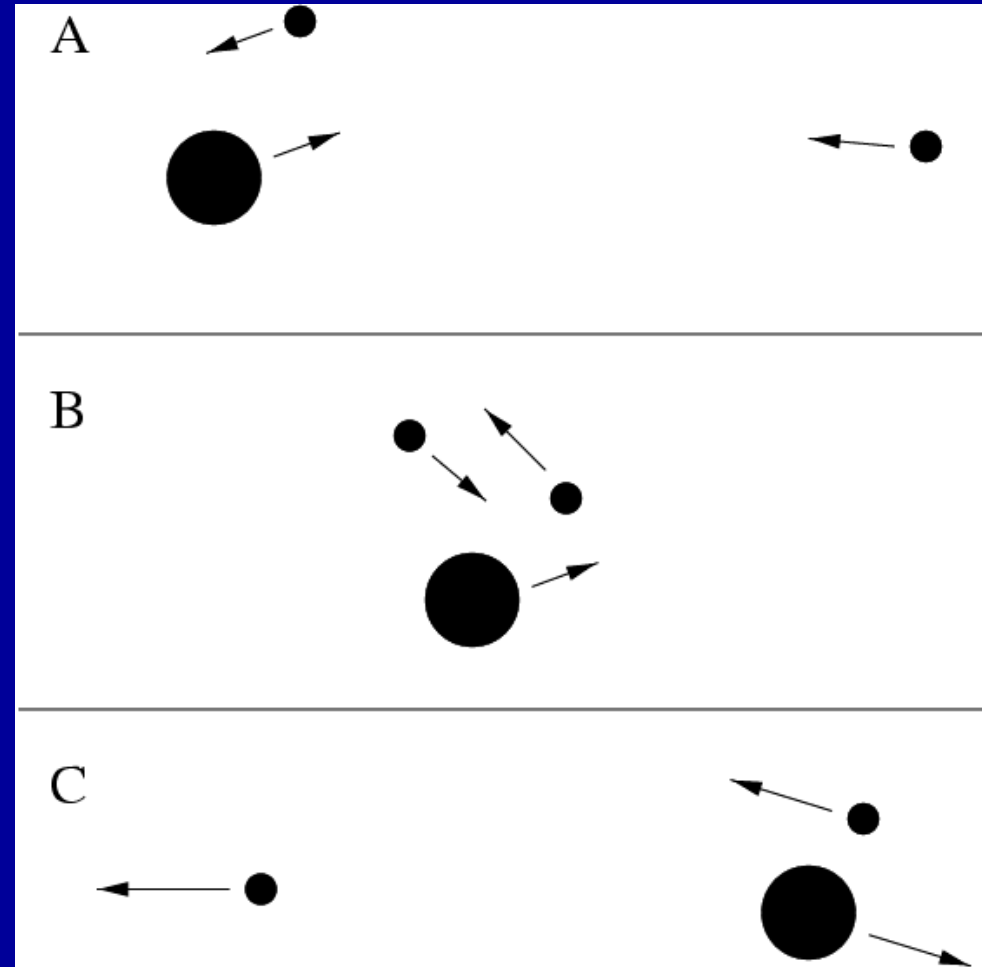


Fregeau et al. 2006

Formation of IMBHs

- Problem: $\sim 10^3 M_{\text{sun}}$ too much from normal star!
- Population III stars
Low Z; weak winds
- **Collisions or mergers**
Needs dense clusters
Young: collisions
Old: three-body

Issue: ejections by 3-body or GW recoil. If $M_{\text{init}} > 300 M_{\text{sun}}$, seems safe.



Open Question: Mass Function?

- Period, radial velocity of companion would give lower mass limit
One example would establish IMBH
- Issue: unique identification
Nearest ULX are few Mpc away!
Even O, B stars are ~24th mag
- Maybe He II 4686A emission lines?
Some candidates being pursued