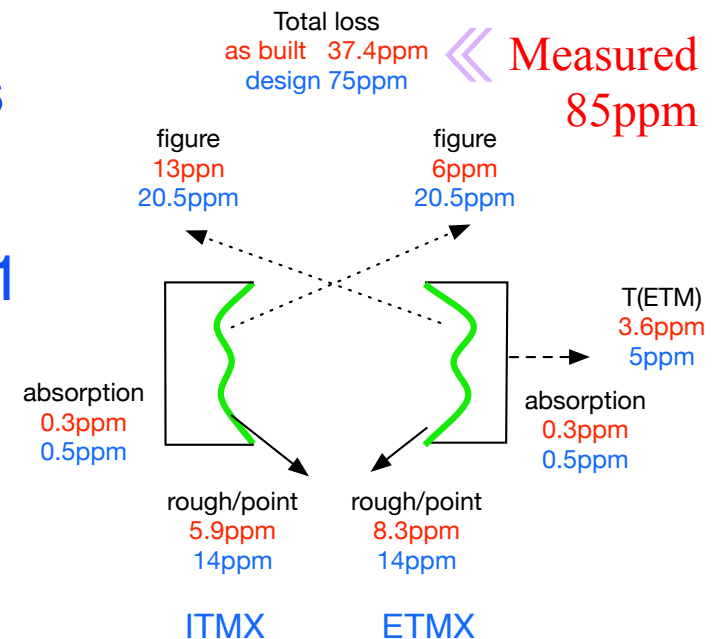




# Mirror profile and intracavity field profile

Hiro Yamamoto LIGO/Caltech

- Introduction
- Mirror spatial frequency and arm loss
- Point scattering and intracavity field
- Spiral patterns on ETMs at L1 and H1
  - » Imbalanced noise by spiral patterns
  - » Direct measurement of the cone scattering by spiral pattern
- Polishing vs coating for the future
- Summary, question to be answered





# Mirror surface aberration, reflected field and intracavity field

$$E_{ref} = E_{ref}^0 \exp(i\omega t - ikz) \cdot \exp(2ikf(x,y))$$

$$= E_{ref}^0 \exp(i\omega t - ikz)(1 - 2(kf)^2) + E_{ref}^0 \exp(i\omega t - ikz) i2kf$$

$$f(x,y) = \sum_{nx,ny} a_{nx,ny} \sin(n_x \omega_x x + n_y \omega_y y + \varphi_{nx,ny})$$

$$dF = E_{ref}^0 k \sum_{nx,ny} a_{nx,ny} (\exp(i\Phi_{nxny}^+) - \exp(i\Phi_{nxny}^-))$$

$$\sigma^2 = \frac{\iint dx dy f^2}{S}$$

Small size aberration →

$$dW = \iint dx dy |E_{ref}^0|^2 4k^2 f^2$$

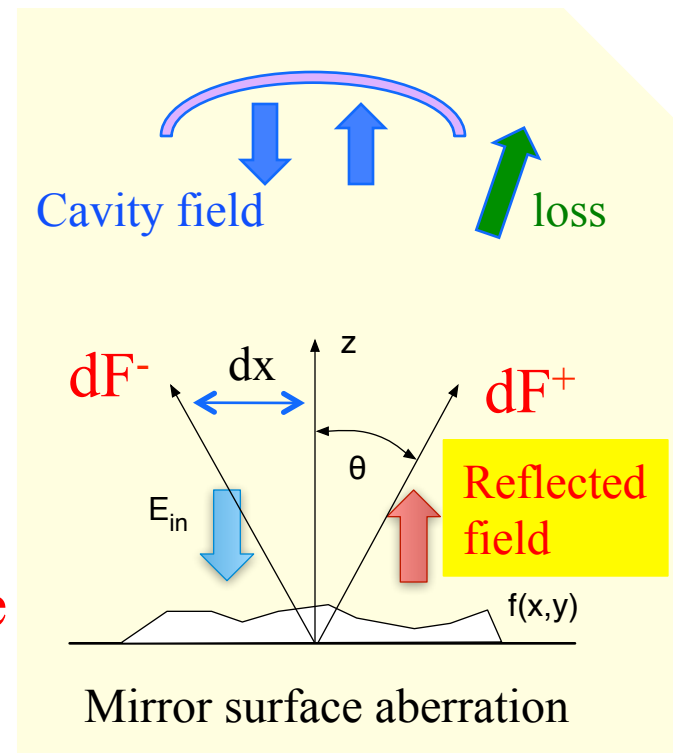
$$= P_{ref}^0 \left( \frac{4\pi\sigma}{\lambda} \right)^2 S$$

\* Periodical aberration scatters to a fixed angle

$$\theta \sim n \sqrt{\omega_x^2 + \omega_y^2} / k \sim n \cdot \lambda / a, \quad dx = L_{cav} \cdot \theta \sim L_{cav} \cdot \lambda / a$$

\* Small size aberration scatters back spherically

$$loss = (1 - (\text{mirror size} / \text{cavity length})^2) \cdot dW$$



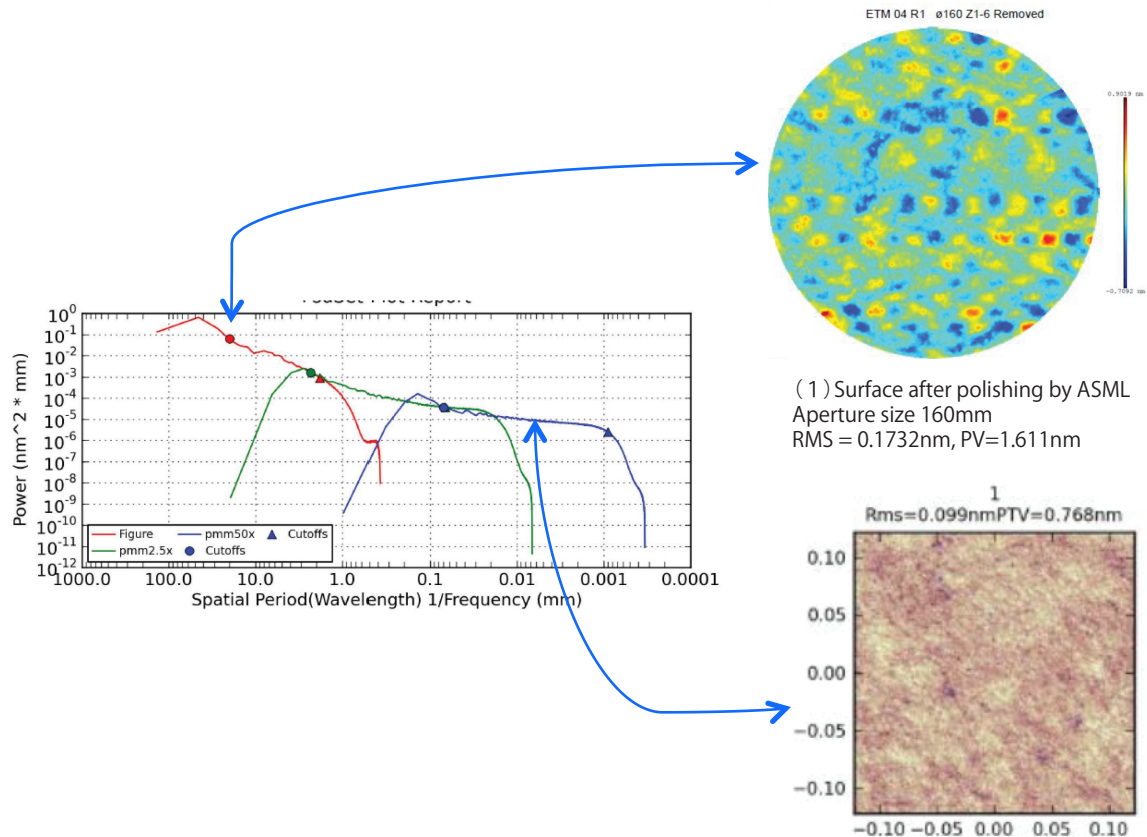


# Measured mirror profile and intracavity field

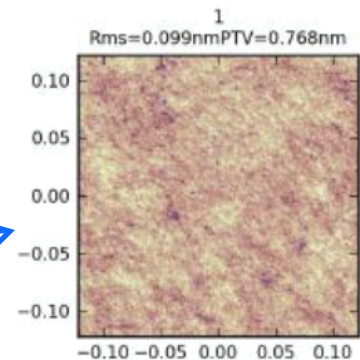
Mirror profile	Spatial resolution	Field angle	Cause and effect in cavity
Phase map	> 1mm	$< 2 \times 10^{-4}$ rad, < 1m at 4km	Intracavity fields and near the edge of mirror, cavity modea
PSD, RMS, BRDF	1 $\mu$ m ~ a few mm by PMM, + phase map	~ large angle	Characterization of <b>continuous structure</b> , field scattered out to large angle
Integrating sphere	fraction of mm	> 5 degree	Total scattering to almost all angle, effects of <b>non contiguous (point) structures</b> captured. Near backward is covered by others.

COC mirror data (characteristics of mirror) +  
appr. Maxwell eq. with rigorous boundary cond.  
⇒ IFO observable

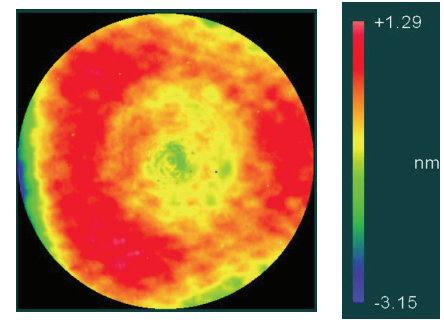
# Raw data of mirror profiles



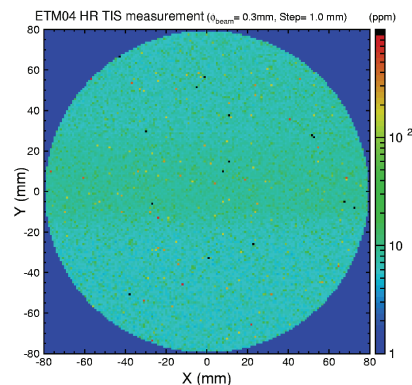
(1) Surface after polishing by ASML  
Aperture size 160mm  
RMS = 0.1732nm, PV=1.611nm



(3) Surface after polishing measured by PMM(phase measuring microscope) with magnification of 50.  
0.25mm x 0.25mm square near center.  
RMS = 0.099nm, PV=0.768nm



(2) Surface after multilayer coating by ion sputtering  
Aperture 160mm  
RMS = 0.563nm, PV=4.436nm

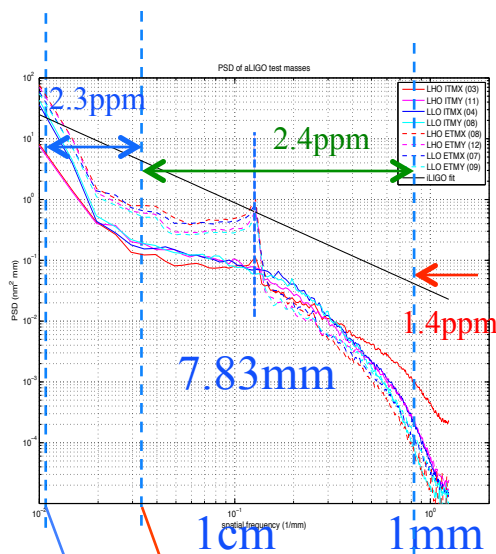


(4) Reflectance measured by an integrating sphere with the scattering angle larger than 1°. The size of the laser is 0.3mm, with spacing 1mm.  
RMS using all data points is 98ppm. RMS is 20ppm after excluding 15 points with reflectance > 1000ppm



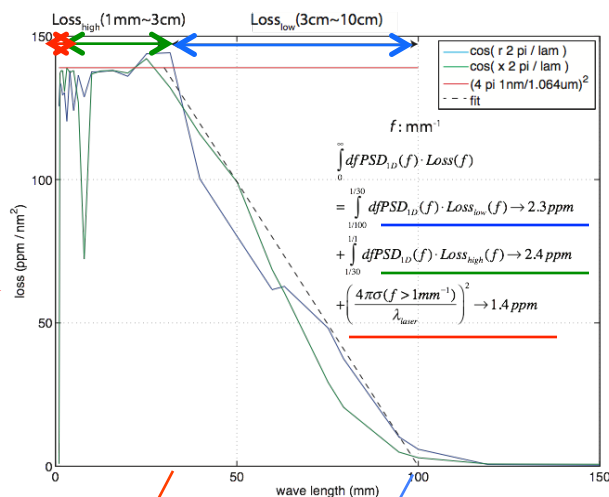
# aLIGO cavity scattering loss by wavelength

## Mirror surface profile

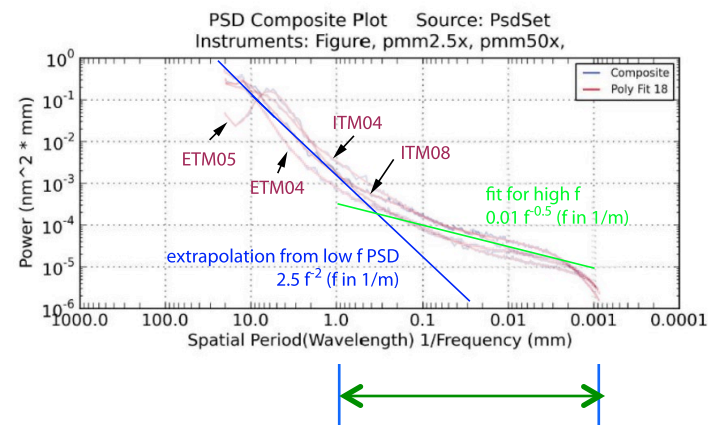


Geometrical acceptance

## Loss of intracavity field vs wavelength



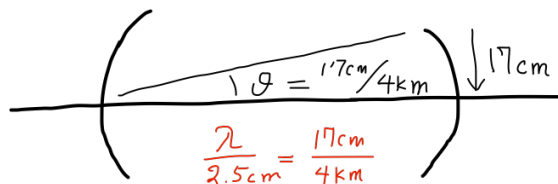
## Not so simple PSD



$$\sigma(1\text{mm} \sim 1\mu\text{m})^2 = \int_{1/1\text{mm}}^{1/1\mu\text{m}} PSD(f) df = (0.14\text{nm})^2$$

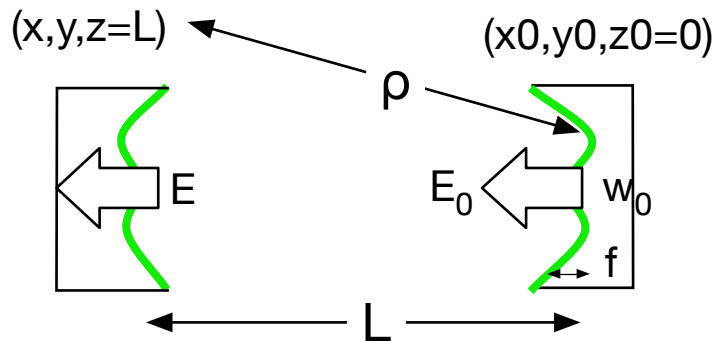
$$\left( \frac{4\pi\sigma(1\text{mm} \sim 1\mu\text{m})}{\lambda} \right)^2 = 3\text{ppm}$$

$$\left( \frac{\sigma(3\text{mm} \sim 1\text{mm})}{\sigma(1\text{mm} \sim 1\mu\text{m})} \right)^2 = \frac{1}{40}$$



# Far field structures

field PSD( $\theta$ )  $\neq$  mirror PSD( $f$ ), const BRDF  $\Rightarrow$  wrong loss



$$E(x, y, z) \equiv \frac{i}{\lambda} \iint dx_0 dy_0 E_0(x_0, y_0, z_0) \frac{\exp(-ik\rho)}{\rho} \cos\theta = F_0 + dF$$

$$\Delta x = x - x_0, \Delta y = y - y_0, L = z - z_0, k = 2\pi / \lambda$$

$$\rho = \sqrt{\Delta x^2 + \Delta y^2 + L^2}, \cos\theta = \frac{L}{\rho}$$

$$dF(x, y, z) \approx \sqrt{\frac{2}{\pi}} \frac{1}{w_0} \frac{i}{L \cdot \lambda} \iint dx_0 dy_0 2ikf(x_0, y_0) \exp(-ik \frac{\Delta x^2 + \Delta y^2}{2L}) \exp(-\frac{x_0^2 + y_0^2}{w_0^2}) \quad \text{small aberration}$$

$$\approx \sqrt{\frac{2}{\pi}} \frac{1}{w_0} \frac{i}{L \cdot \lambda} \exp(-ik \frac{x^2 + y^2}{2L}) 2ik \iint dx_0 dy_0 f(x_0, y_0) \exp(ik \frac{x \cdot x_0 + y \cdot y_0}{L}) \quad \text{Fresnel approx}$$

Point source :  $dF \Rightarrow \text{const BRDF} \Rightarrow 2\pi dS / \lambda^2 \times \text{true scattering}$

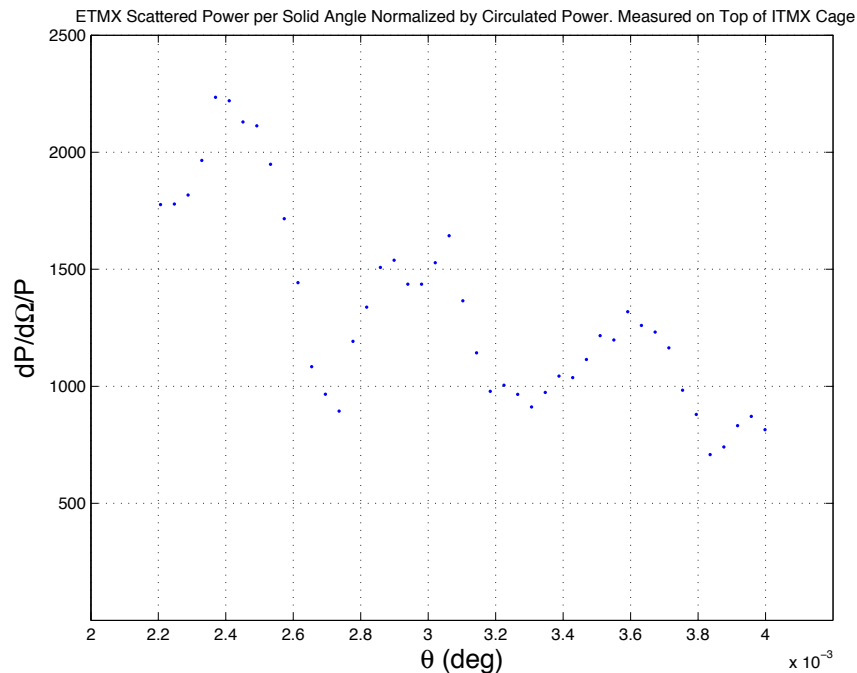
$$\text{PSD to } dF : |dF[x, y, z]|^2 = \frac{32\pi^2}{w^2 \lambda^4 L^2} \left| \iint_{-\infty}^{\infty} \iint_{-\infty}^{\infty} \Delta[f_u, f_v] \delta\left[f_u - \frac{x}{\lambda L}, \varepsilon\right] \delta\left[f_v - \frac{y}{\lambda L}, \varepsilon\right] df_u df_v \right|^2$$

$\Delta$  : 2D amplitude spectral density,  $\varepsilon \sim 1/a$  few cm

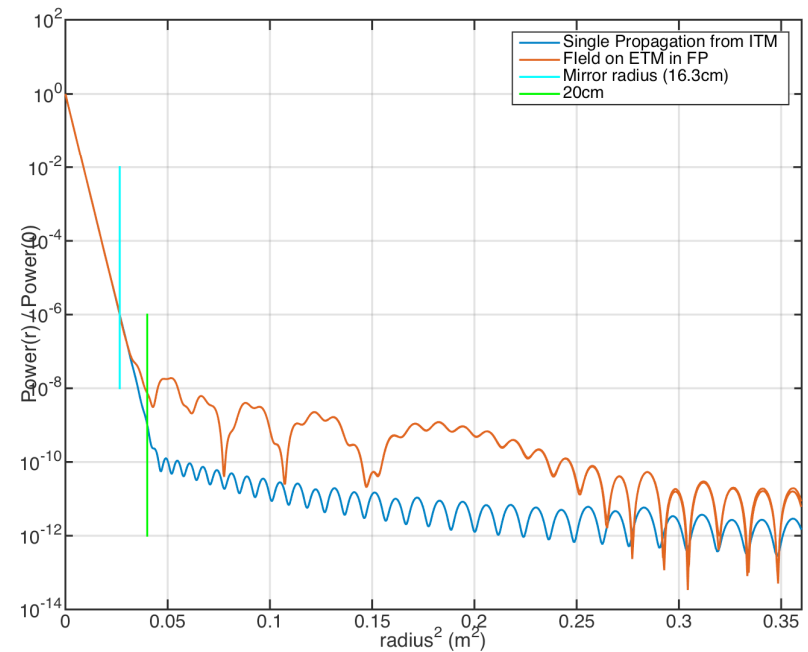


# Single propagation vs cavity field Airy ring outside of mirror

iLIGO data by Valera

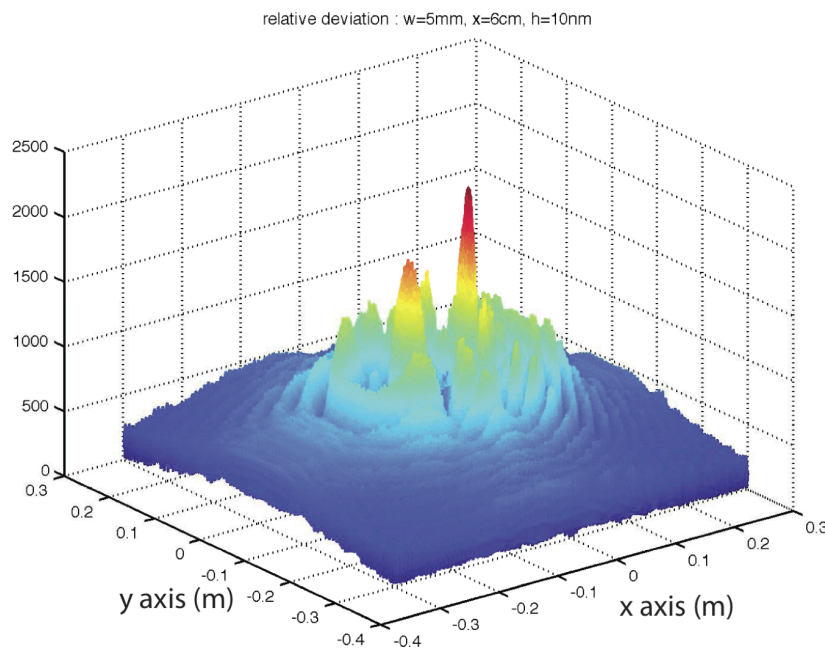


aLIGO simulation :  
single propagation vs  
resonating field around cavity



# Small anomaly induces widespread tiny disturbance

$$dW(loss) = \sum_{anomalies} \left( \frac{4\pi\sigma_a}{\lambda} \right)^2 S_a \cdot P_a$$



- Disturbance of fields by a point anomaly propagates out spherically
- Intracavity field is affected entirely, not partially
- Disturbance induced by a point anomaly is widespread weakly
- Difficult to measure the effect, except for using the total loss measurement





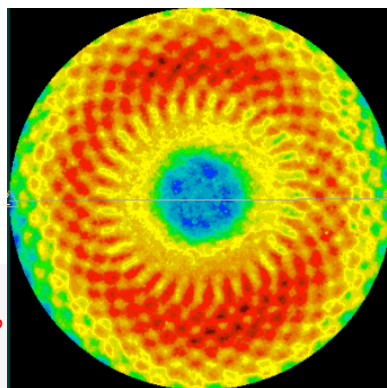
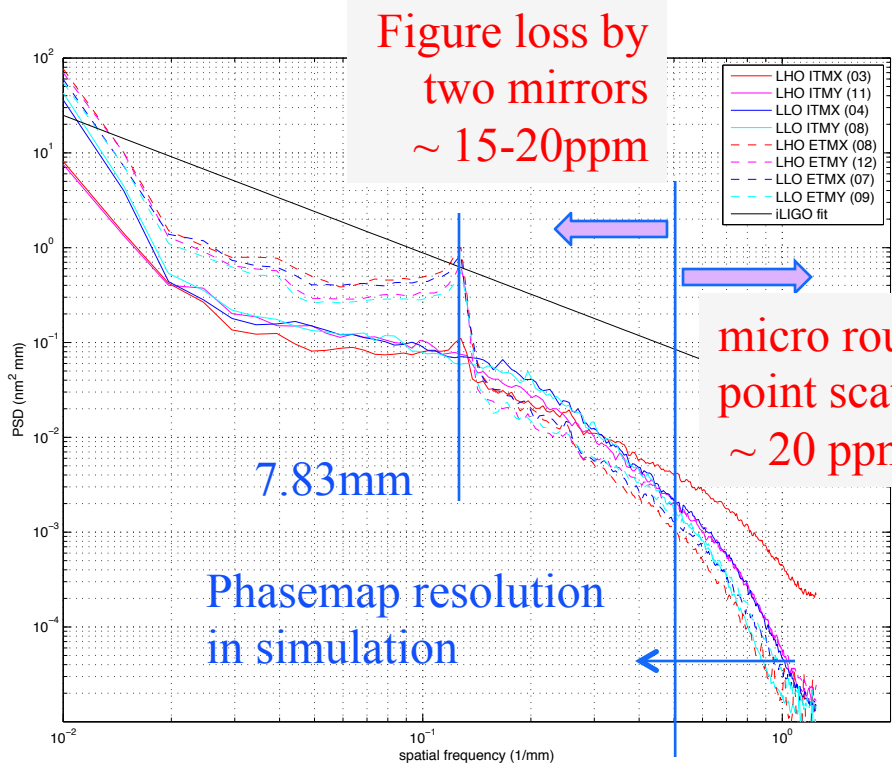
# LMA coating on ETMs

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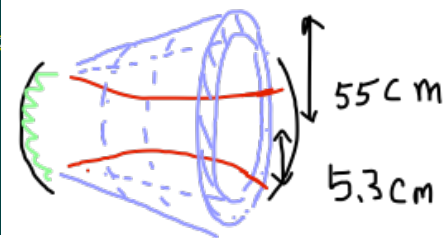
- This is about the installed ETMs at L1 and H1
- State of the art coating is presented in the talk by Laurent Pinard of LMA



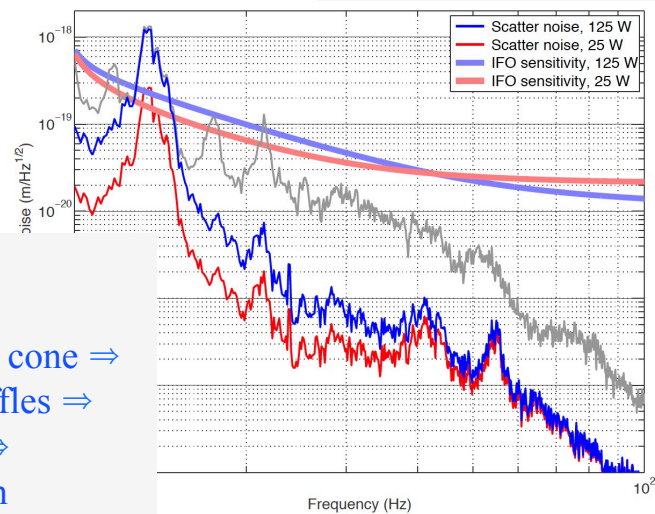
# Periodical structure on a mirror induces reflected field into a cone with a fixed angle



ETM07 map



T1300354 by PF, HY



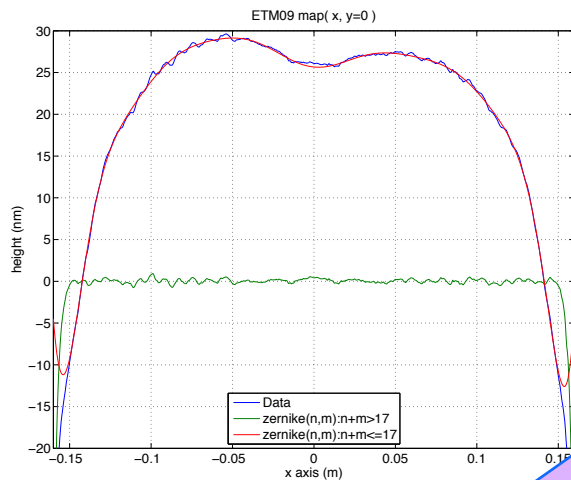
main beam ⇒  
 ETM reflection ⇒  
 larger angle scattering into cone ⇒  
 reflected by beam tube baffles ⇒  
 back scattered into ETM ⇒  
 merged into the main beam



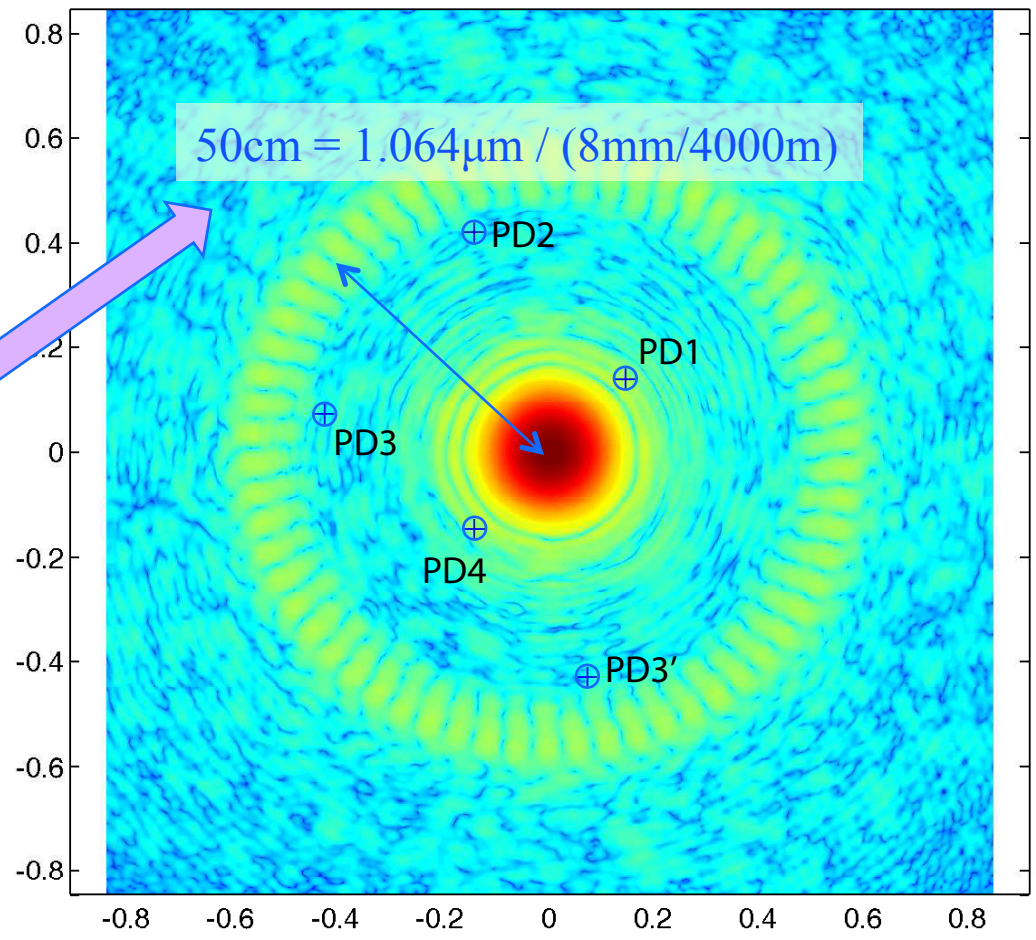
**LIGO**

# Detection of the scattering to cone using test mass baffle PDs

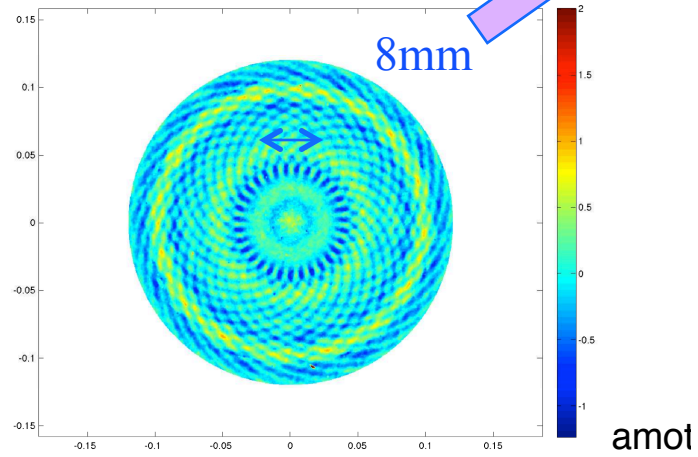
ETM09 map



Field going to ITM

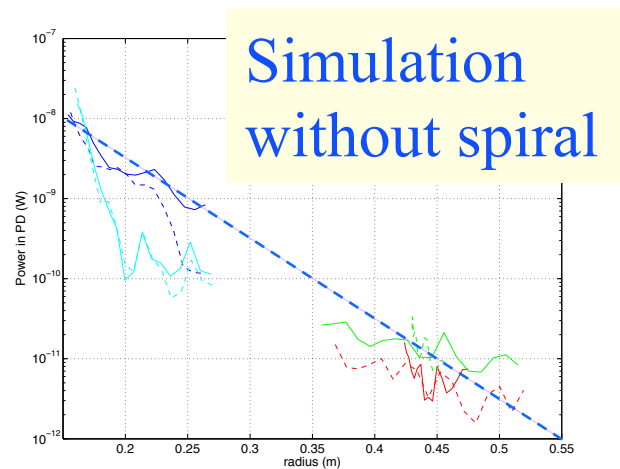
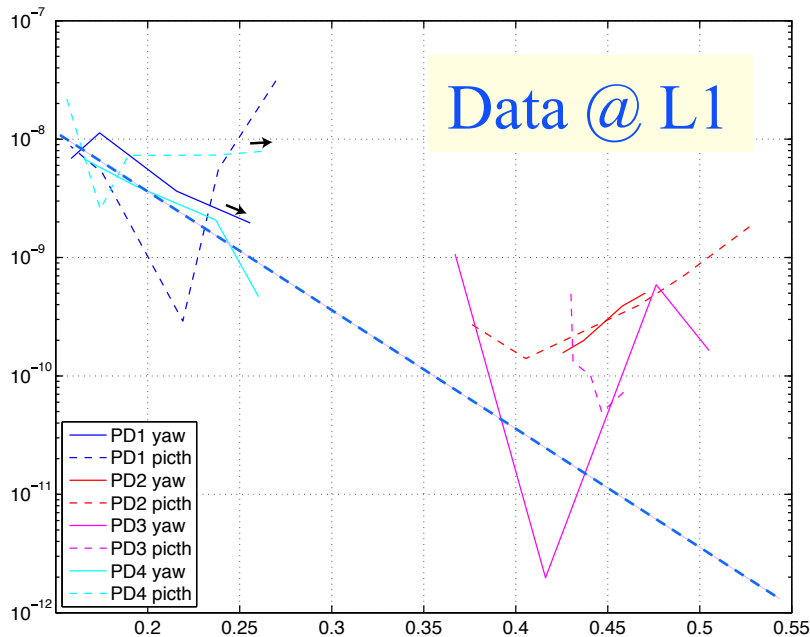
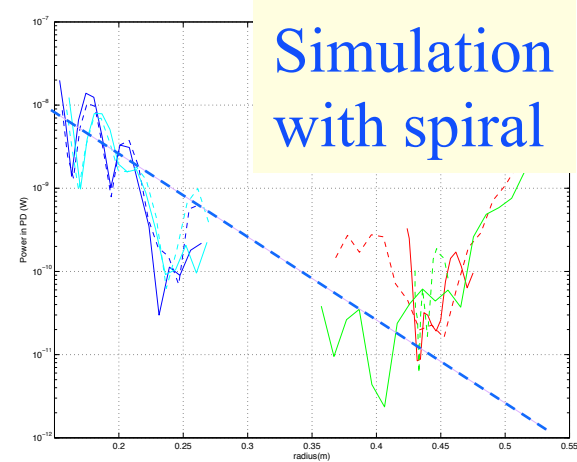
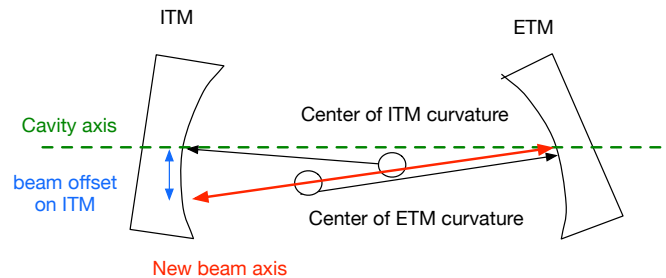
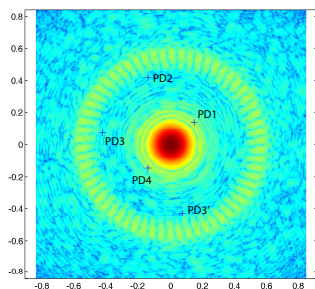


Spiral component



Real PD diameter is  $\frac{1}{4}$  of  $\odot$

# Signature at L1 ITM baffle PDs



Distance of PD from center



# Different backscattering noise?

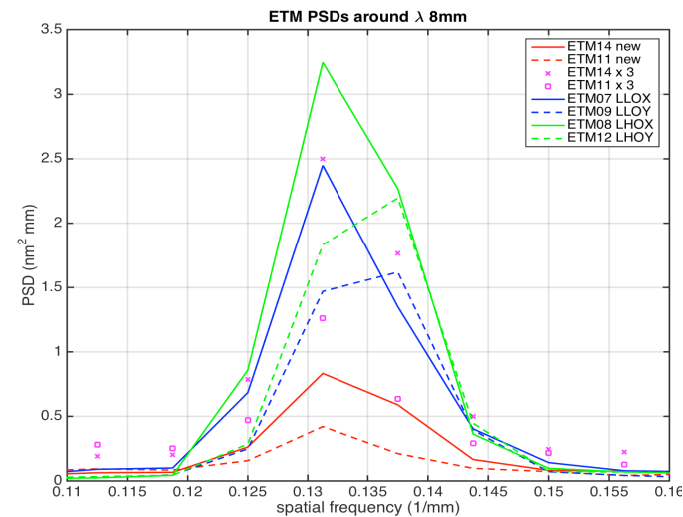
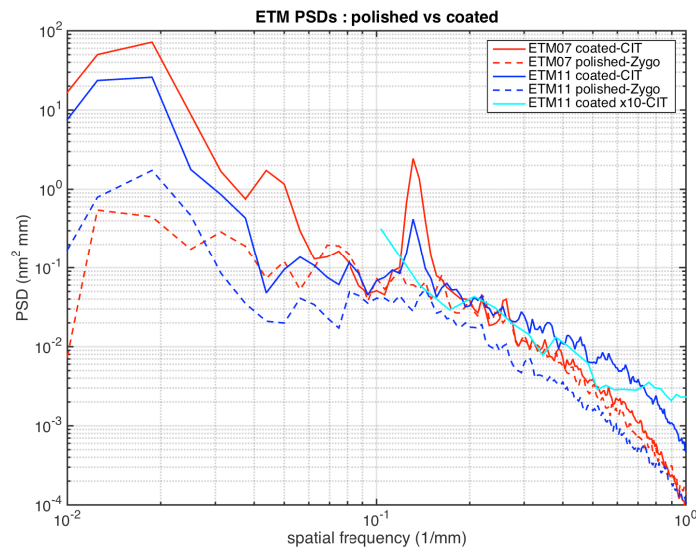
L1

H1

	ETM14	ETM11	ETM07	ETM09	ETM08	ETM12
power (45cm~70cm)	2.4	1.5	6.3	4.3	7.7	5.2
round trip loss	74	73	80	78	80	80
HOM	226	283	208	288	227	312



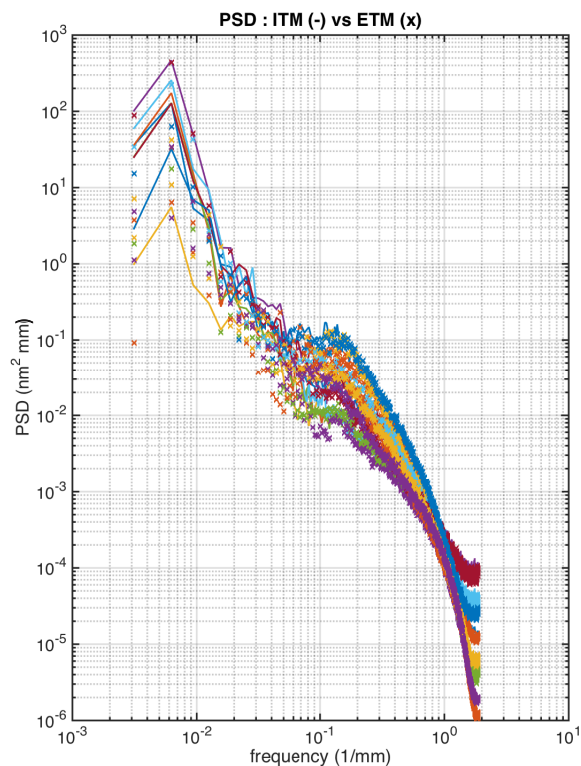
Small, but into a fixed direction



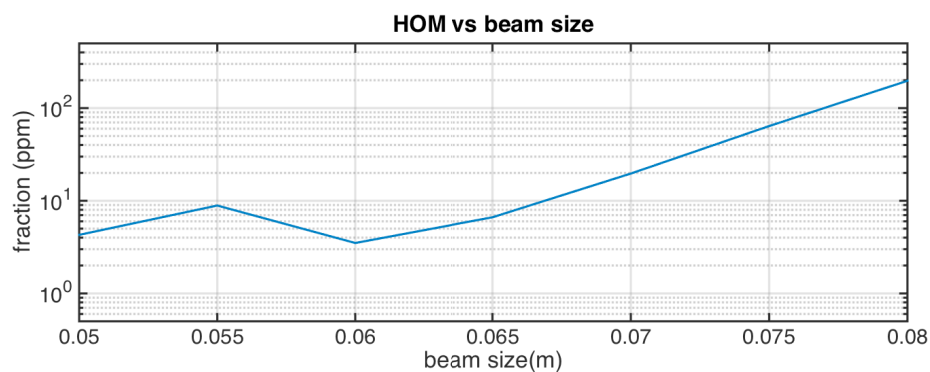
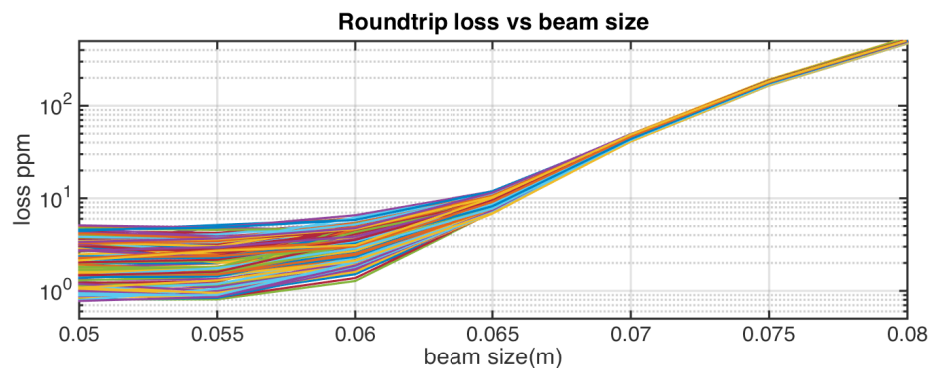


# For the future ... Polishing, not bad

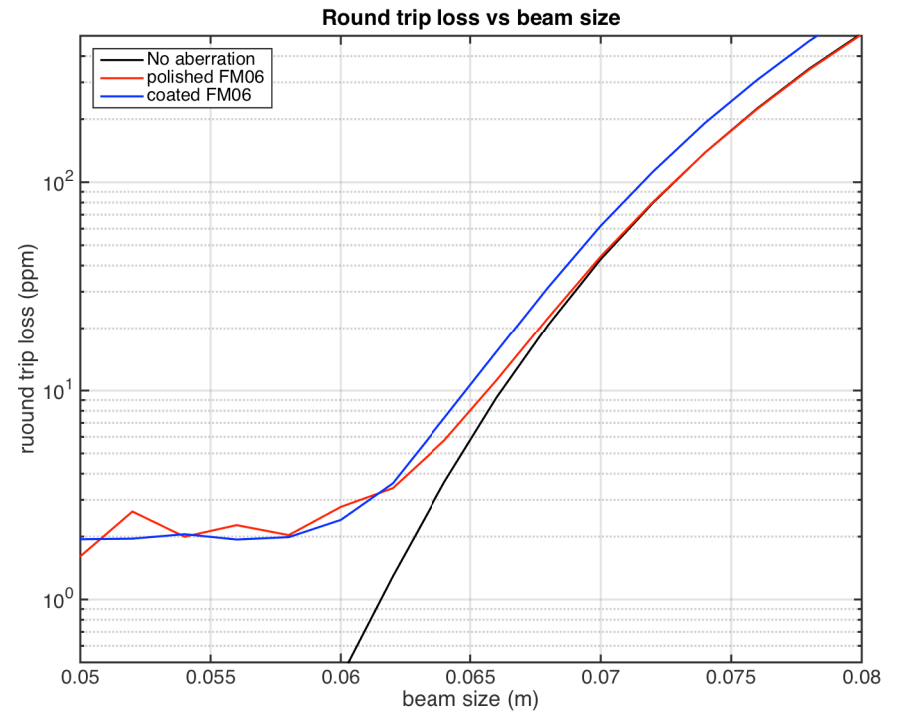
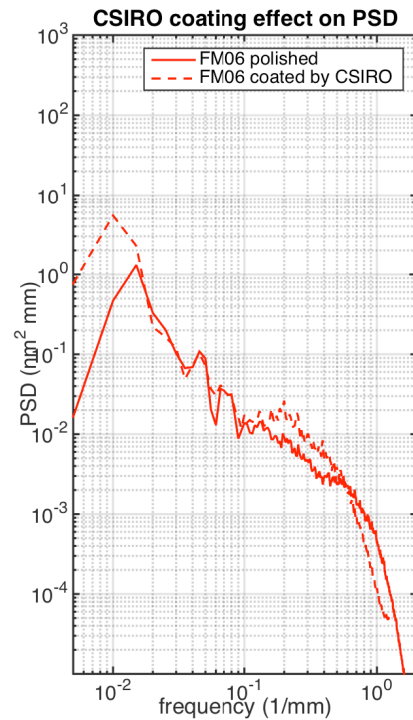
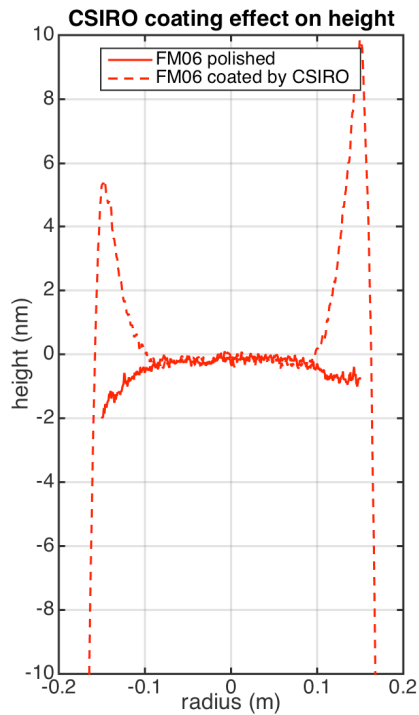
## aLIGO ITM/ETM Polished map PSD



## Round trip loss and HOM in a symmetric FP cavity



# Coating uniformity some improvement wanted

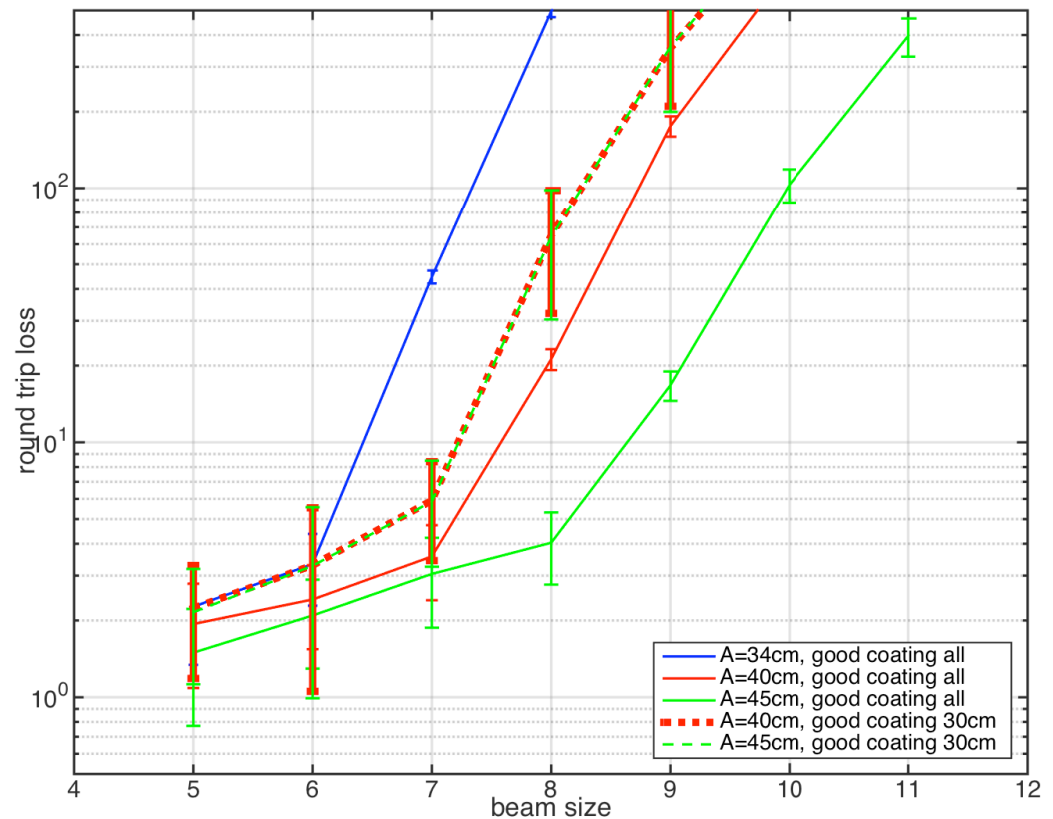




# Coating limits

## larger beam size configuration

- Larger optics can accommodate larger beam size
- Polishing is good enough for that (solid lines)
- Polishing uniformity can limit that (two dashed lines)



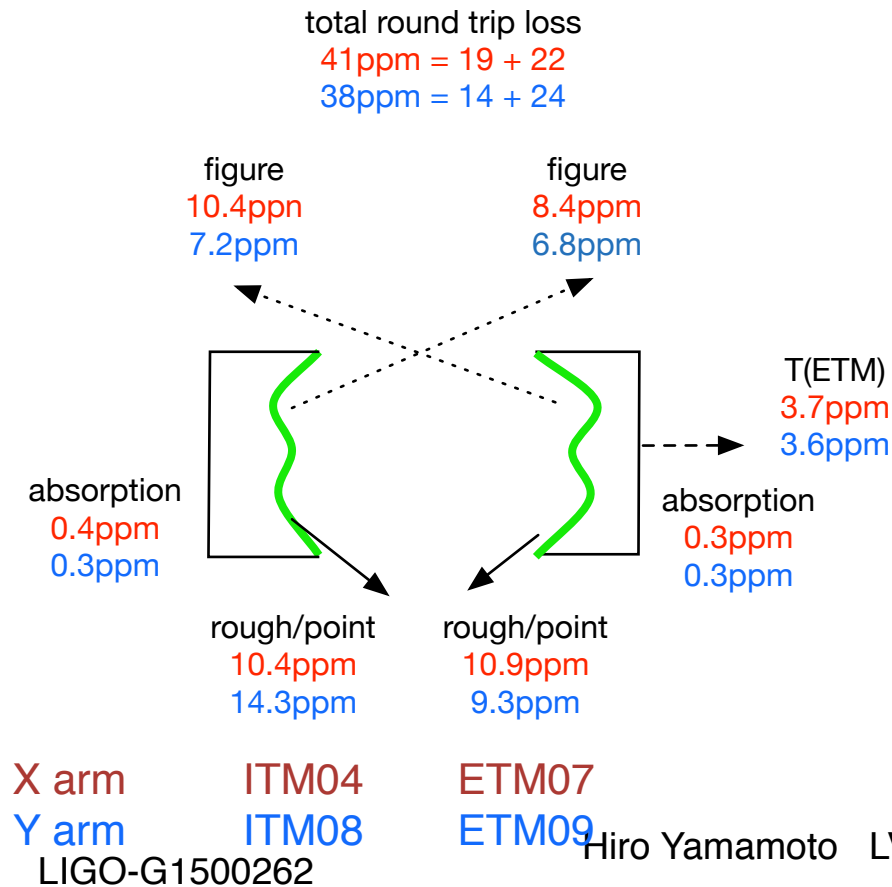




**LIGO**

# Missing loss of 40ppm needs to be well understood to discuss future IFO loss

## Phasemap and Caltech/LMA scattering loss measurements



- alog13414 ETMY scattering
  - » Total : 36ppm
  - » Point scattering : 18ppm
- alog13769 Best round trip loss 85ppm
  - » Extra 30-40ppm, where???
- COC data + Model
  - » Round trip loss error < 14ppm
  - » Integrated scattering
    - 7.5ppm by LMA
    - 9.3ppm by Caltech
  - » Zygo rms  $\Rightarrow$  loss(<1mm) < 1ppm
  - » PSD  $\Rightarrow$  loss(<5mm) < 1ppm