

LHO Test Mass Power Scattering Calculations

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1 ITM_x

Using the layout of the corner station [3], the center of the WA-1C flange (the Pcal camera used to take the images is located at VP2 in global coordinates is (37661, 0, 0) mm. The coordinates of ITM_x are (5013, -200, -80) mm [4]. The D7100 was attached to a Celestron telescope. The telescope had a 6 inch aperture mask installed which was centered on the telescope, yielding an effective viewing area of 13340 mm² (aperture area minus the area of the secondary mirror, which has a 69mm diameter) [2]. VP2 is 30 inches (762 mm) from the centerline at an angle of 90 degrees from the vertical [5]. This places the telescope observing surface at (37661, 0, 762) mm, so the distance from ITM_x is (32648, 200, 842) mm or 32659 mm. Dividing the observing area by the surface area of a sphere:

$$SA = 4\pi R^2,$$

results in a good approximation of the solid angled subtended by the camera. The radius is the distance between the test mass and camera:

$$13440\text{mm}^2 / (1.34 * 10^{10}\text{mm}^2) = 1.00 * 10^{-6}\text{steradians}.$$

See aLog35327[1] for details on the images. The best estimate for the ITM_x scattering power is 1.42*10⁸ watts [7], so ITM_x scatters approximately .0142 watts/steradian at an angle of 1.52°. Similar measurements could be used to find the distance from ITM_y to its PCal camera.

2 ETM_x

The ETM_x global coordinates are (3999498, -200, -80), and its local coordinates are (-502, -200, -80) [4], using the center of BSC9 as the origin for the local coordinates [9]. The Pcal camera is located at the WA-1E flange in the VP6 viewport. The WA-1E flange is located at (-5652, 0, 0) mm [9]. The camera is therefore at the (-5652, 566, 509) mm because the viewport is not directly along the centerline [6]. The distance from ETM_x to the camera is (-5150, 766, 589) mm, or 5240 mm. The D7100 camera is attached to a VR Nikkor 55-300 zoom lens, which was set to a focal length of 240mm, with an f-stop of f/13.

The f-stop is the focal length divided by the diameter of the aperture, so the aperture diameter is 18.46mm, yielding a viewing area of 268 mm². Dividing this area by the surface area of a sphere results in a good approximation of the solid angled subtended by the camera. The radius is the distance between the test mass and camera:

$$267.7\text{mm}^2 / (3.45 * 10^8 \text{mm}^2) = 7.76 * 10^{-7} \text{steradians}.$$

Photos were taken on August 1st, 2017 at around 14:00:00 local time, with the interferometer locked. Power in the X-arm was stable at the time. The best estimate for the ETMx scattering power is 8.42*10⁶ watts [7] (from extending the dynamic range), so ETMx scatters approximately 10.84 watts/steradian at an angle of 10.6°. Compare results with T1600085, which used photodiodes [8].

3 Data Table

Test Mass	TM Coor (mm)	Camera Coor (mm)	Camera/TM Distance (mm)	Angle (degrees)
IMTx	(5013, -200, -80)	(32648, 200, 842)	32655	1.52
ETMx	(-502, -200, -80)	(-5652, 566, 509)	5240	10.6

Test Mass	Effective Aperture Area (mm ²)	Measured Power (W)	Radiance (W/sr)
IMTx	13340	1.42*10 ⁸	10.84
ETMx	268	8.42*10 ⁶	.0142

References

- [1] *aLog35327*. URL: <https://alog.ligo-wa.caltech.edu/aLOG/index.php?callRep=35327>.
- [2] *Celestron EdgeHD8 Telescope*. URL: <https://www.celestron.com/products/edgehd-8-optical-tube-assembly-cg5>.
- [3] *Corner Station Vacuum Drawings*. URL: https://lhocds.ligo-wa.caltech.edu/vac/vac_drawings/Washington/LVEA/Arrangement/5001s1.PDF.
- [4] *DCC: D0901920*. URL: <https://dcc.ligo.org/D0901920>.
- [5] *DCC: D980228*. URL: <https://dcc.ligo.org/D980228>.
- [6] *DCC: T1000746*. URL: <https://dcc.ligo.org/T1000746>.
- [7] Christian Pluchar. *Measuring Scattering off LHO Test Masses*. URL: <https://dcc.ligo.org/G1701180-v1>.
- [8] Vincent Roma. *Optical Lever and Baffle Diode Information*. URL: <https://dcc.ligo.org/LIGO-T1600085>.

- [9] *XEnd Vacuum Drawings*. URL: https://lhocds.ligo-wa.caltech.edu/vac/vac_drawings/Washington/XEND/5005.pdf.