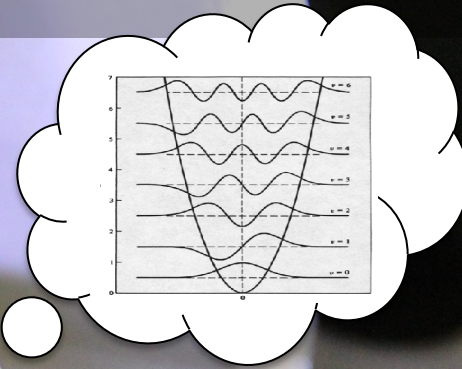


# Toward Quantum Opto-Mechanics in a Gram-Scale Suspended Mirror Interferometer



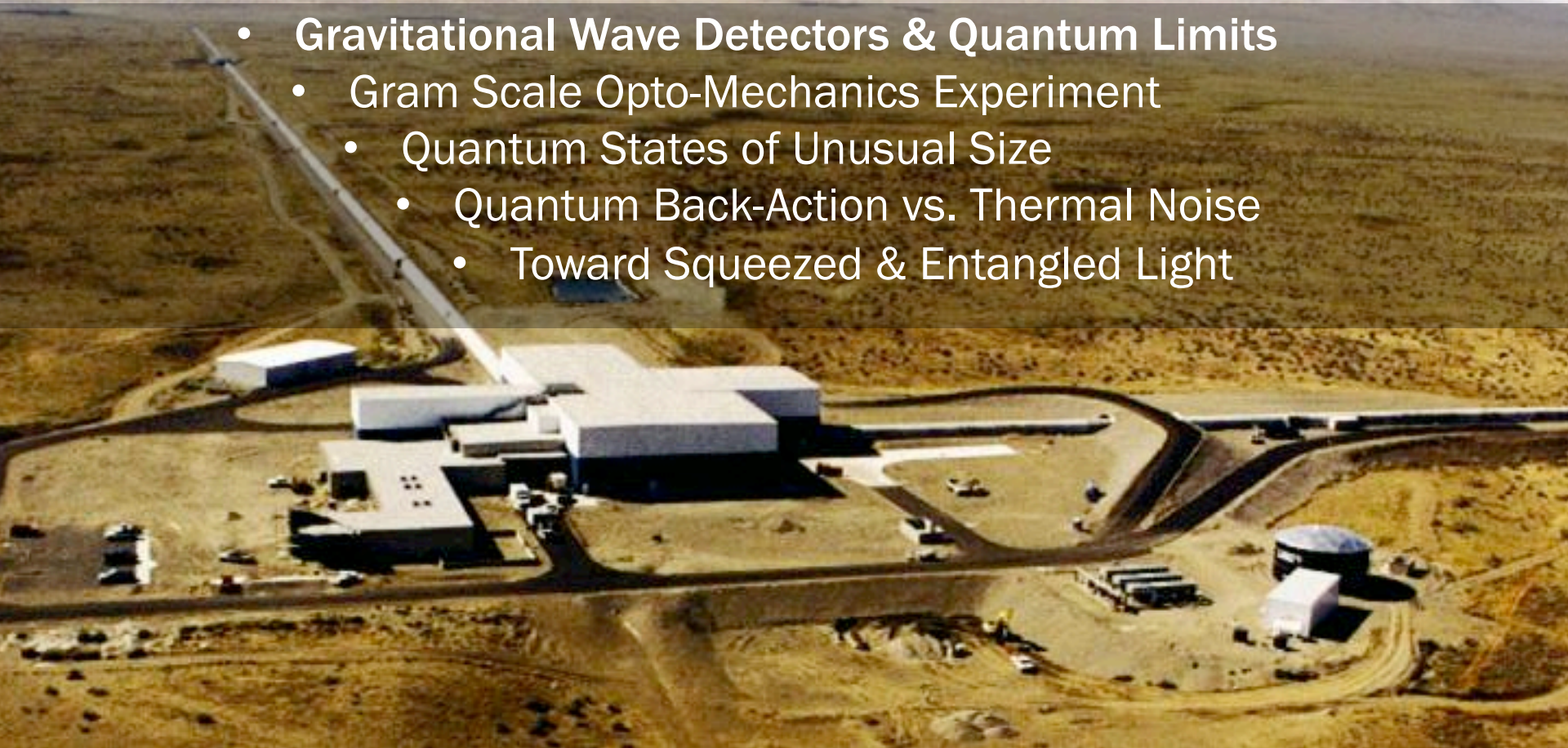
**Christopher Wipf**

Thesis Supervisor: **Nergis Mavalvala**

Thesis Committee Members: **Leonid Levitov, Vladan Vuletic**

# Overview

- **Gravitational Wave Detectors & Quantum Limits**
  - Gram Scale Opto-Mechanics Experiment
    - Quantum States of Unusual Size
      - Quantum Back-Action vs. Thermal Noise
      - Toward Squeezed & Entangled Light



# THE BORDER TERRITORY

QUANTUM DOMAIN

CLASSICAL DOMAIN

PHOTONS  
ELECTRONS  
ATOMS

SUN  
PLANETS  
○  
○  
○  
US  
○  
○  
○

GRAVITY WAVE DETECTOR

QUANTUM FLUIDS



1

SIZE (# OF ATOMS)

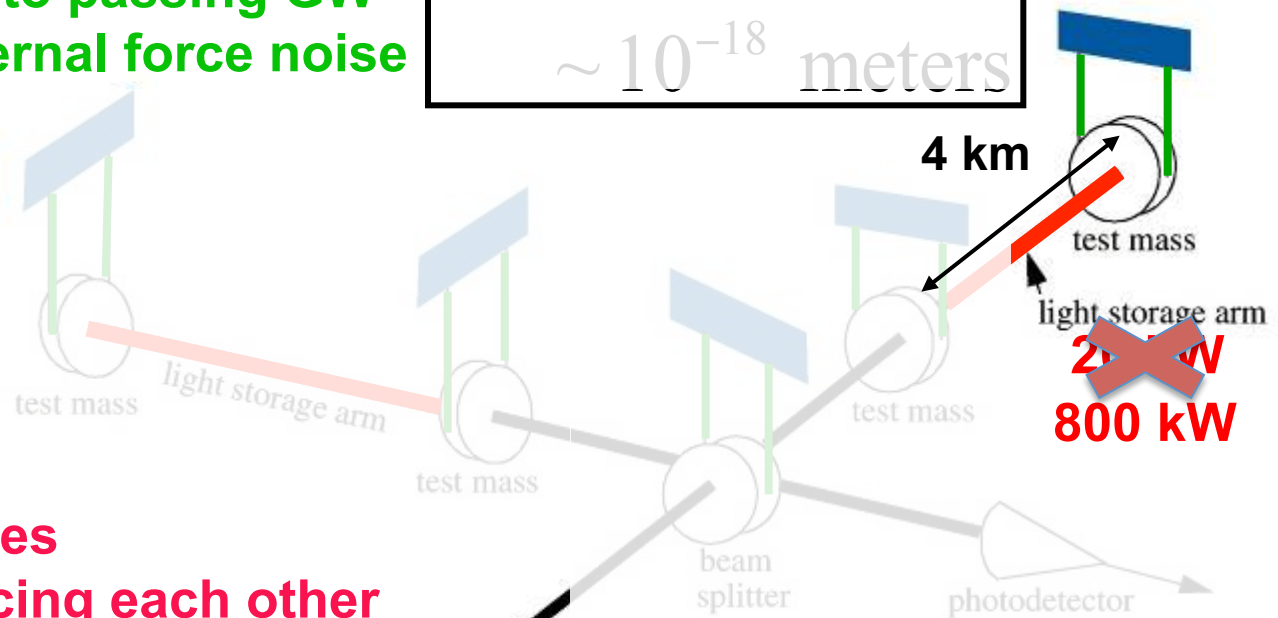
$10^{23}$

# How to Catch a Gravitational Wave 〰

## Mirrors hang as pendulums

- Quasi-free particles
- Respond to passing GW
- Filter external force noise

$$\begin{aligned}\Delta L &= h_{GW} L \\ &= 10^{-21} \times 4000 \\ &\sim 10^{-18} \text{ meters}\end{aligned}$$



## Optical cavities

- Mirrors facing each other
- Builds up light power

laser  
~~180 W~~  
180 W

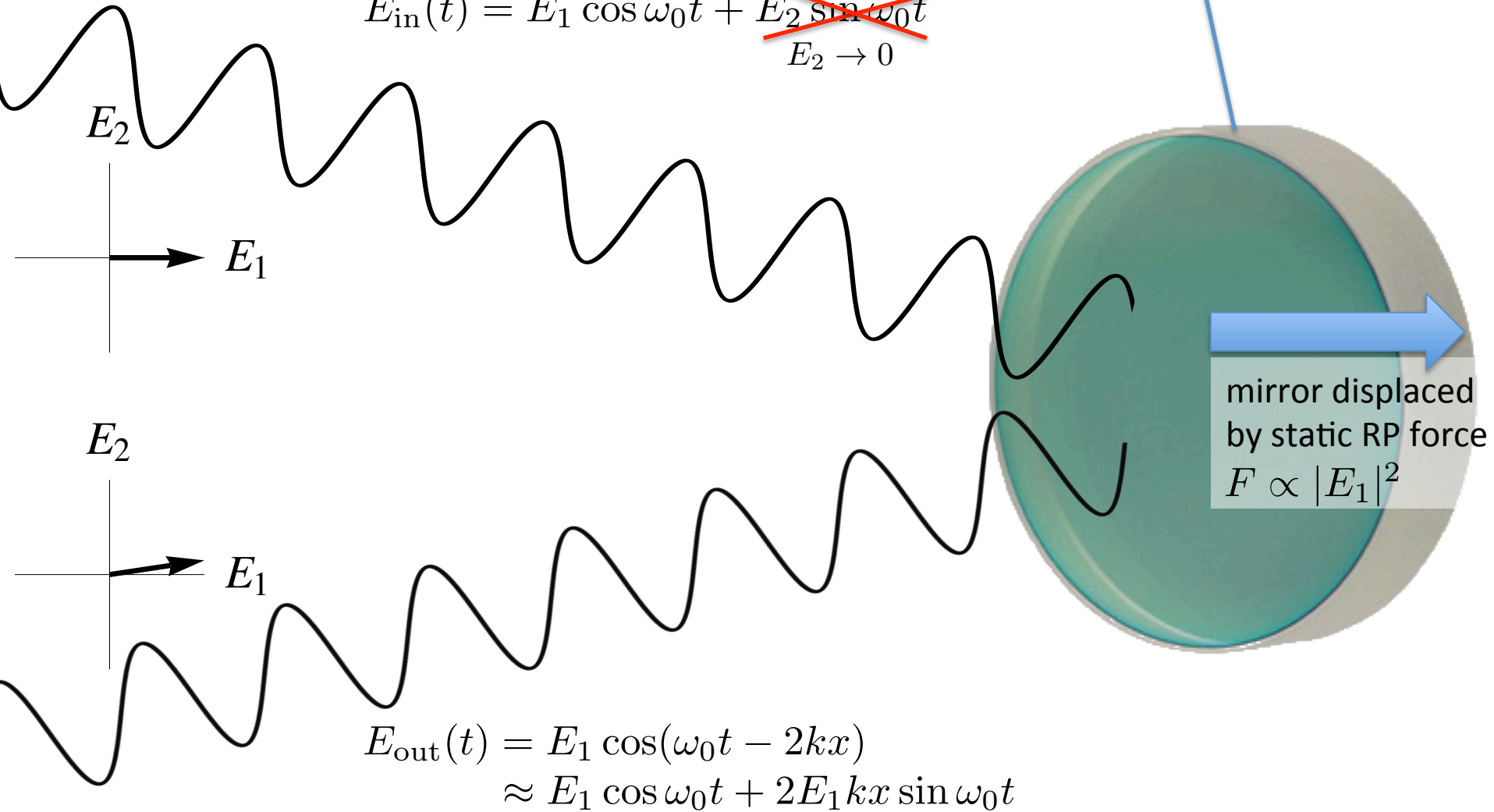
Lots of laser power  $P$

- Signal  $\sim P$
- Noise  $\sim \sqrt{P}$

# Opto-Mechanics

$$E_{\text{in}}(t) = E_1 \cos \omega_0 t + \cancel{E_2 \sin \omega_0 t}$$

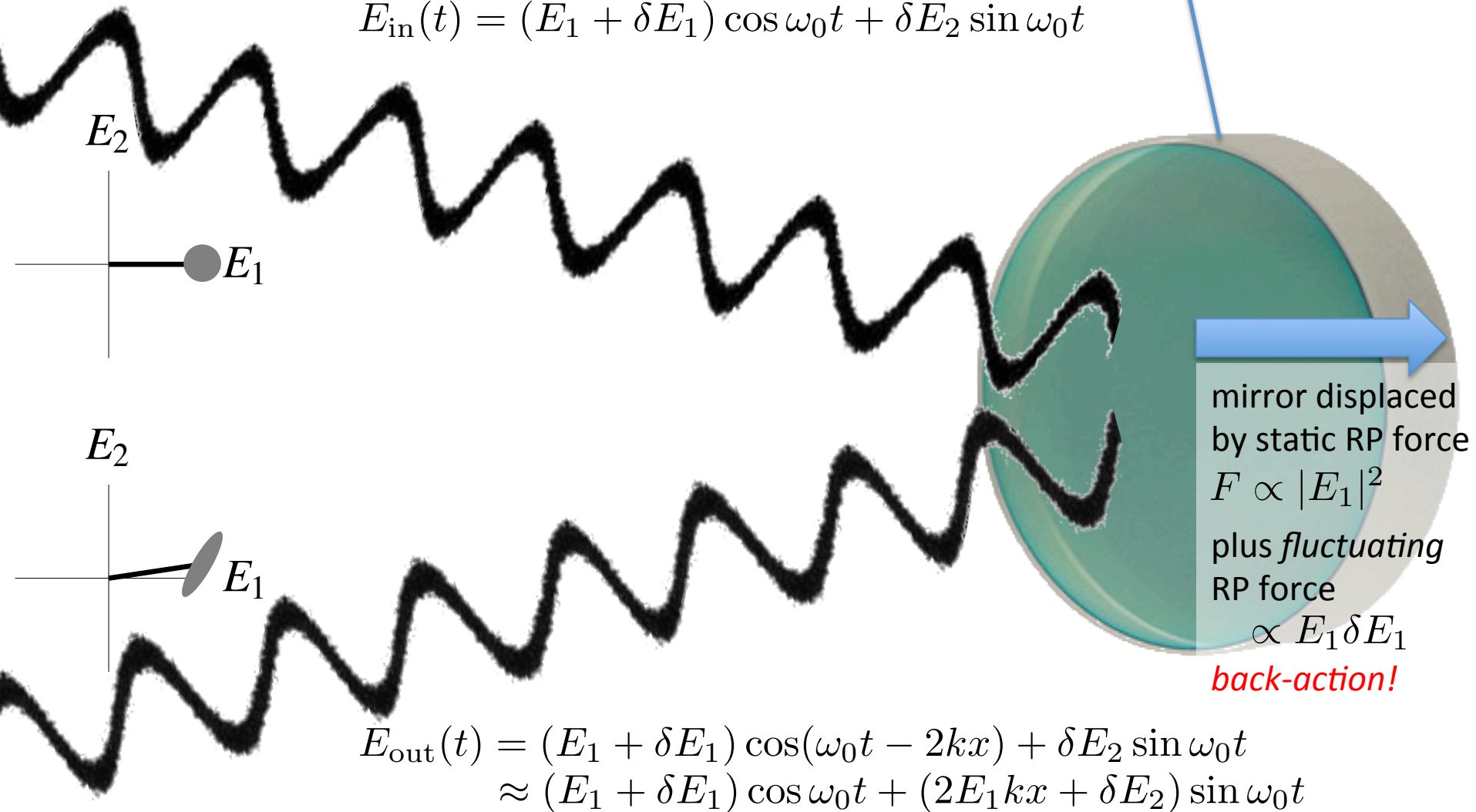
$E_2 \rightarrow 0$



$$E_{\text{out}}(t) = E_1 \cos(\omega_0 t - 2kx)$$
$$\approx E_1 \cos \omega_0 t + 2E_1 kx \sin \omega_0 t$$

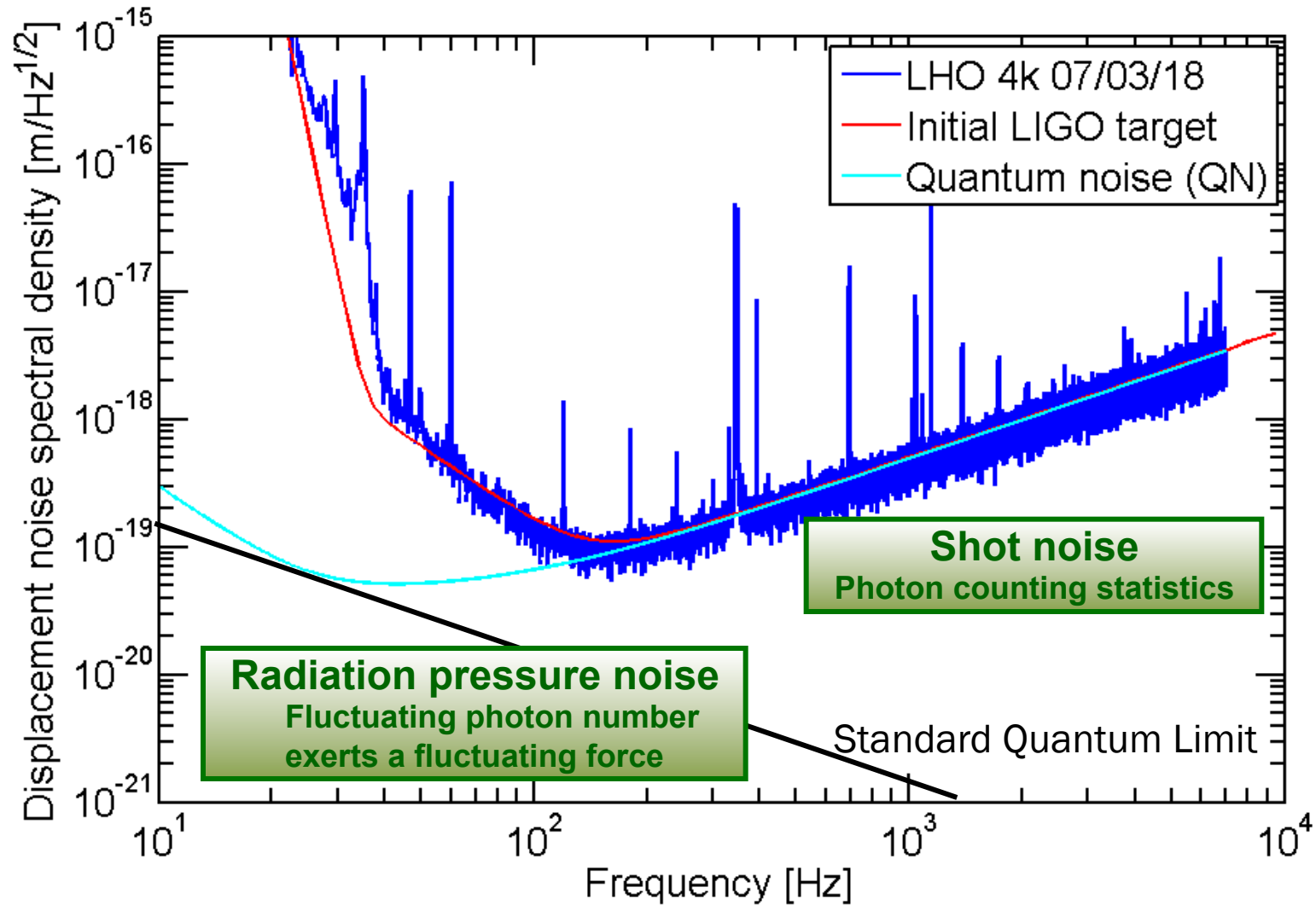
# Quantum-Opto-Mechanics

$$E_{\text{in}}(t) = (E_1 + \delta E_1) \cos \omega_0 t + \delta E_2 \sin \omega_0 t$$

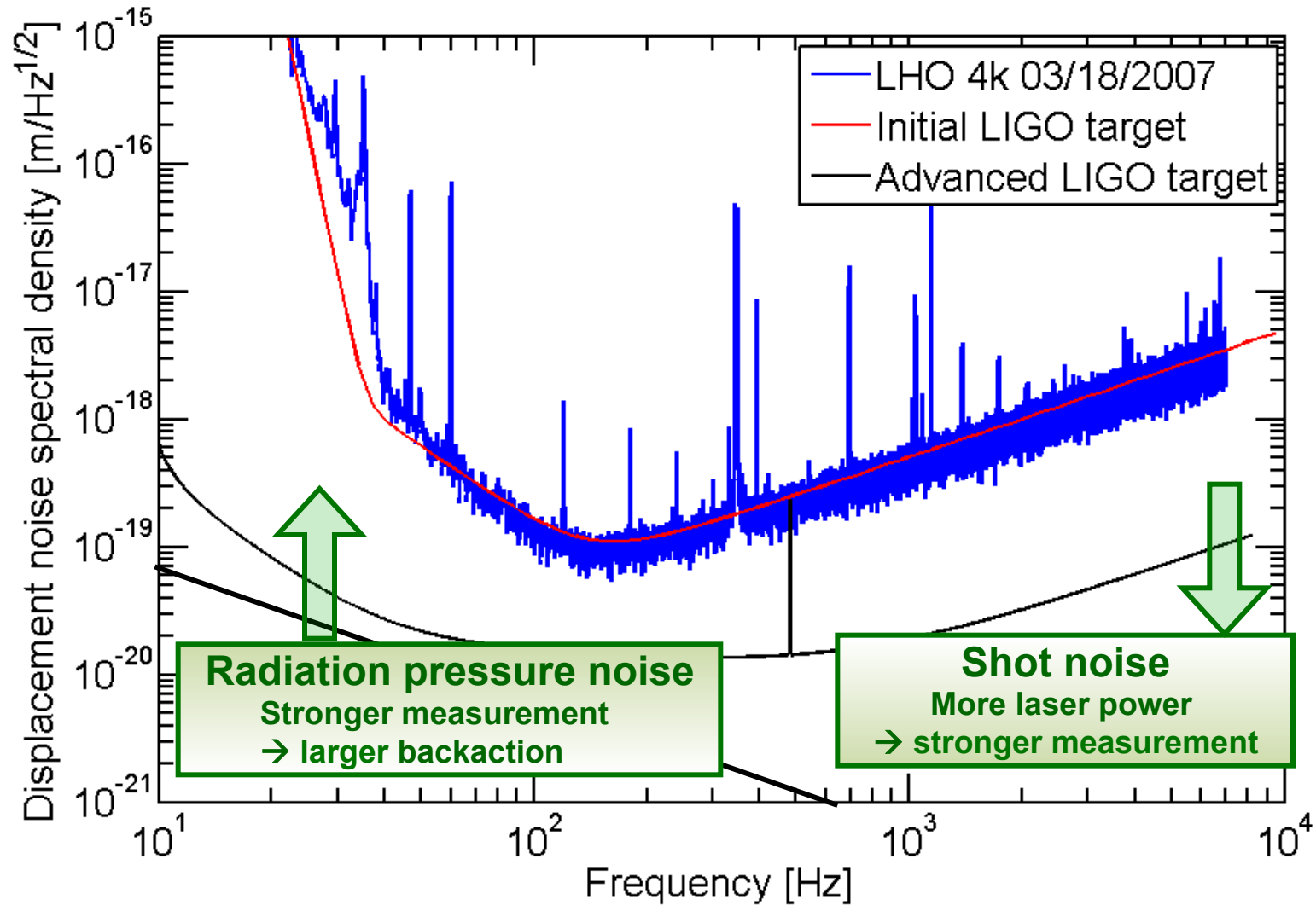


$$E_{\text{out}}(t) = (E_1 + \delta E_1) \cos(\omega_0 t - 2kx) + \delta E_2 \sin \omega_0 t$$
$$\approx (E_1 + \delta E_1) \cos \omega_0 t + (2E_1 kx + \delta E_2) \sin \omega_0 t$$

# Quantum Noises in Initial LIGO



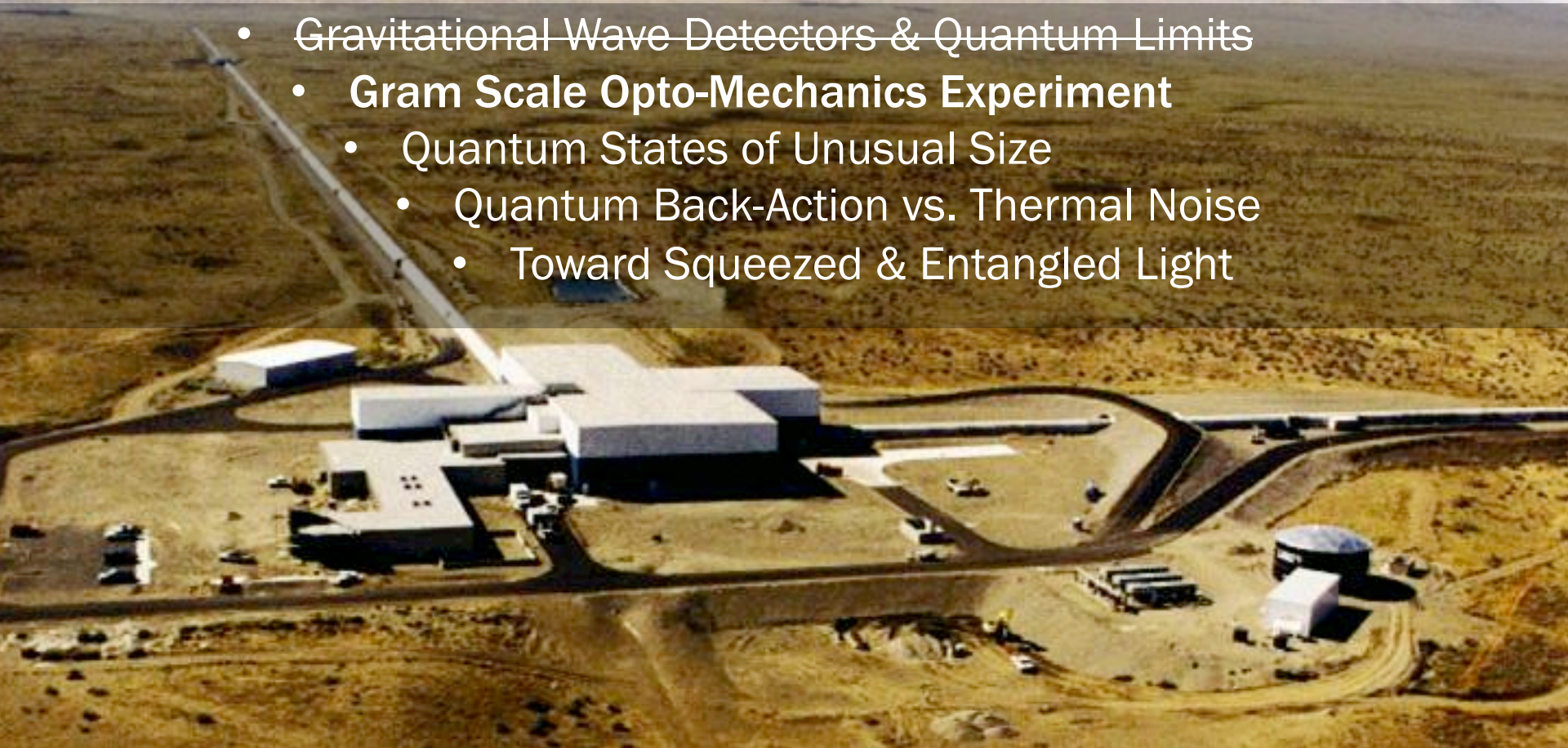
# Quantum Limit in Advanced LIGO





# Overview

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- **Gram Scale Opto-Mechanics Experiment**
  - Quantum States of Unusual Size
    - Quantum Back-Action vs. Thermal Noise
    - Toward Squeezed & Entangled Light

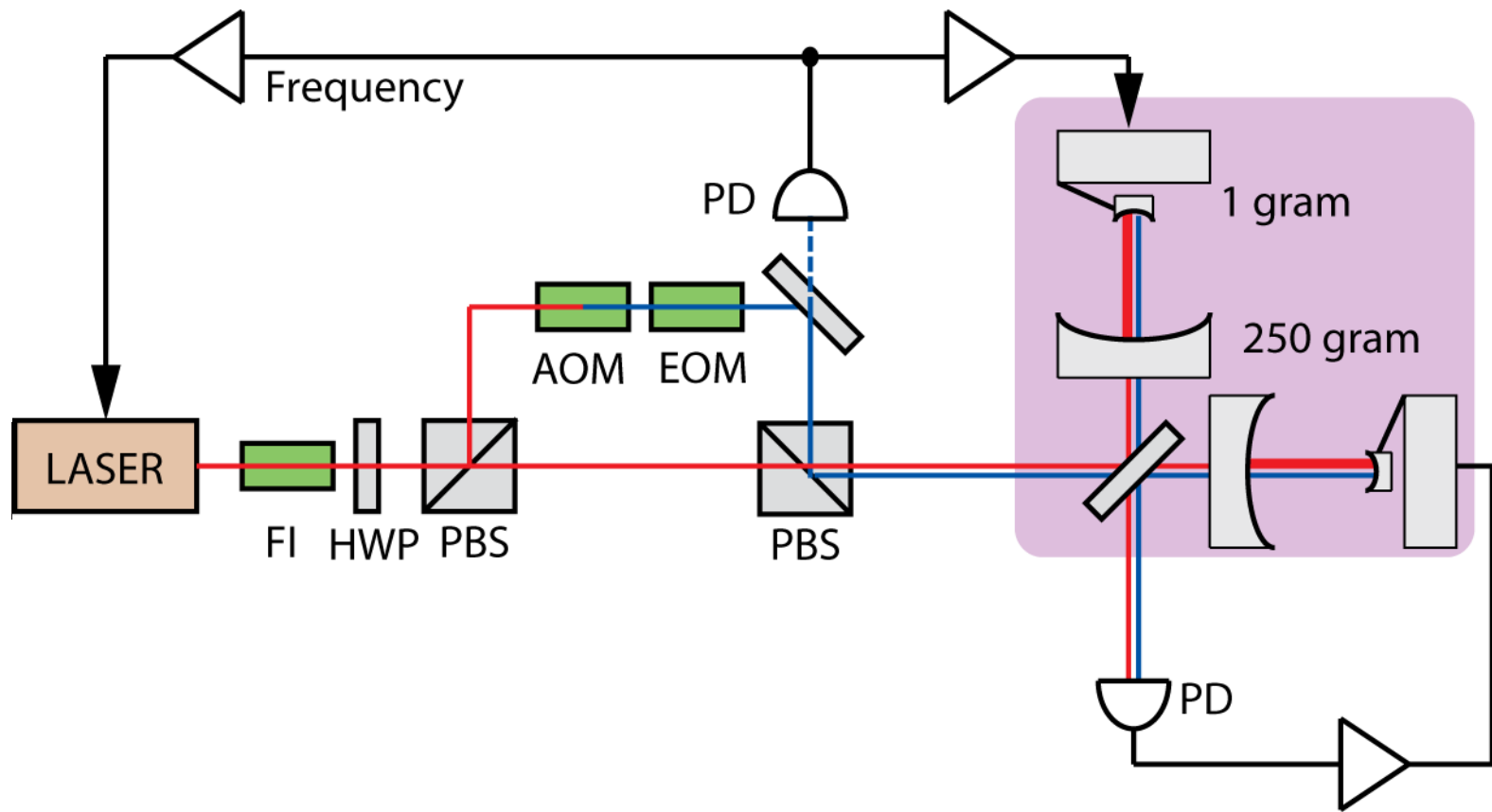


# Why a Gram-Scale Experiment?

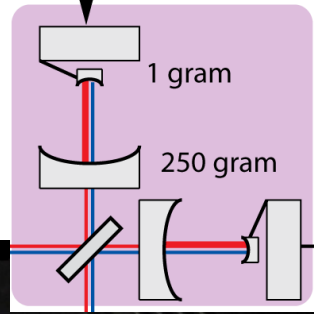
- Testbed for opto-mechanical effects anticipated for Advanced LIGO
  - Classical radiation pressure forces
  - Quantum radiation pressure noise, squeezing
- New regime for “Macroscopic Quantum Mechanics”
  - Cooling to the ground state
  - Entanglement

# Design Features

- Reuse techniques and components developed for GW detectors
- Low frequency, high  $Q$  mirror suspensions
- Tabletop testbed: gram scale masses, 1 meter optical path
- Dual optical fields with tunable frequency offset
- Michelson interferometer to cancel laser noise



# Lab Tour



10 W pre-stabilized  
laser

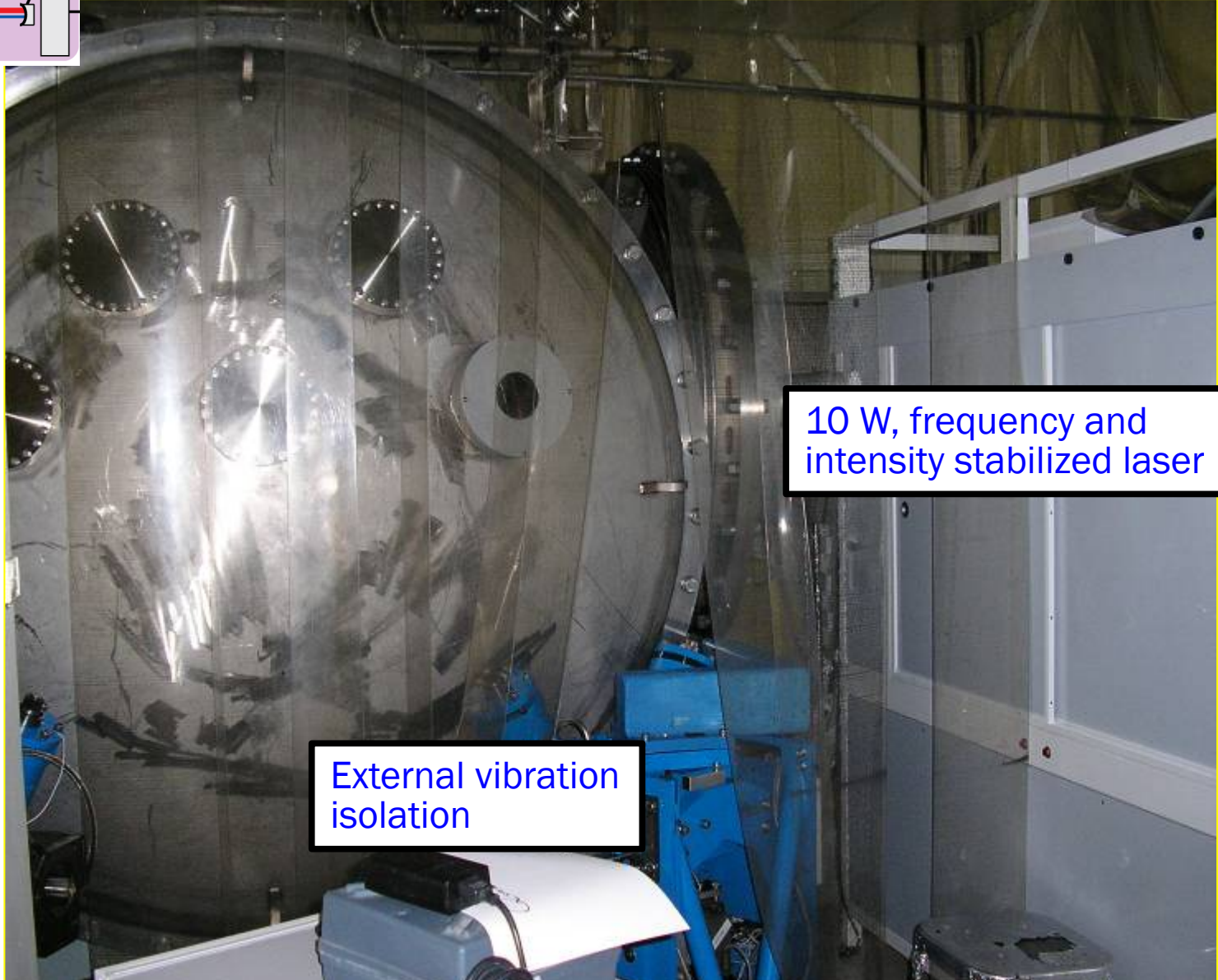
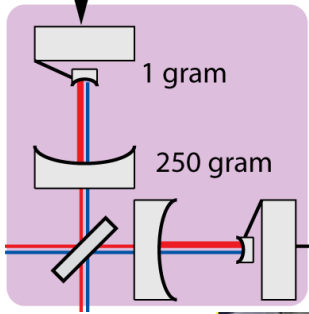
Fabry-Perot Michelson  
length = 1 m  
finesse  $\approx 8000$   
circ. power  $\approx 10$  kW

mini-mirror

mass = 1 g

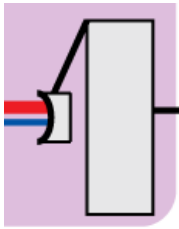
natural freq. = 10 Hz

# Lab Tour



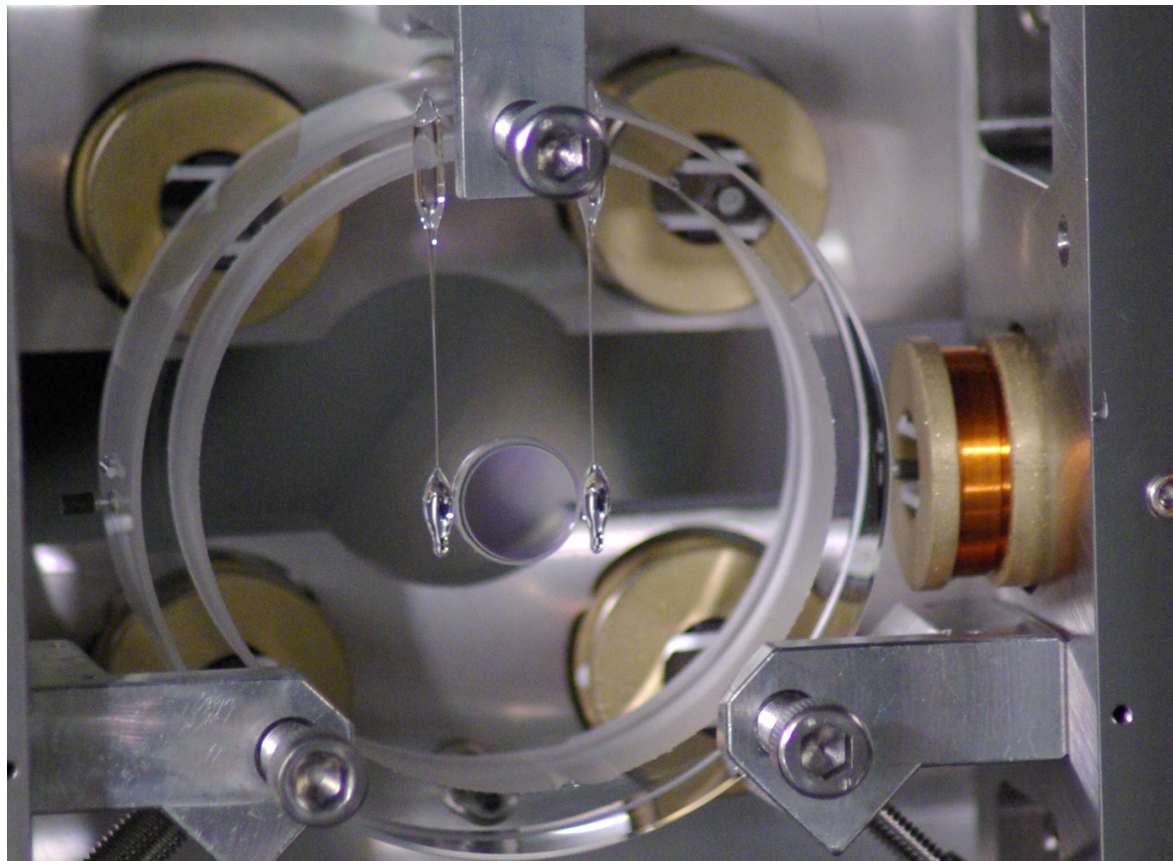
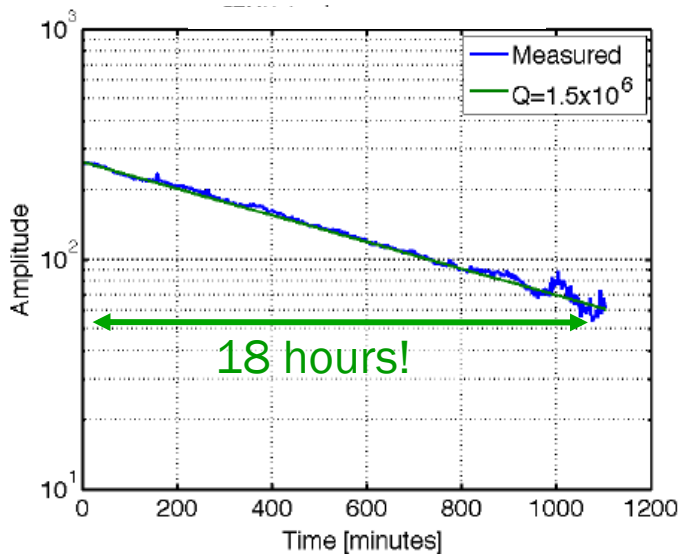
10 W, frequency and intensity stabilized laser

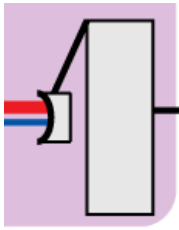
External vibration isolation



# 1 Gram Mirror Suspension

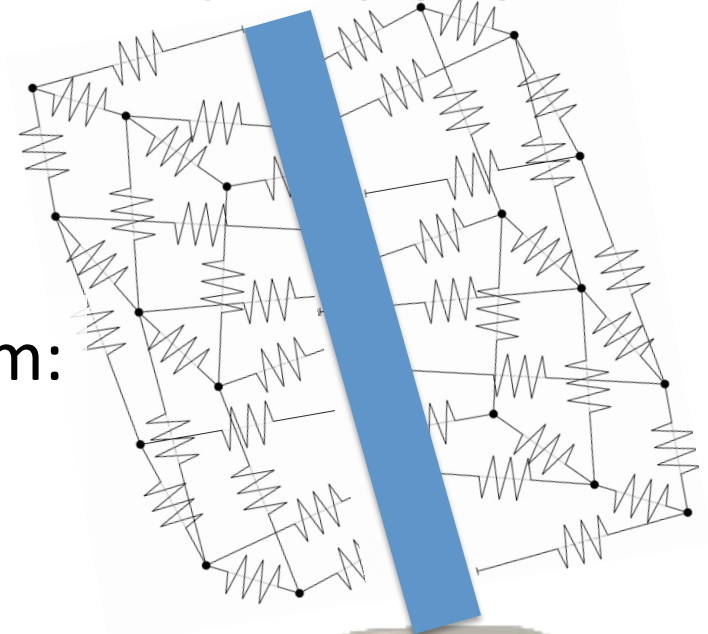
- Double suspension with actuators on the intermediate mass (the “ring”)
- Bottom stage: glass fibers tapered to 200  $\mu\text{m}$  diameter
- “Ears” prevent bending at the glue joints, reducing losses
- $Q > 10^6$  for 10 Hz mode





# Thermal Noise, Our Nemesis

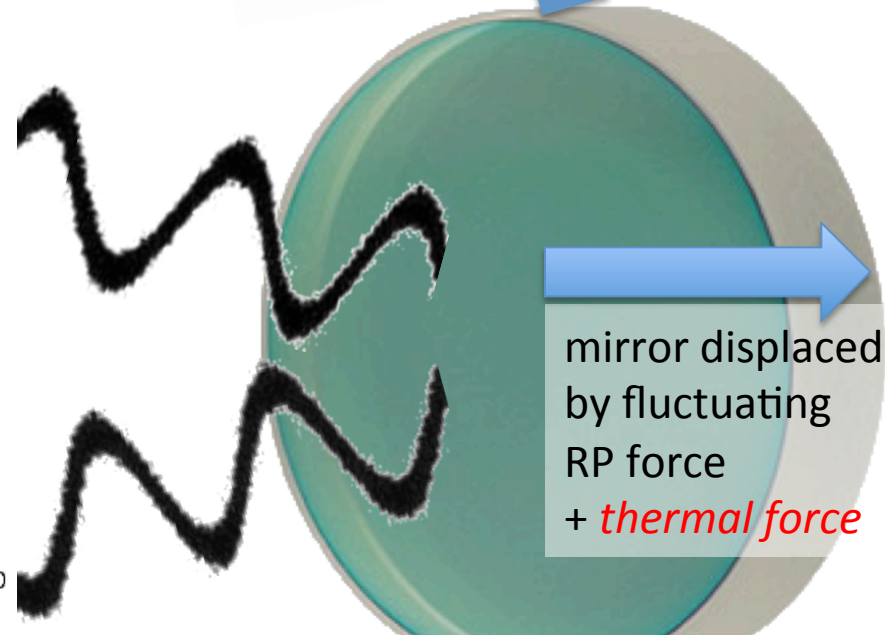
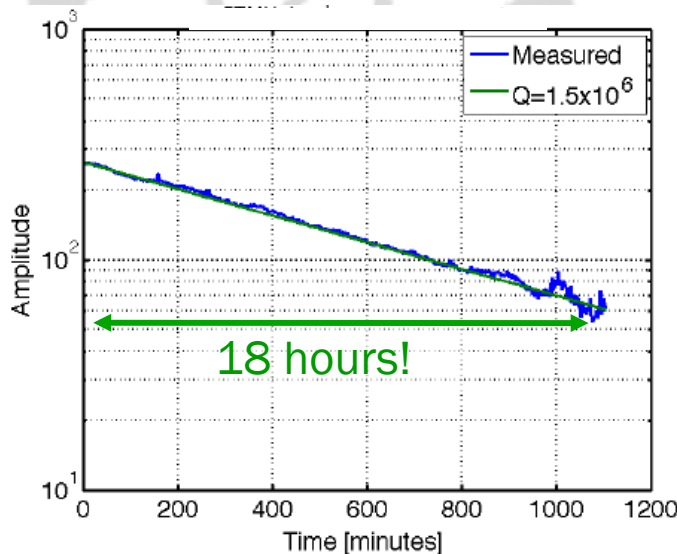
Mirror oscillator is coupled to its room temperature environment (model as a bath of weakly coupled oscillators, each with energy  $k_b T$ )



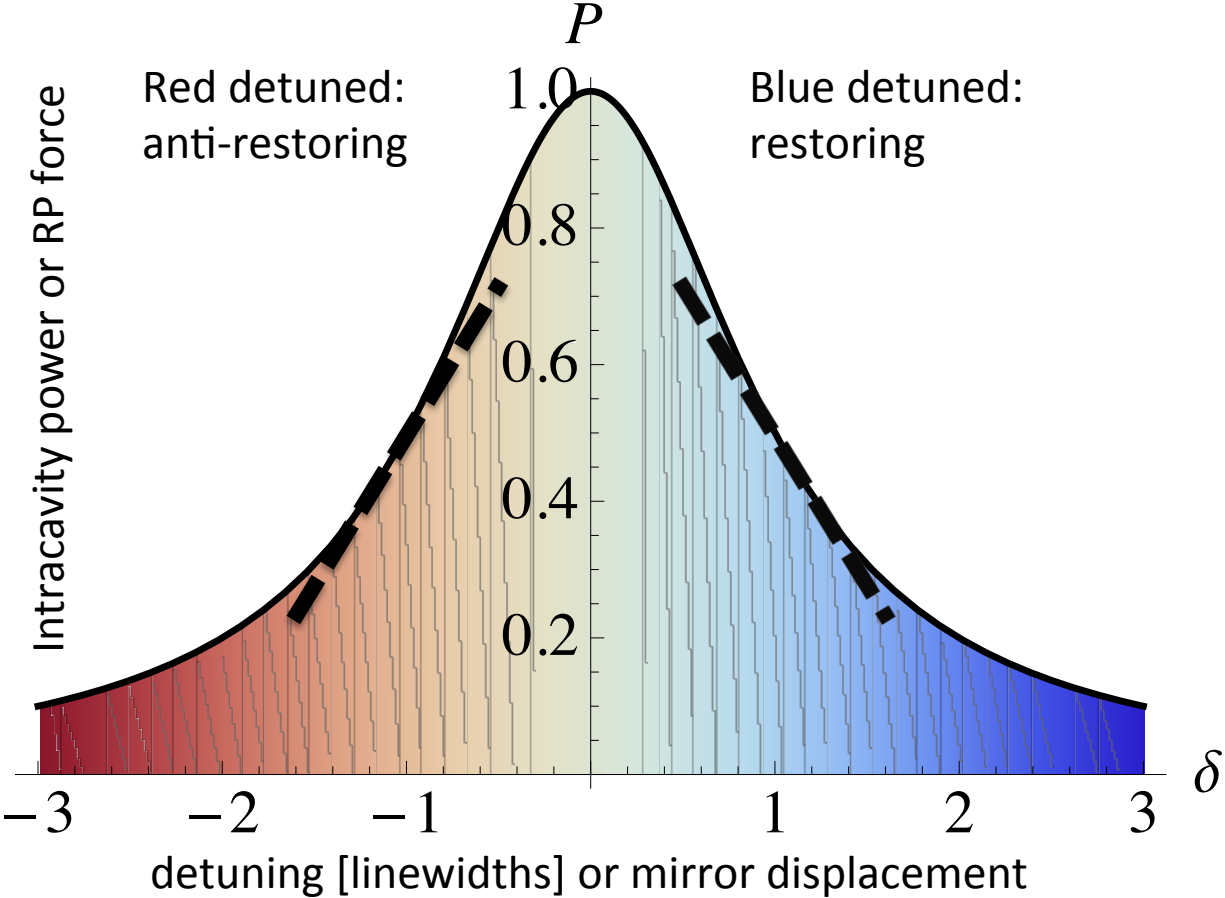
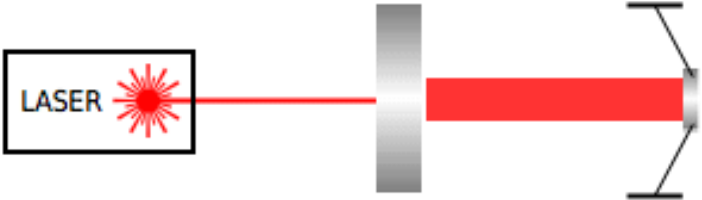
Fluctuation Dissipation Theorem:  
Damping  $\Leftrightarrow$  Thermal Noise

$$S_F^{(T)}(\Omega) = 4k_b T m \Gamma_m$$

(assuming viscous damping)

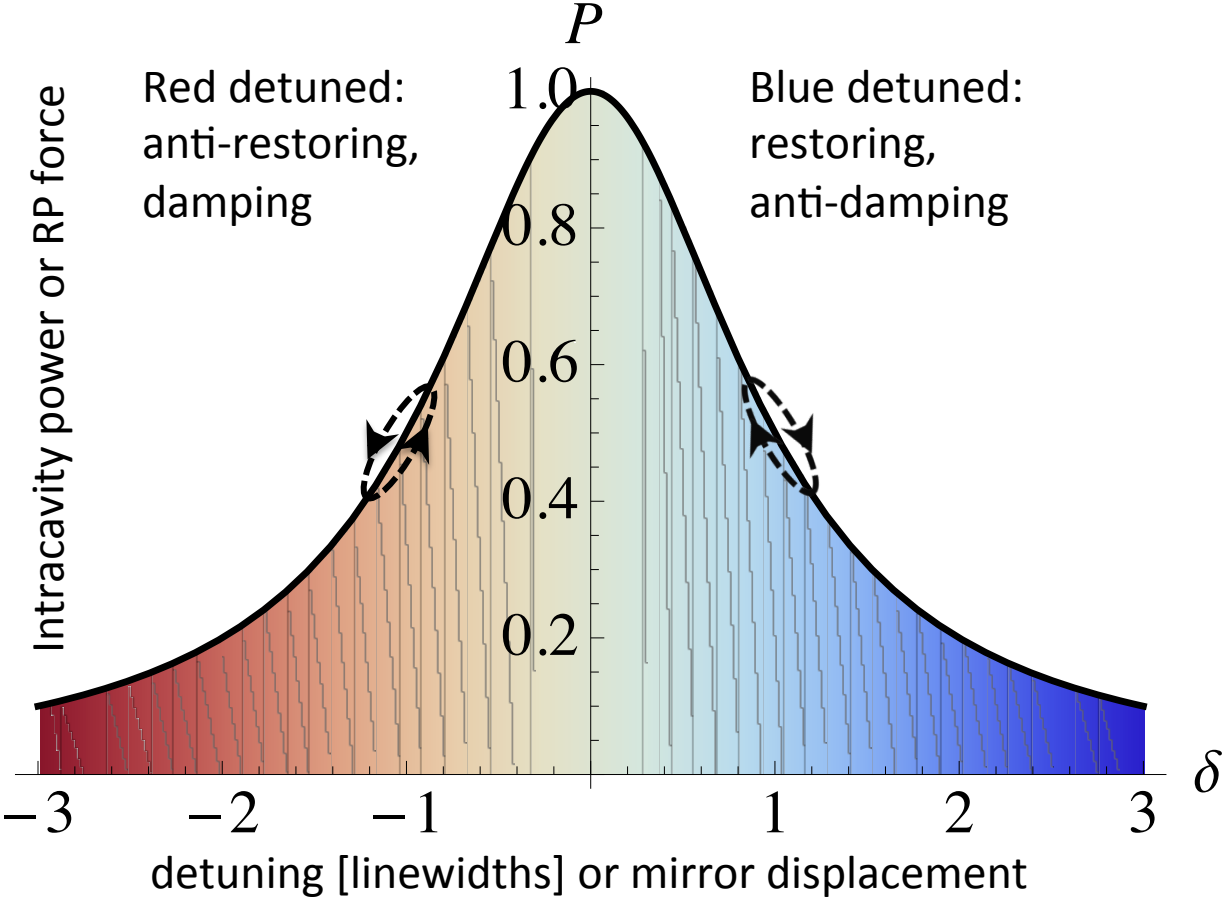
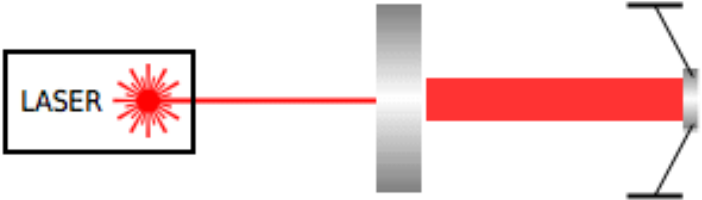


# Radiation Pressure in a Cavity

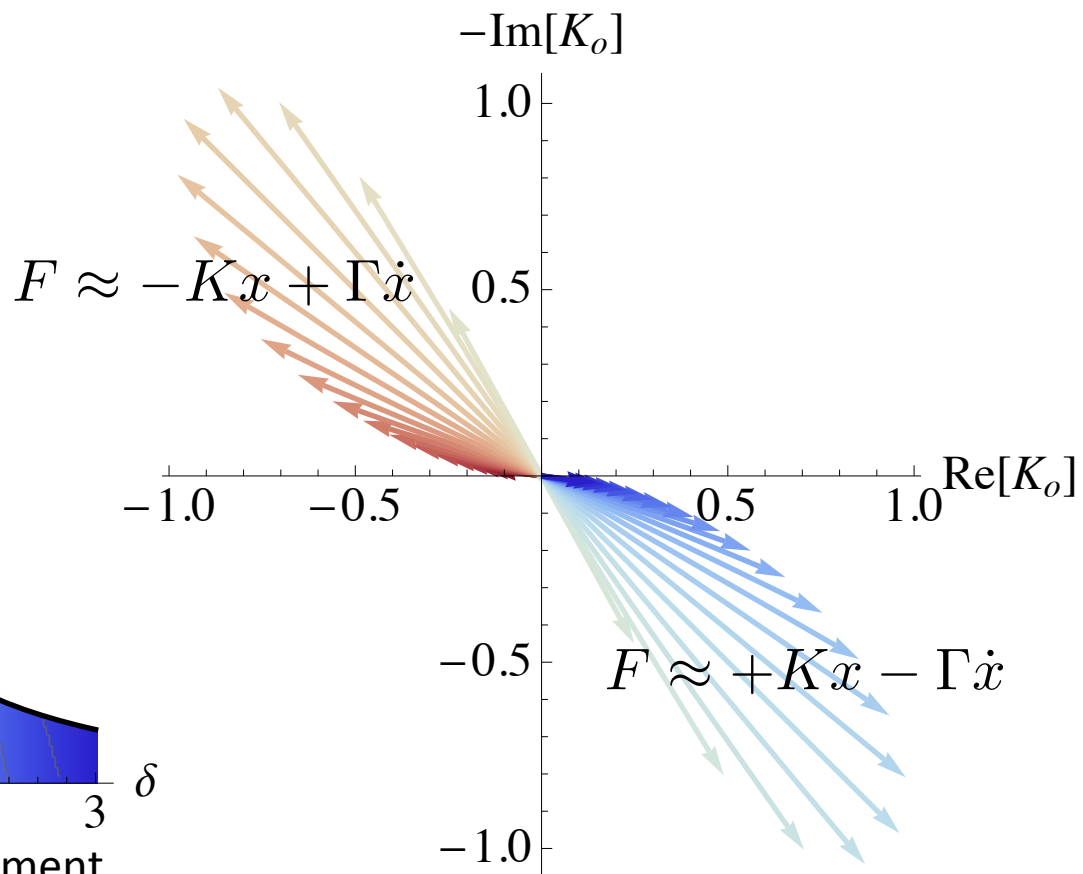
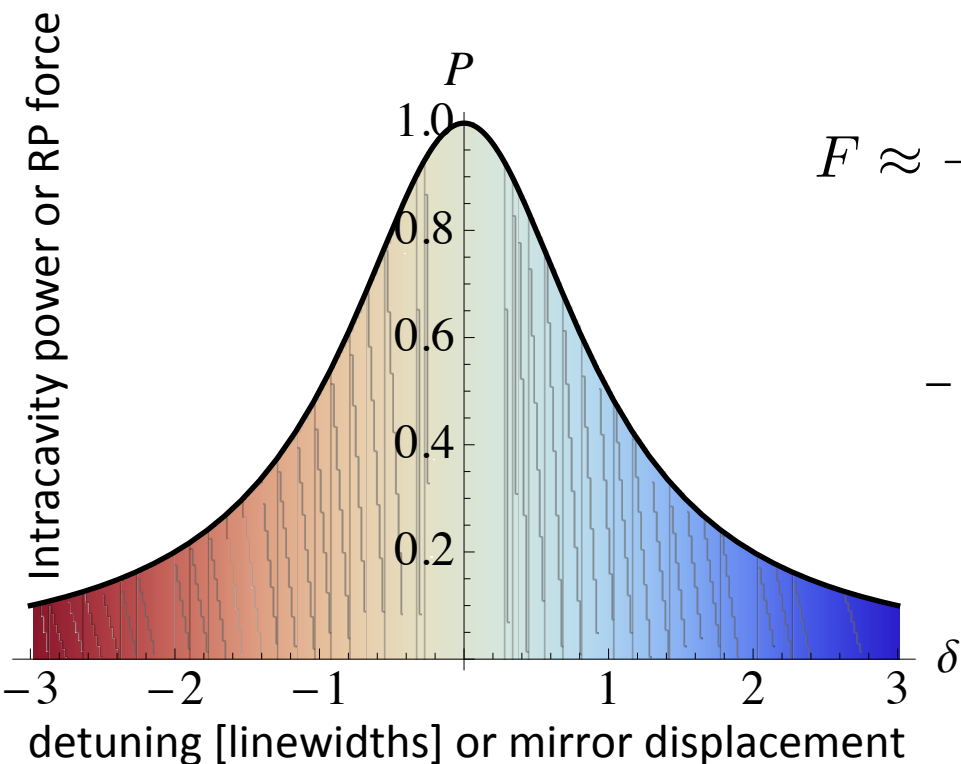




# Radiation Pressure in a Cavity

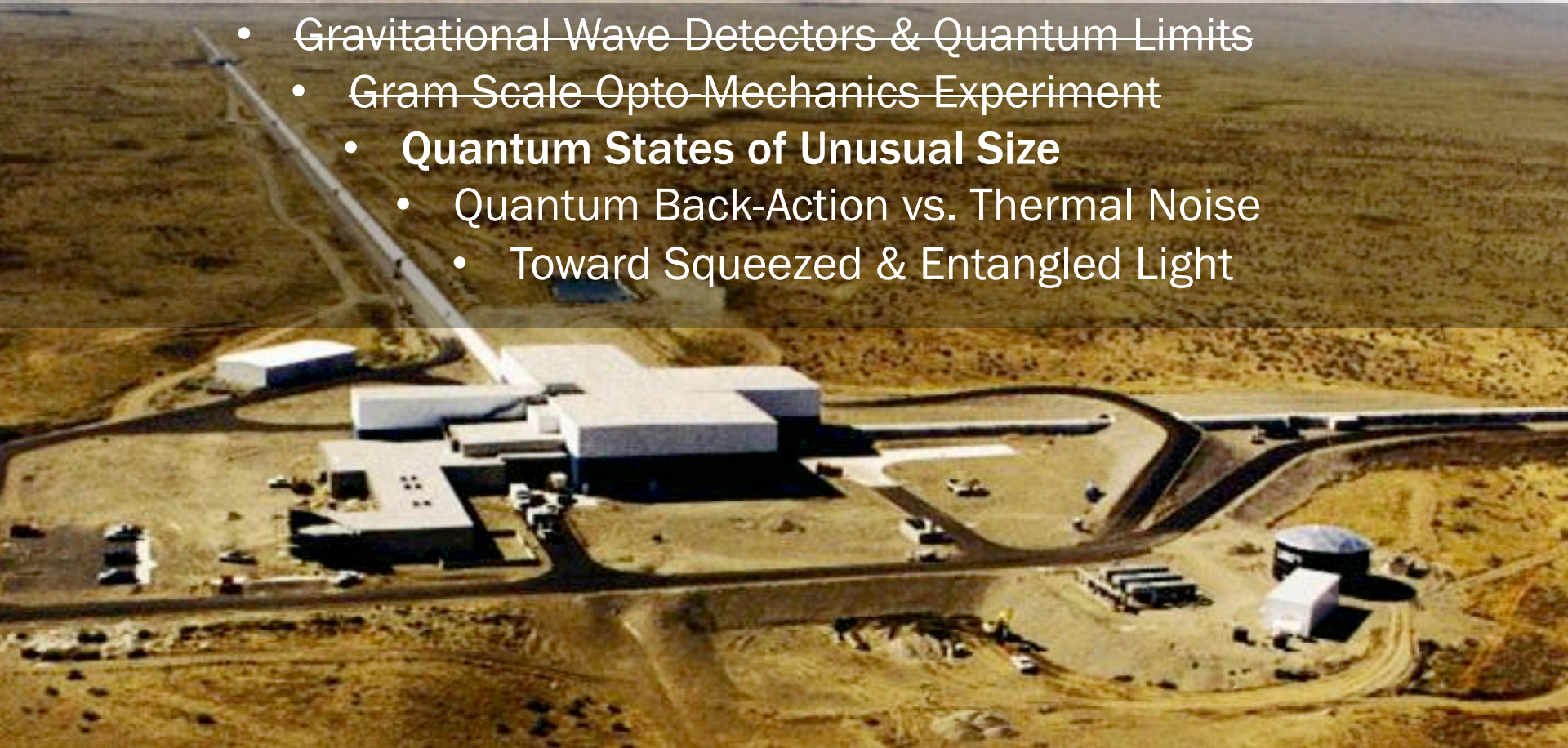


# Radiation Pressure in a Cavity



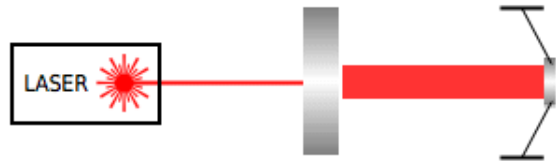
# Overview

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# Opportunity for Macroscopic Quantum Mechanics

- Model system: Optical cavity with a movable mirror



- Quantum mechanics of mirror are normally swamped by thermal noise
  - Thermal energy  $k_b T$  vastly exceeds the ground state energy  $\frac{1}{2} \hbar \Omega$
  - Occupation number
$$N = \frac{k_b T}{\hbar \Omega} \sim 10^{12} \text{ for LIGO}$$
- Can we use novel, non-cryogenic cooling techniques to approach the quantum ground state?

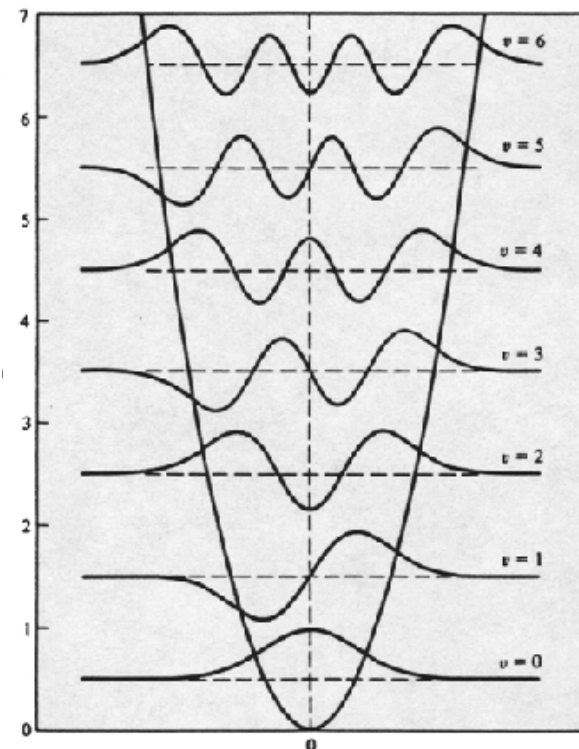
## letters to nature

### **Cavity cooling of a microlever**

Constanze Hühberger Metzger & Khaled Karrai

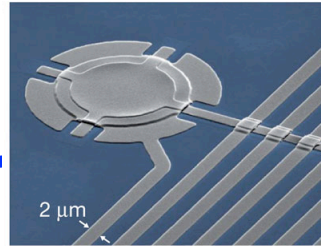
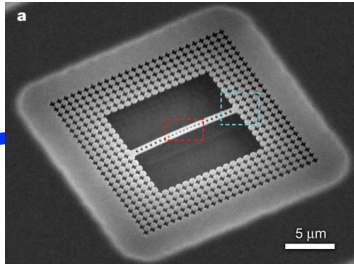
Center for NanoScience and Sektion Physik, Ludwig-Maximilians-Universität München, Geschwister-Scholl-Platz 1, 80539 München, Germany

The prospect of realizing entangled quantum states between macroscopic objects and photons<sup>1</sup> has recently stimulated interest in new laser-cooling schemes<sup>2,3</sup>. For example, laser-cooling the vibrational modes of a mirror can be achieved by subjecting



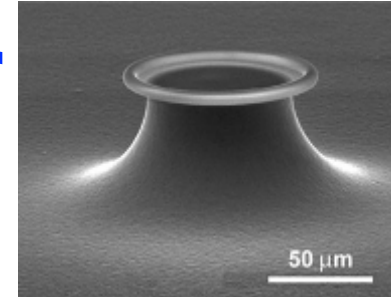
# Mechanical Resonators Race to the Ground State

Photonic crystal  
nanobeam  
→  $10^{-13}$  g

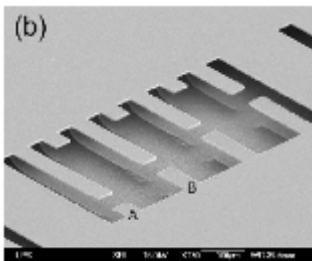


NEMS  
→  $10^{-11}$  g

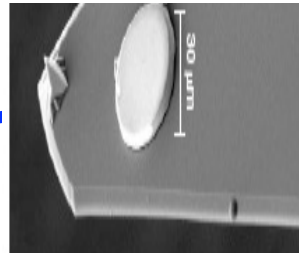
Toroidal microcavity  
→  $10^{-11}$  g



Micro mirrors  
→  $10^{-7}$  g

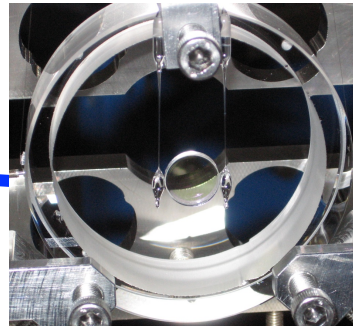


AFM cantilevers  
→  $10^{-8}$  g



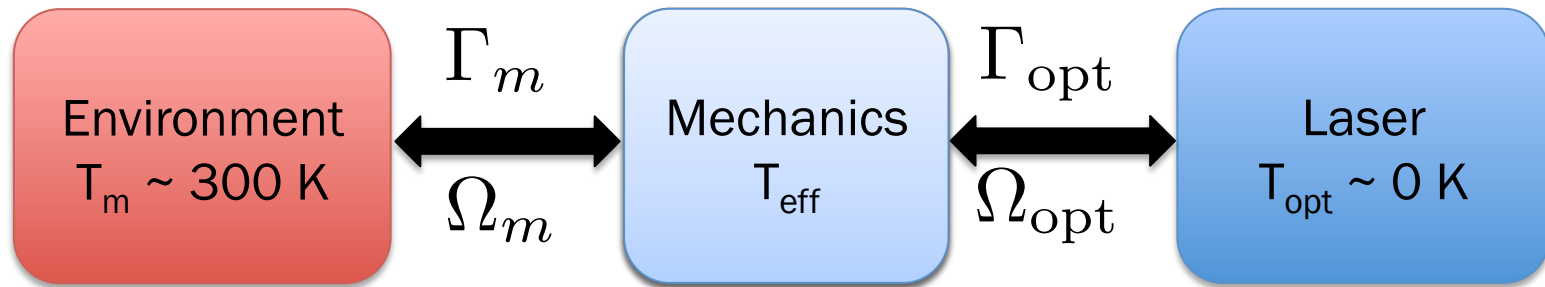
Si<sub>3</sub>N<sub>3</sub> membrane  
→  $10^{-8}$  g

Mini mirror → 1 g



LIGO  
→  $10^3$  g

# Optical Cooling of Mechanical Structures



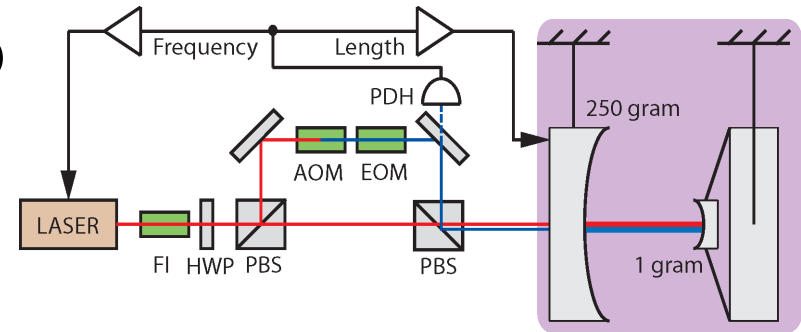
- Fluctuation Dissipation Thm  $\Rightarrow$  thermal noise  $\sim T_m, \Gamma_m$
- Add an optical damping force:  
(can be quantum limited with  $T_{\text{opt}} \sim 0$ )  
New effective damping rate is  $\Gamma_{\text{eff}} = \Gamma_m + \Gamma_{\text{opt}}$   
Cold force drains energy from the mechanics,  
*without adding thermal noise*
- Add an optical restoring force:  
New effective resonant frequency is  $\Omega_{\text{eff}}^2 = \Omega_m^2 + \Omega_{\text{opt}}^2$   
New effective occupation number:

$$N \approx \frac{k_b T_m}{\hbar \Omega_m} \frac{\Omega_m}{\Omega_{\text{opt}}} \frac{\Gamma_m}{\Gamma_{\text{opt}}}$$

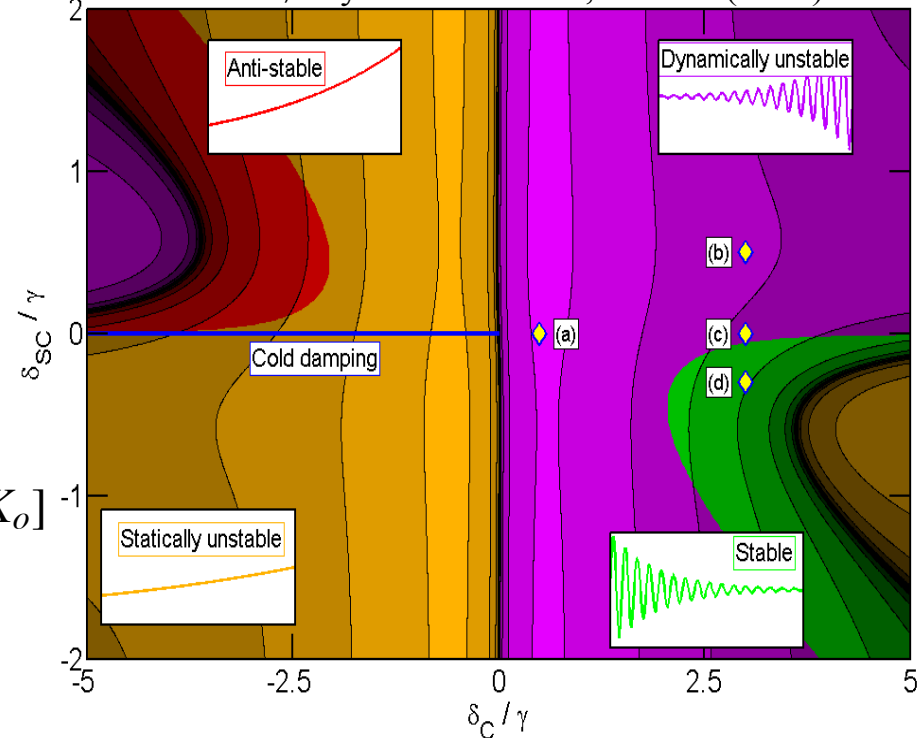
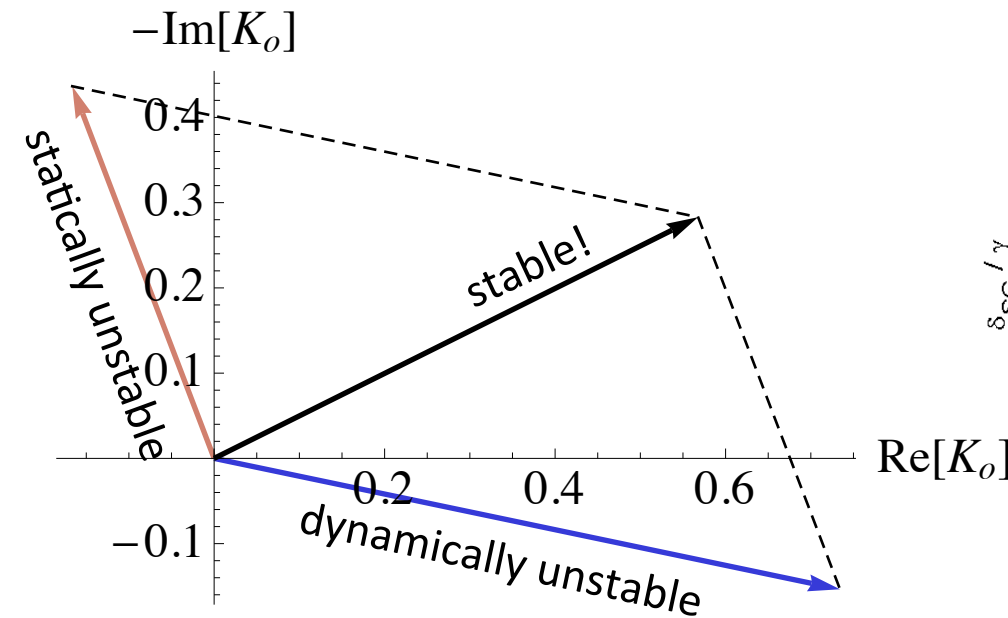
Want high Q mechanics,  
and high frequency  
low Q optical spring!

# Double Optical Spring

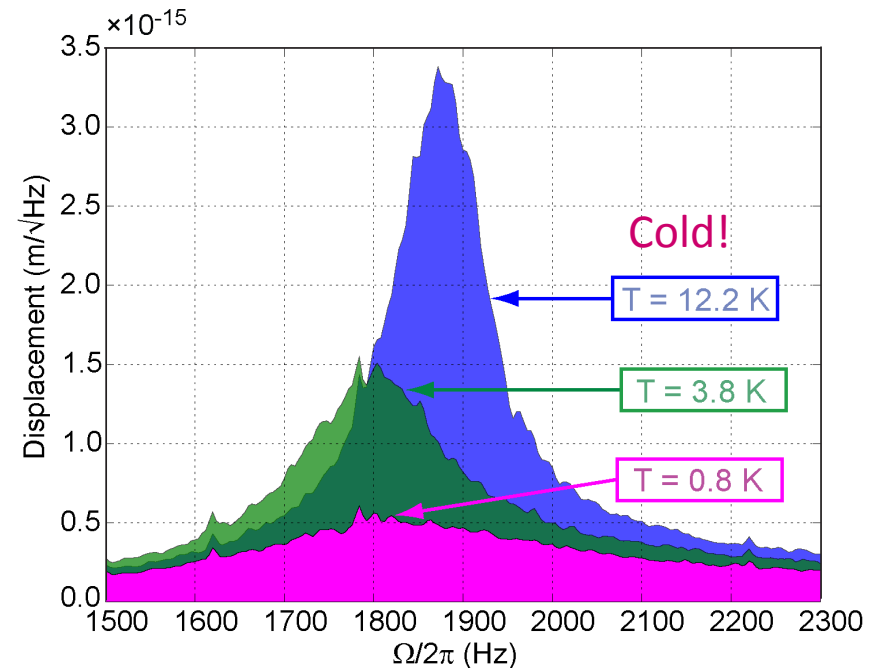
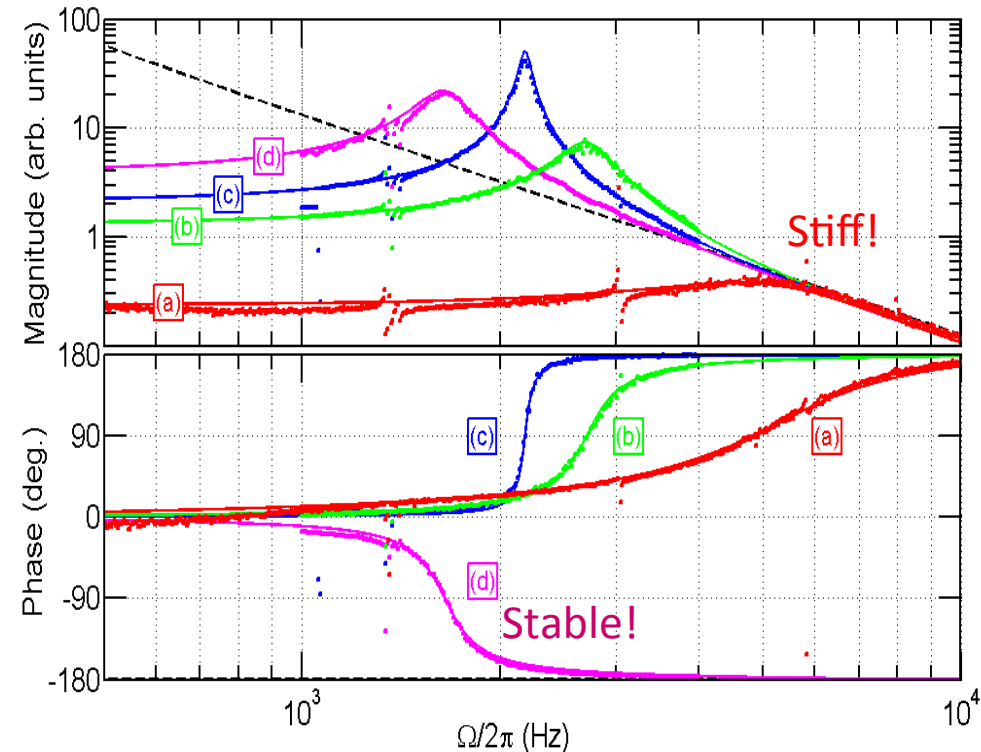
- Combining the RP of two fields may lead to a stable configuration (if the power and detuning of each is well chosen)



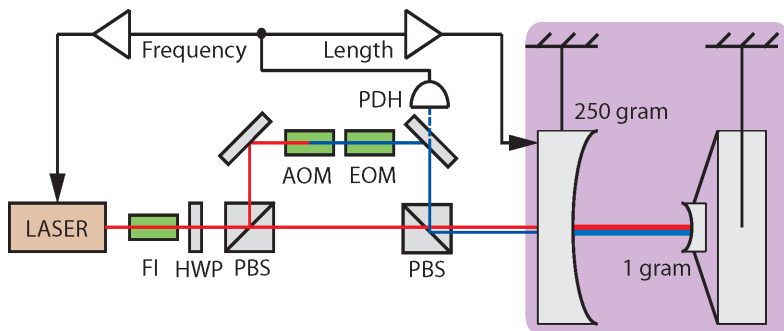
Corbitt et al., Phys. Rev. Lett. 98, 150802 (2007)



# All-Optical Trap for a 1 Gram Mirror



- Stiff optical springs!  
Cavity mode => diamond rod
- Stable optical trap using two light fields, opposite detuning
- Cooling limited by laser noise





# Quantum Limit of Cavity Cooling

- Mirror oscillator is heated by quantum radiation pressure fluctuations

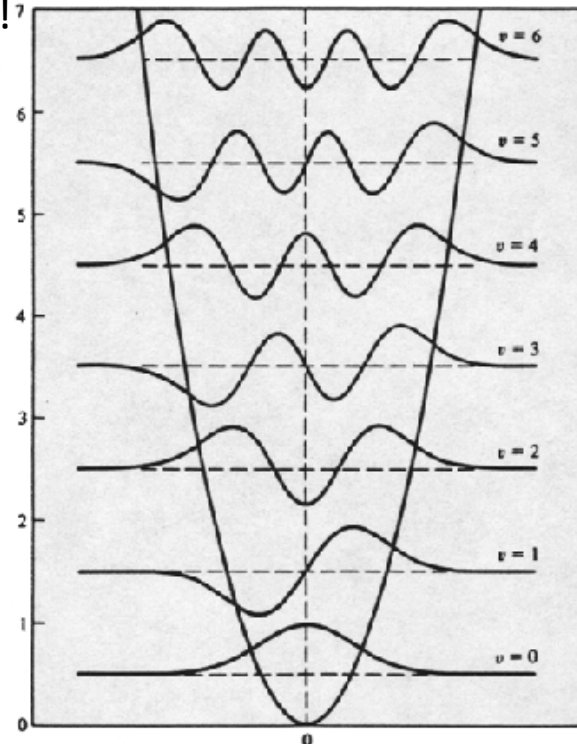
- Limiting occupation number is

$$N \approx \frac{1}{2} \frac{\gamma_c}{\Omega_{\text{eff}}} \quad (\Omega_{\text{eff}} \lesssim \gamma_c) \quad \text{“bad cavity”} \quad \text{good measurement!}^7$$

$$N \approx \frac{1}{4} \frac{\gamma_c^2}{\Omega_{\text{eff}}^2} \quad (\Omega_{\text{eff}} \gtrsim \gamma_c) \quad \text{“good cavity”} \quad \text{bad measurement!}$$

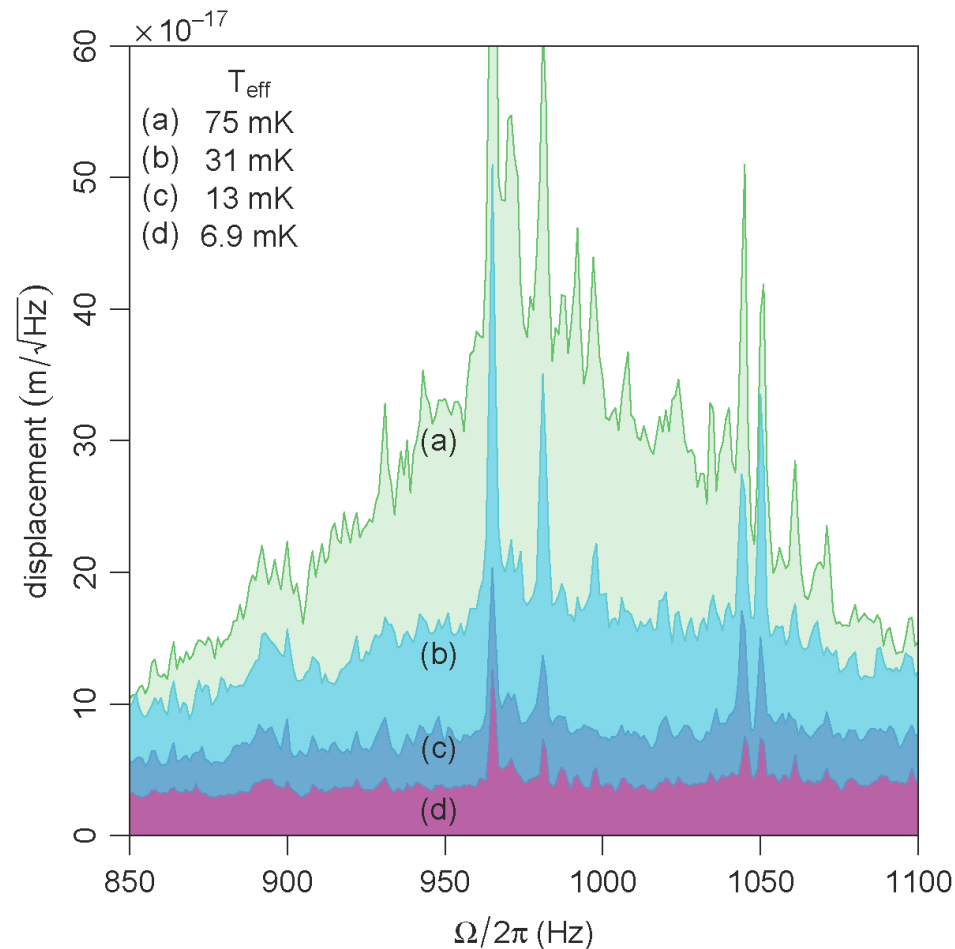
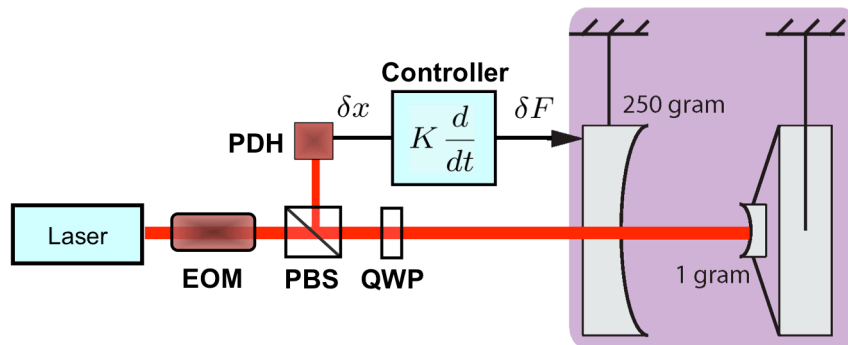
(with coherent state input)

- Powerful cooling technique for micro-mechanics --- not optimal for the gram-scale system



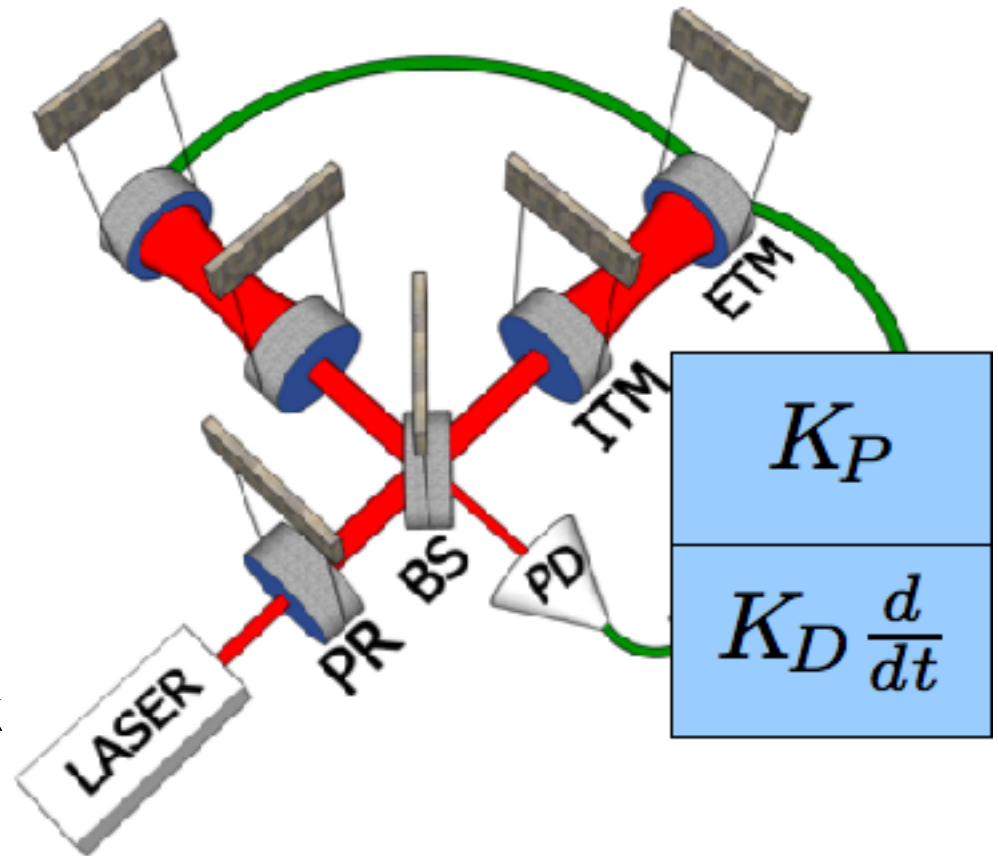
# Optical Trapping, Feedback Cooling

- Shortened cavity for reduced laser noise
- Electronic feedback of mirror displacement signal
  - Damps and stabilizes the optical spring
  - Plays to the strength of a “good measurement” cavity
  - Variant of previously known “cold damping” techniques
- Still limited by laser noise!



# Electro-Optical Trap

- Strong optical damping/restoring forces not available in Initial LIGO
- Instead, damping and restoring forces may be synthesized via feedback
  - Derivative feedback  
=> cold damping
  - Proportional feedback  
=> servo spring



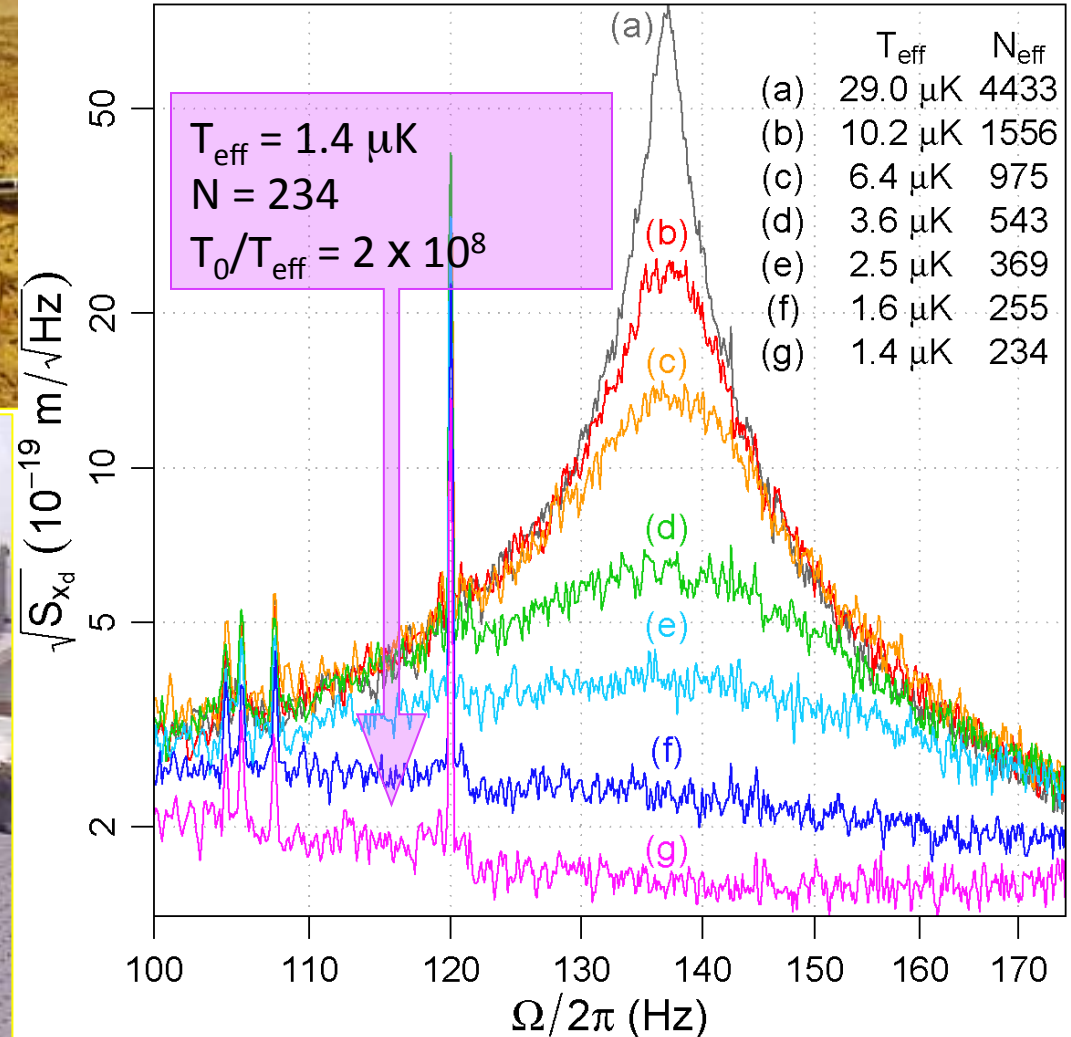
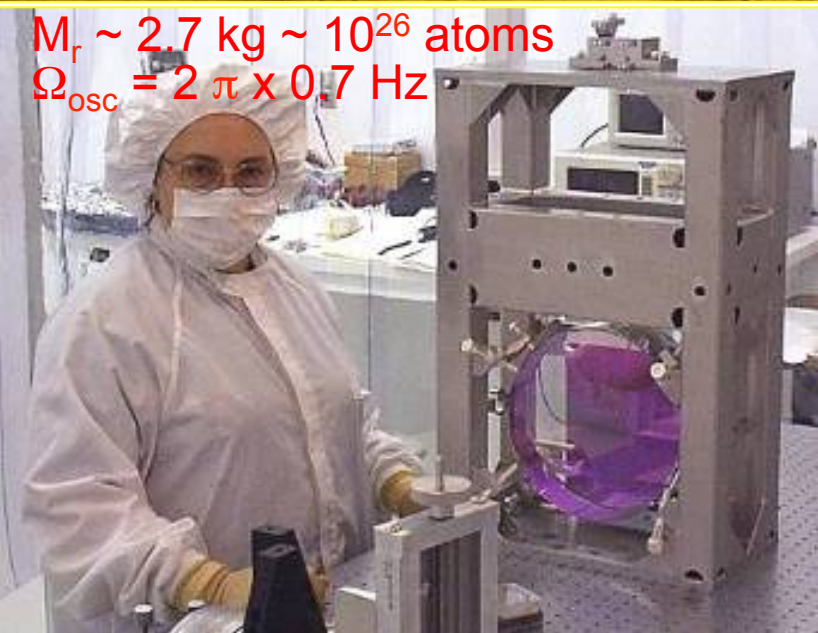
# Cooling of LIGO Mirrors

*New J. Phys.* **11** 073032 (2009)

Performed with Hanford  
4 km interferometer



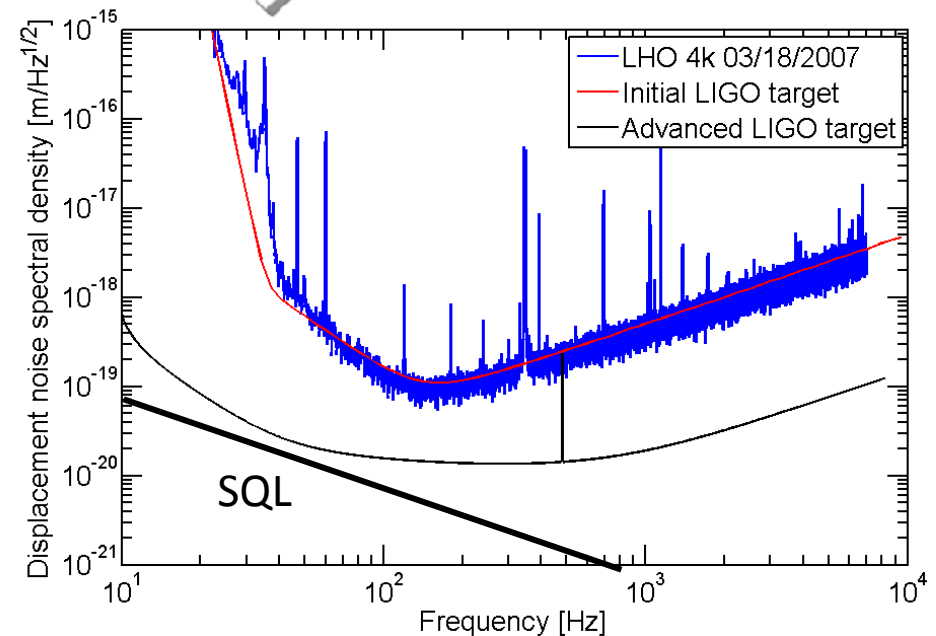
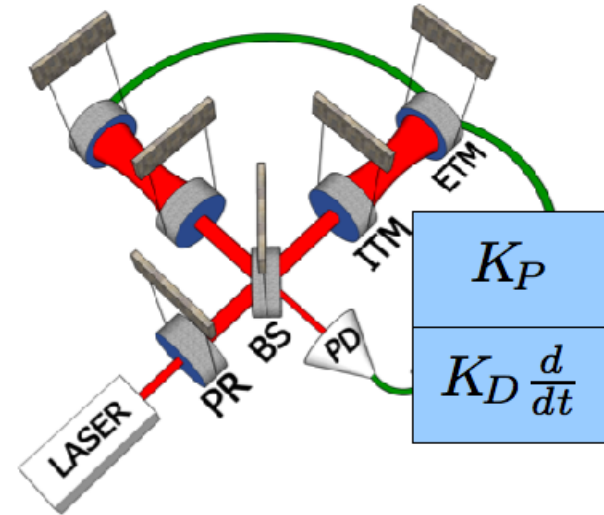
$M_r \sim 2.7 \text{ kg} \sim 10^{26} \text{ atoms}$   
 $\Omega_{\text{osc}} = 2\pi \times 0.7 \text{ Hz}$



# Reaching the SQL Enables Ground State Cooling

- Optimal feedback strategy has two parts
  - Shift the oscillator to the frequency of closest approach to the SQL
  - Subtract energy with a cold damping force
- Resulting occupation:

$$N_{\text{opt}} = \frac{k_B T_{\text{eff}}}{\hbar \Omega_{\text{eff}}} \approx \frac{S_x(\Omega_{\text{eff}})}{S_x^{(\text{SQL})}(\Omega_{\text{eff}})}$$



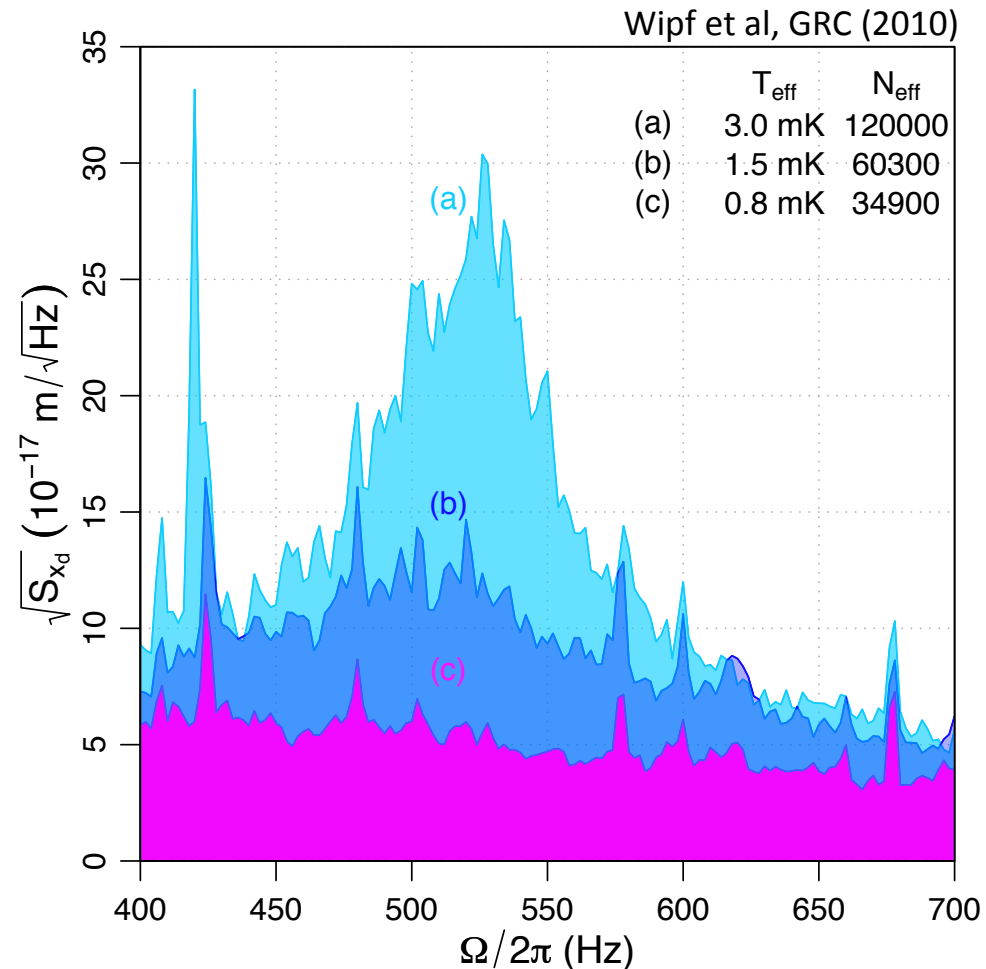
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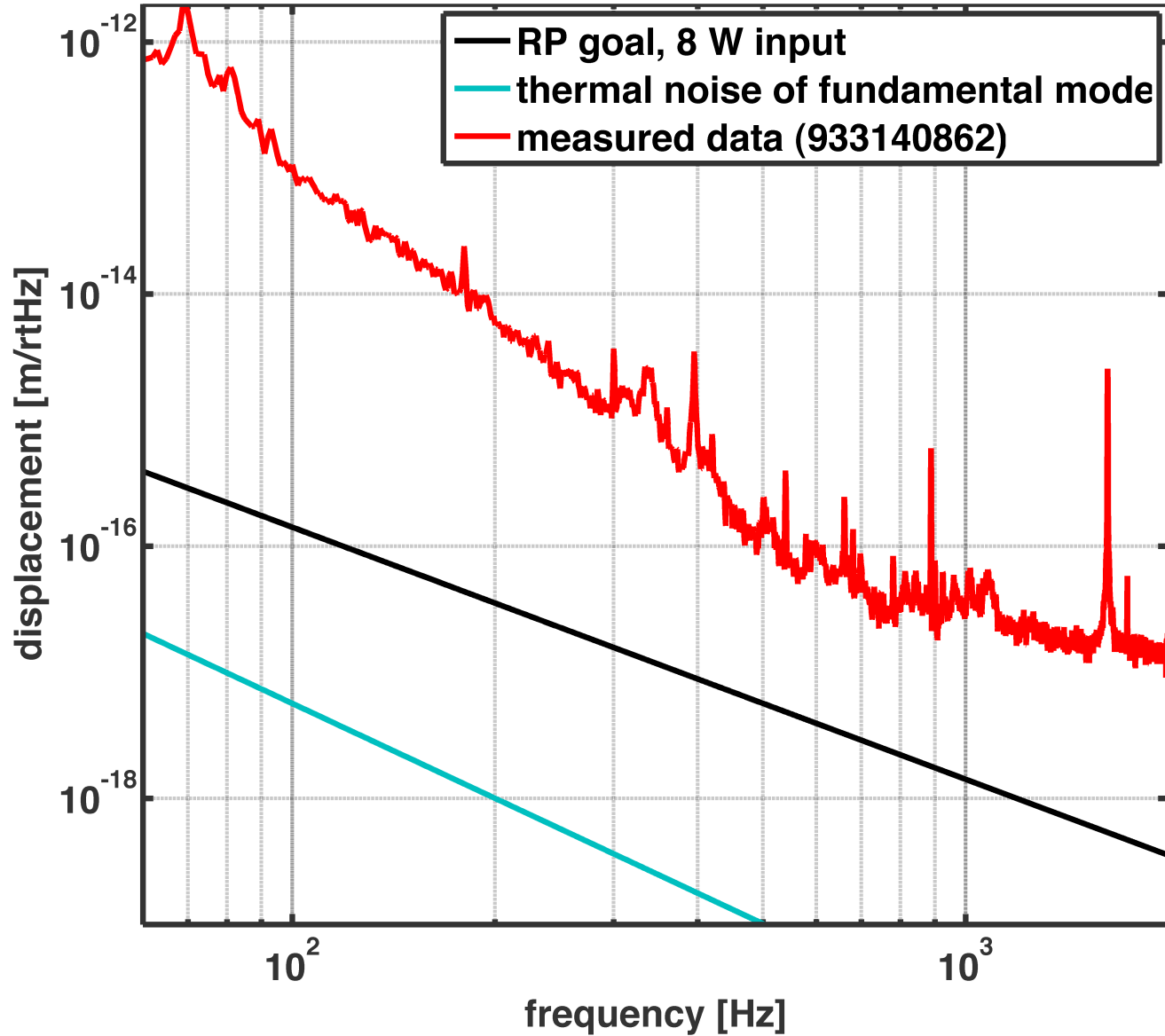


# Benchmark Cooling Run

- Early experiment with the completed testbed interferometer
- Another demonstration of feedback cooling and trapping technique
- Michelson subtraction of laser noise in the differential readout
- ~10x colder than single-cavity feedback cooling result
- Noise floor = ???

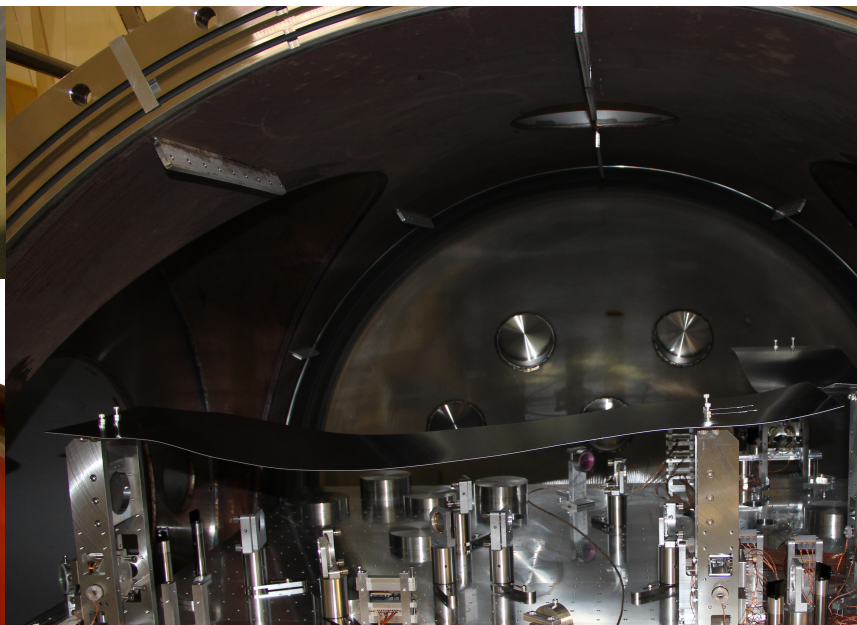
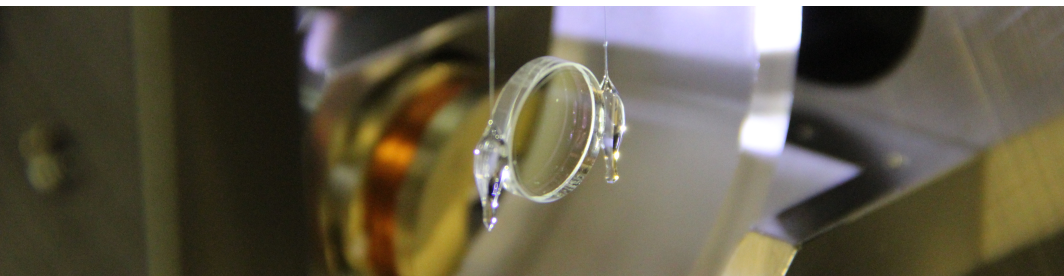


# Initial Situation





# Debugging



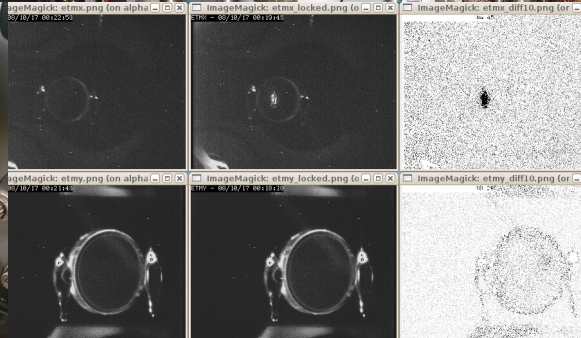
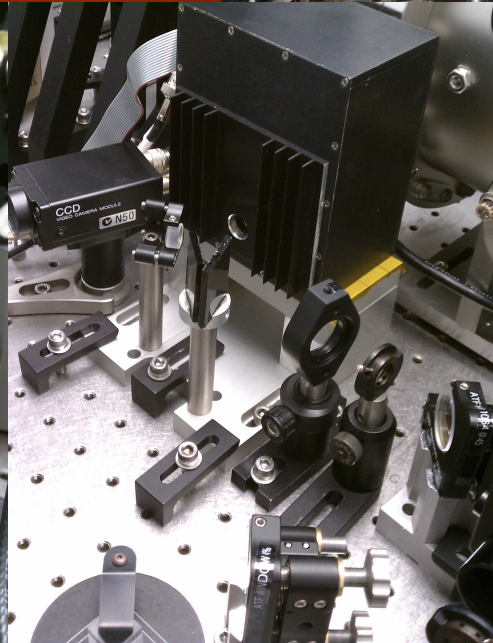
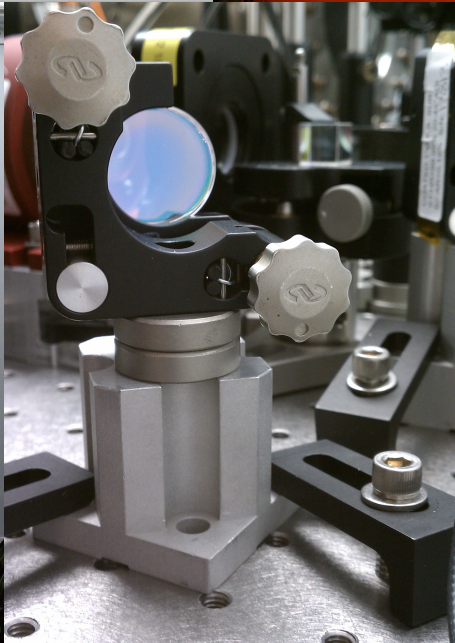
```
Quake Term
dacOut[jj][ii] = -limit;
overflowDac[jj][ii] ++;
// pLocalEpics->picsOutput.ovAccum ++;
overflowAcc ++;
diagWord |= 0x1000 * (jj+1);

#ifdef DAC_NOISE_SHAPING
dacOutState[jj][ii] += 65536 * dacOut[jj][ii];
int dac_out = dacOutState[jj][ii] >> 16;
dacOutState[jj][ii] -= dac_out << 16;
#else
int dac_out = dacOut[jj][ii];
#endif

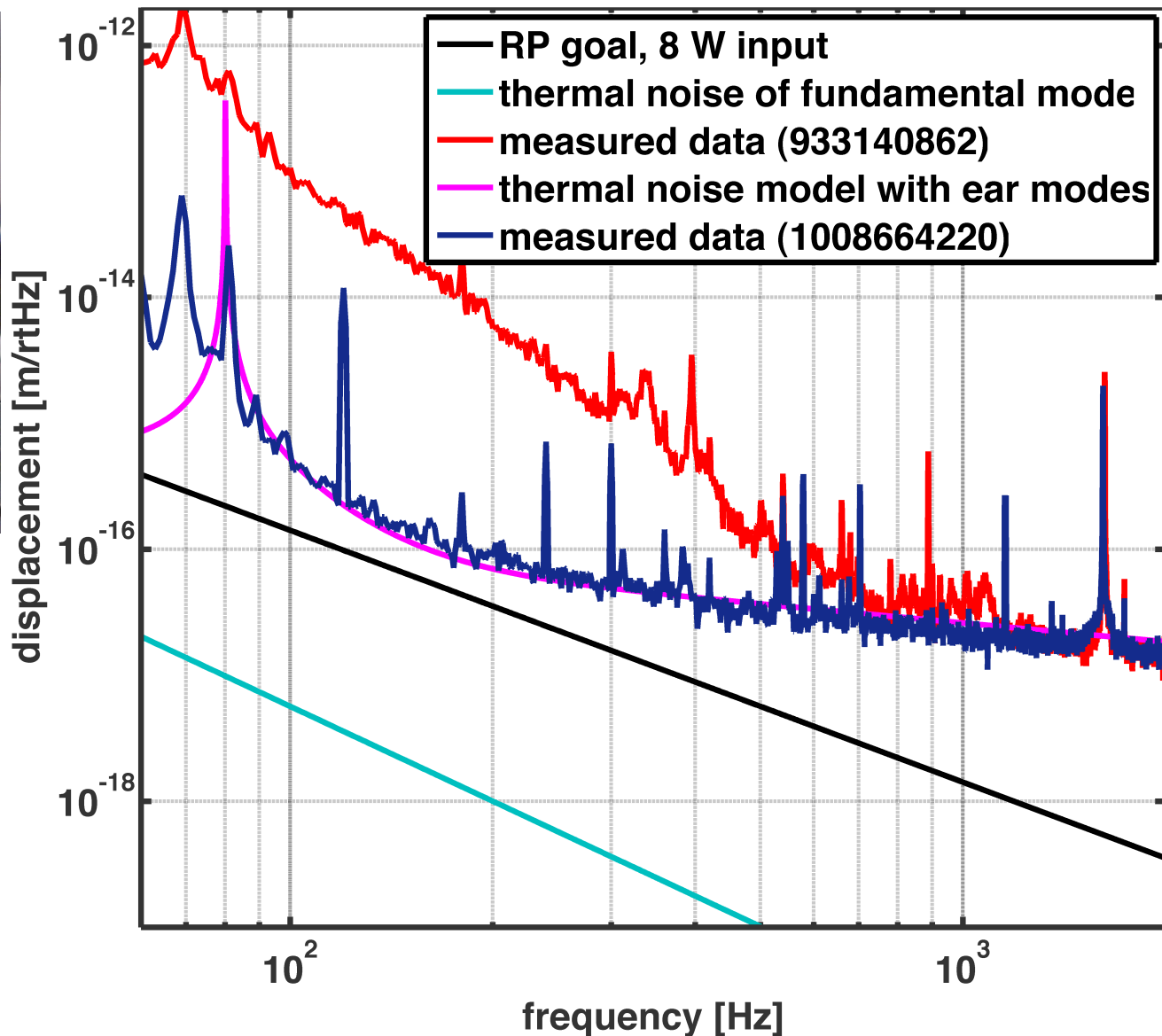
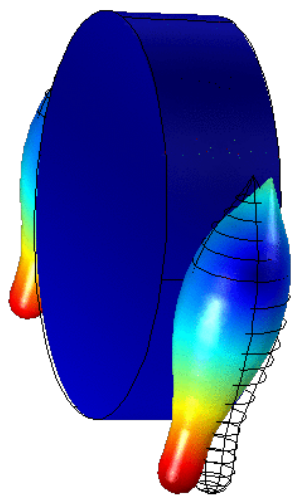
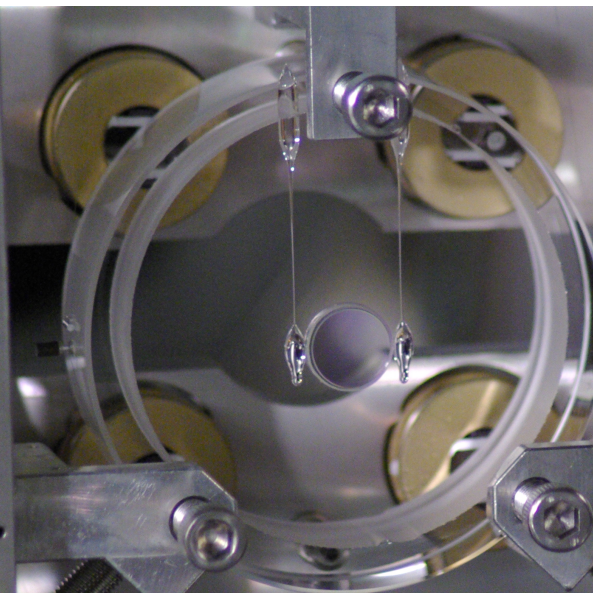
dac_out += offset;
// if ((ii == 0) && (jj == 2) && (clock16K == 0)) printf("md
*pDacData = (unsigned int)(dac_out & mask); printf("md
pDacData ++;

#ifdef OVERSAMPLE_DAC
#endif

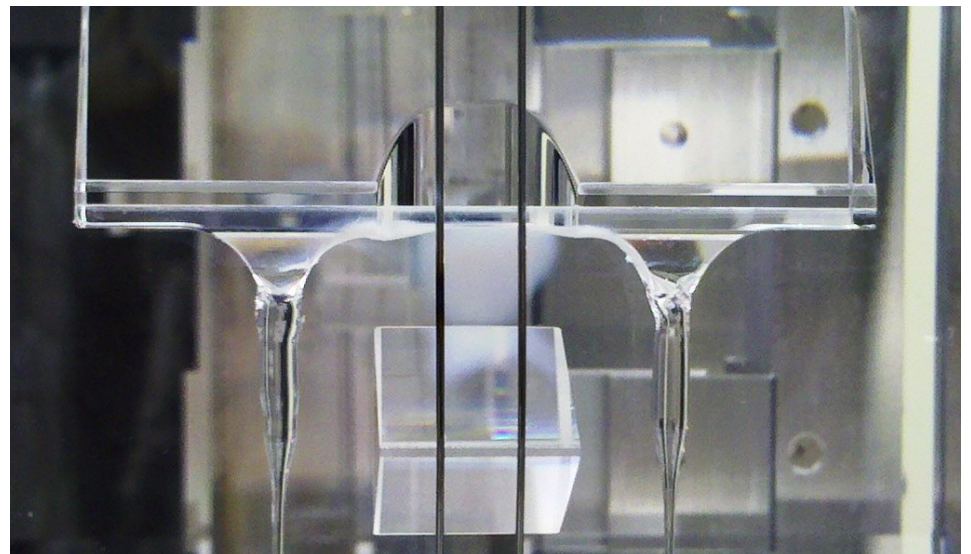
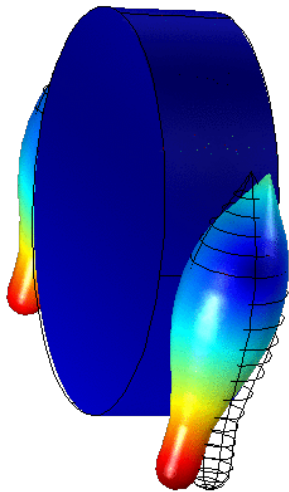
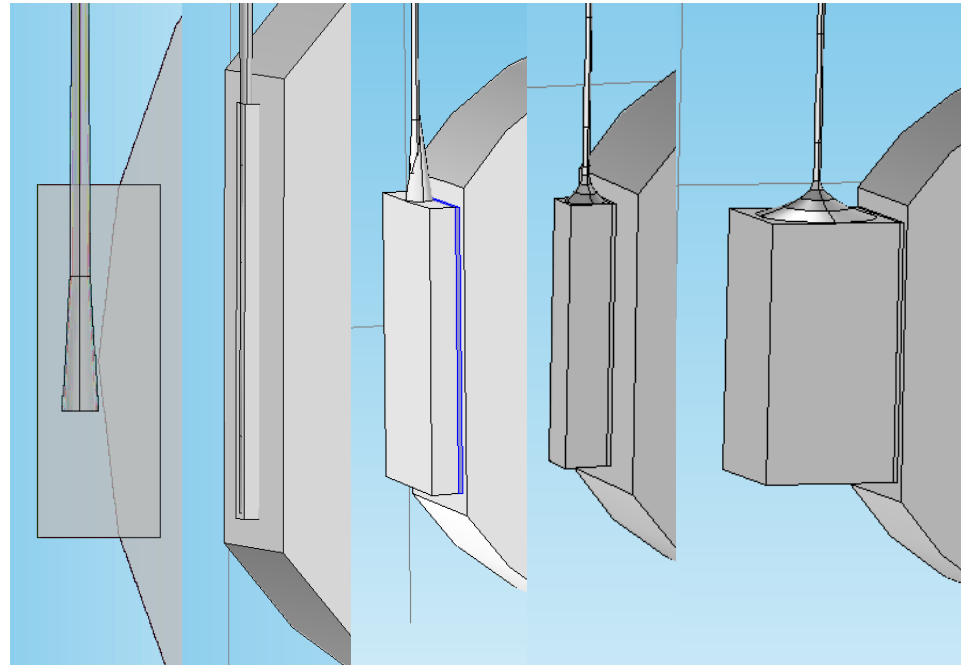
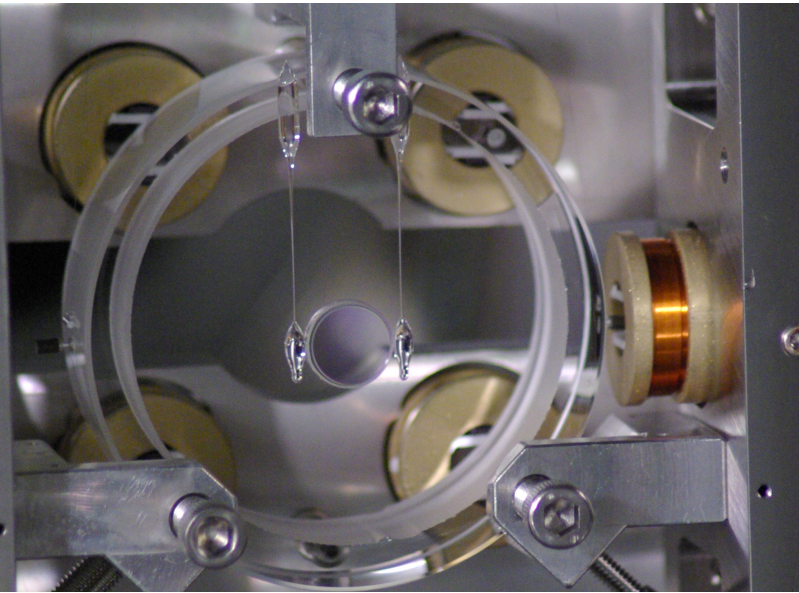
// DMA out dac values
gsaDacDma2(jj, cdsPciModules.dacType[jj]);
controller.c lines 1126-1148/1702 65%
```



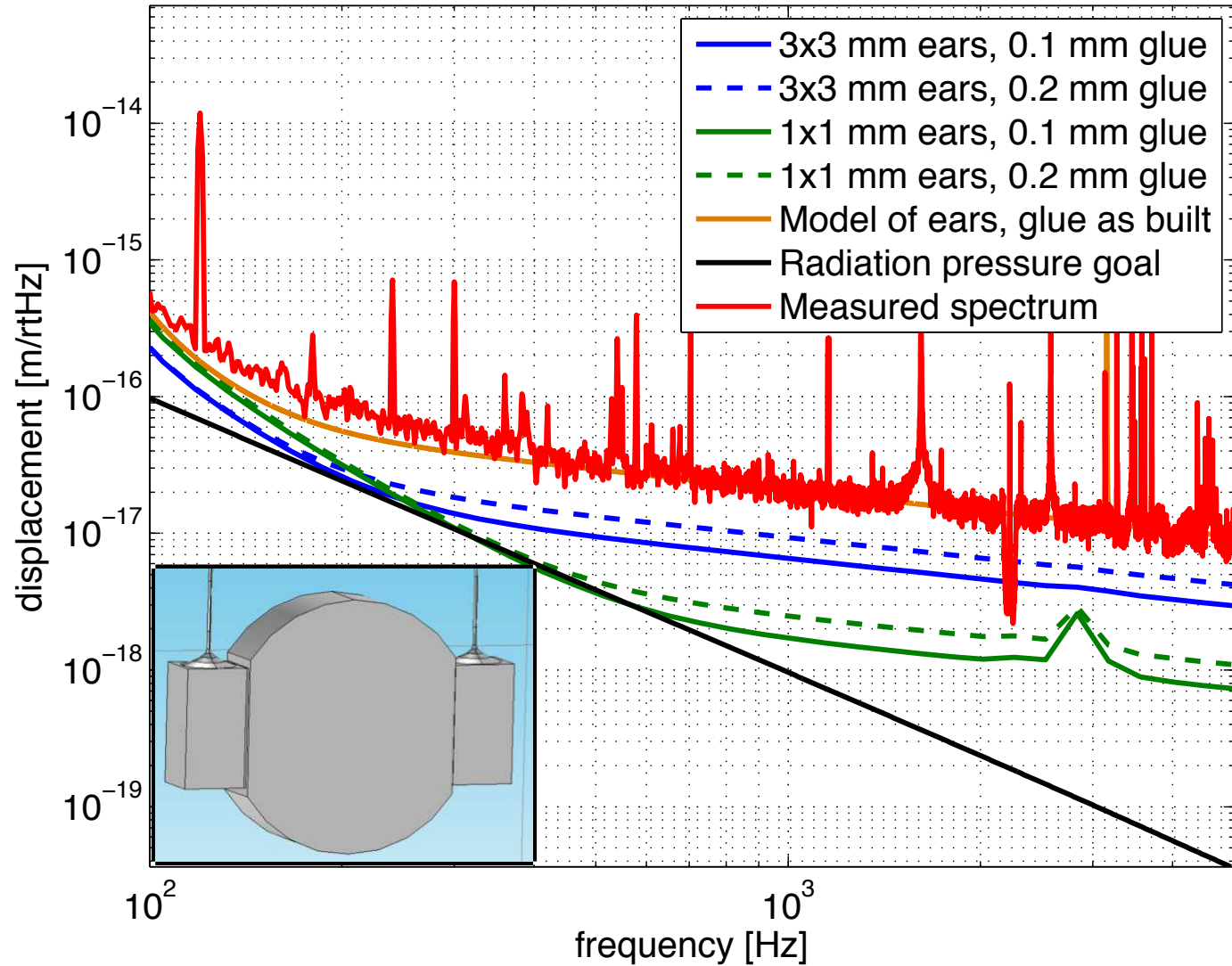
# Achieving the Thermal Noise Limit



# New Suspensions



# New Suspensions



# Overview

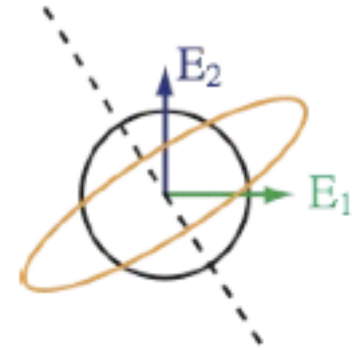
- Gravitational Wave Detectors & Quantum Limits
- Gram Scale Opto-Mechanics Experiment
  - Quantum States of Unusual Size
    - Quantum Back-Action vs. Thermal Noise
    - Toward Squeezed & Entangled Light



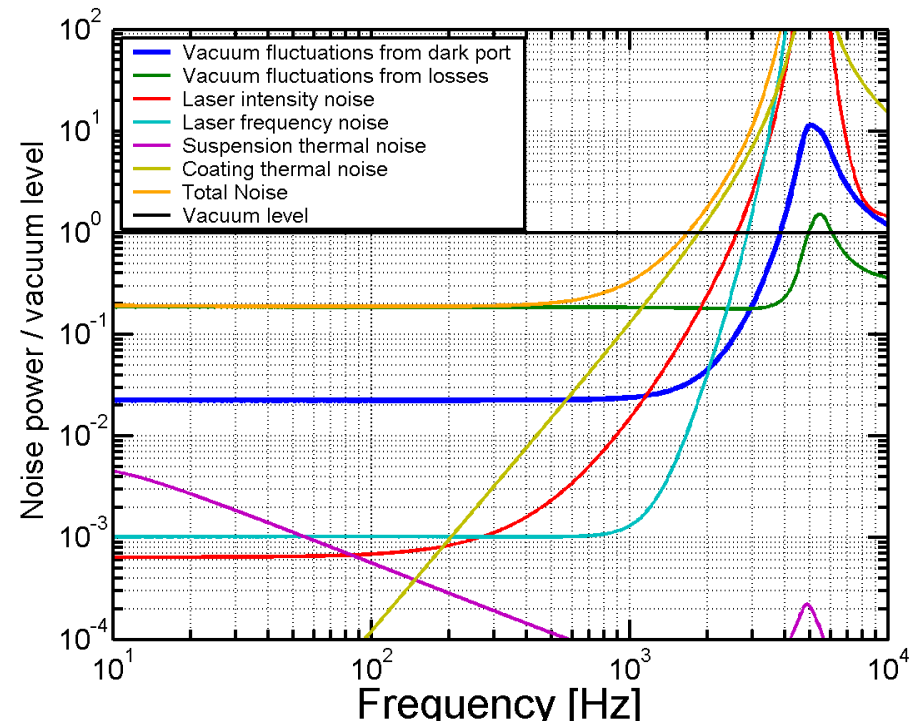
# Optical Spring Assisted Squeezing

- Radiation pressure correlates amplitude and phase quadratures

$$\begin{aligned} E_1^{\text{out}} &= E_1^{\text{in}} \\ E_2^{\text{out}} &= E_2^{\text{in}} - \frac{I}{M\Omega^2} E_1^{\text{in}} \end{aligned}$$

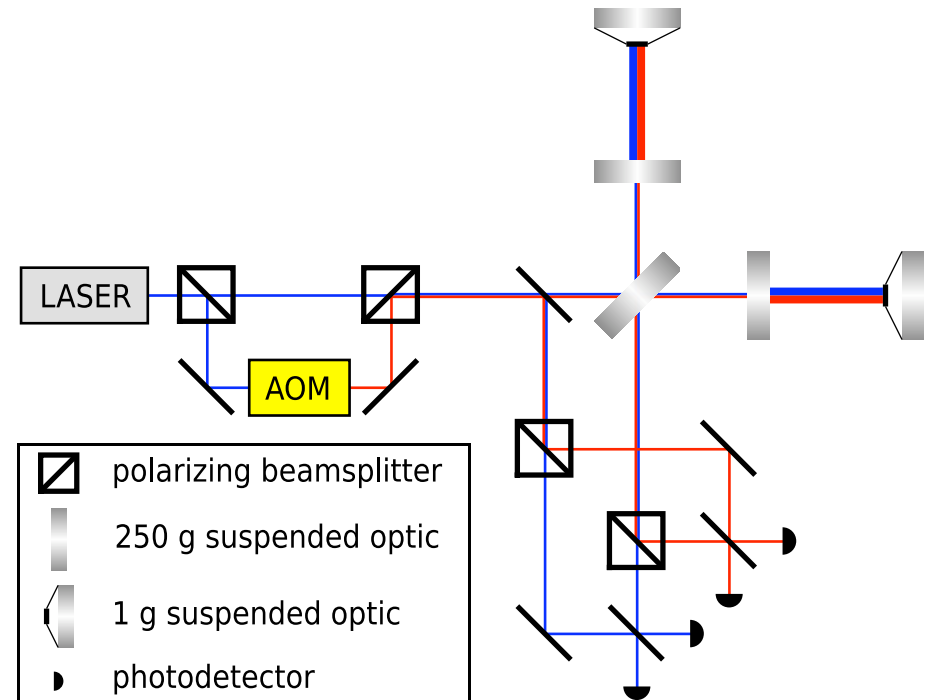


- Stiff optical spring enables broadband, frequency independent squeezing
- 7 dB squeezing predicted (if thermal noise requirements are met)



# Quantum Correlations in the Double Spring Optical Trap

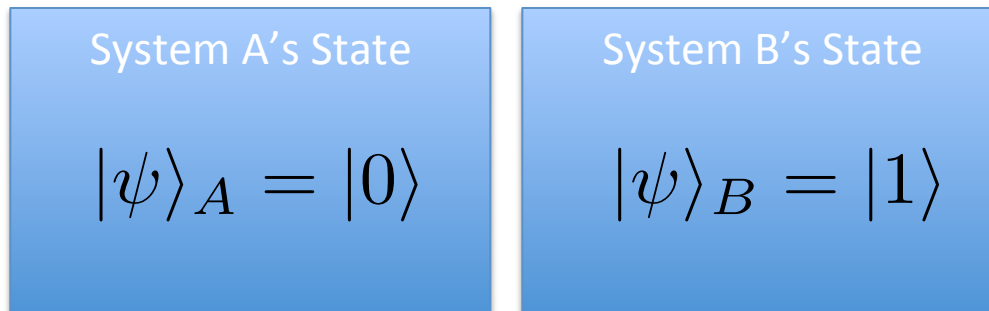
- Mirror driven by RP of two optical fields should generate quantum correlations linking both
- Quadrature Squeezing => Quadrature Entanglement
- Need to read out multiple quadratures of both fields to verify the entanglement (homodyne tomography)



# Entanglement

- Simplest case: two discrete systems

Joint state:  $|\psi\rangle_A |\psi\rangle_B = |0\rangle_A |1\rangle_B$



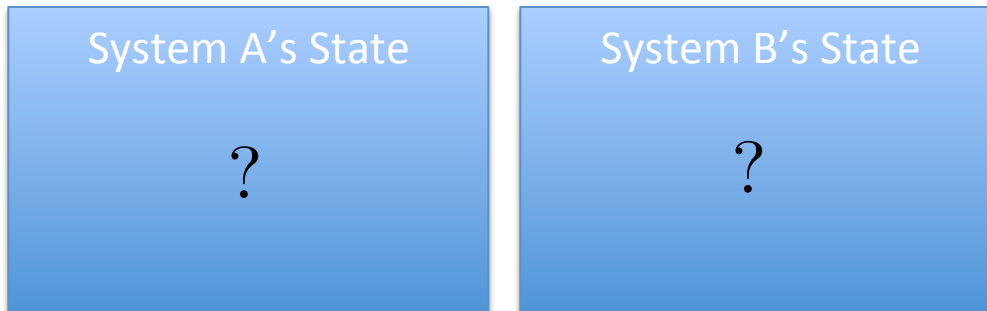
- We have complete knowledge of the system and can write down the state of each part separately



# Entanglement

- Simplest case: two discrete systems

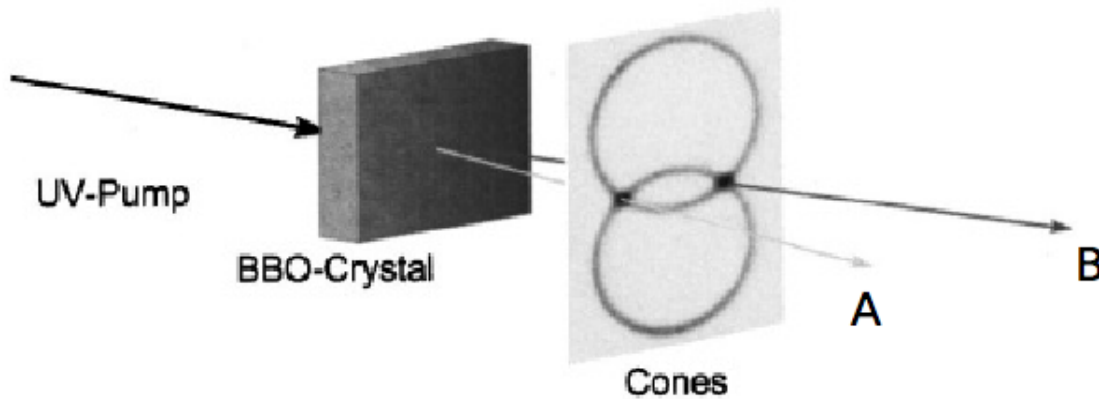
Joint state:  $|\psi\rangle_A |\psi\rangle_B = \frac{1}{\sqrt{2}} (|0\rangle_A |1\rangle_B + |1\rangle_A |0\rangle_B)$



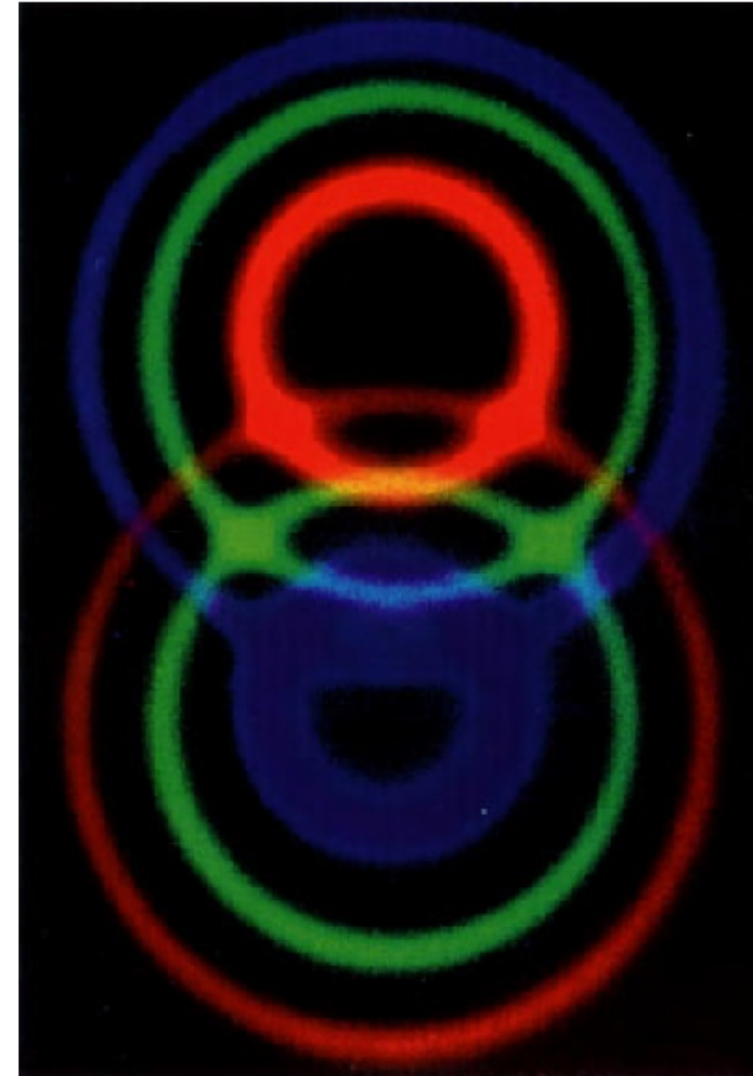
- This joint state is *entangled*: the state of A can no longer be described on its own (without reference to B)

# Optical Realization of Entanglement

## Photon polarization

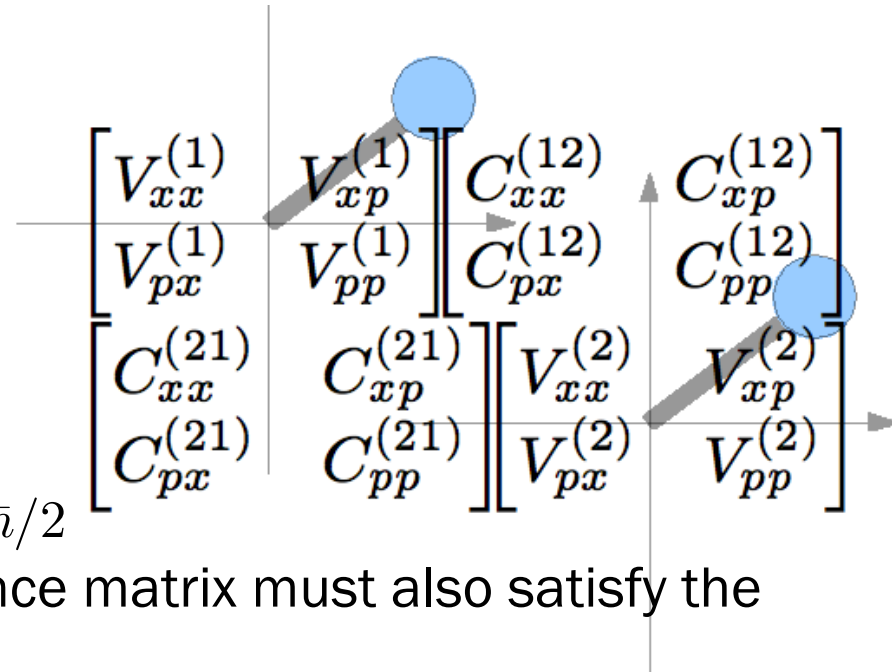


$$|\psi\rangle_{\text{joint}} = \frac{1}{\sqrt{2}} (|H\rangle_A |V\rangle_B + |V\rangle_A |H\rangle_B)$$

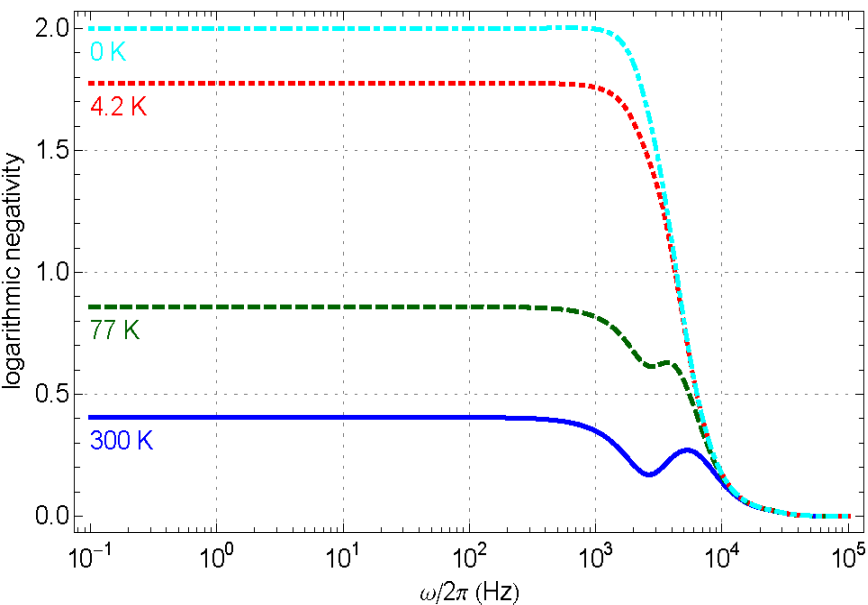
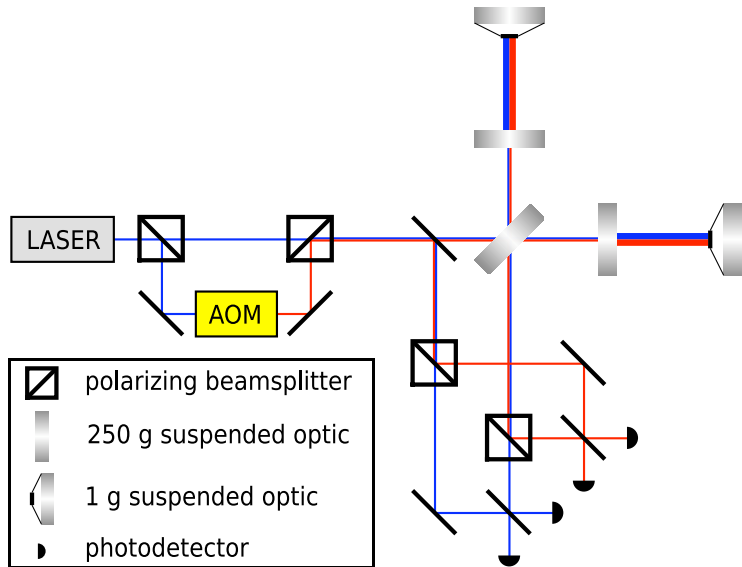


# Quantification of Entanglement

- Ensemble of homodyne detector measurements gives us a variance matrix.  
Is it entangled?
- Variance matrix is constrained by an uncertainty principle, the matrix generalization of  $\Delta x \Delta p \geq \hbar/2$
- The time reversed ( $p \Rightarrow -p$ ) variance matrix must also satisfy the same constraint
- Simon's entanglement criterion
  - Apply time reversal to *one subsystem only*
  - If the state is entangled, this operation is unphysical, so there may be a violation of the uncertainty principle
- “Logarithmic Negativity” entanglement measure is based on quantifying this violation



# Double Spring Assisted Entanglement



- Mirror driven by quantum RP of multiple optical fields generates quantum entanglement
- Exploits advantages of the optical trap configuration
  - High power stability permits strong coupling via the mirror
  - Optical entanglement becomes robust against thermal noise
  - Possible to entangle fields of **different wavelengths**

# Summary

- GW detectors now being built will:
  - Attain the Standard Quantum Limit
  - Approach the ground state of motion of their kg-scale test masses
  - Detect gravitational waves
- Gram-scale experiment has demonstrated:
  - Classical radiation pressure forces that dominate over the mechanical forces
  - Trapping and cooling with RP and feedback, laser noise limited
  - Cancellation of laser noise in the Michelson configuration
  - Broadband sensitivity reaching the limit set by suspension thermal noise
- A suspension upgrade to mitigate the thermal noise should reveal:
  - Quantum radiation pressure
  - Squeezing and entanglement



# Closing Credits

- Prof. Nergis Mavalvala
- Thomas Corbitt, Tim Bodiya, Eric Oelker, Abraham Neben
- Sarah Ackley, Nancy Aggarwal, Lisa Barsotti, Rolf Bork, Yanbei Chen, Fred Donovan, Sheila Dwyer, Matt Evans, Peter Fritschel, Edith Innerhofer, Tomoki Isogai, Alex Ivanov, Junghyun Lee, Myron MacInnis, Fabrice Matchard, Rich Mittleman, Helge Müller-Ebhardt, David Ottaway, Henning Rehbein, Daniel Sigg, Nicolás Smith-Lefebvre, Stan Whitcomb, Marie Woods, Mike Zucker
- LIGO Laboratory colleagues and the LIGO Scientific Collaboration

