

# An Issue with PE Results Using Bilby and TD Approximants

(And Resolution)

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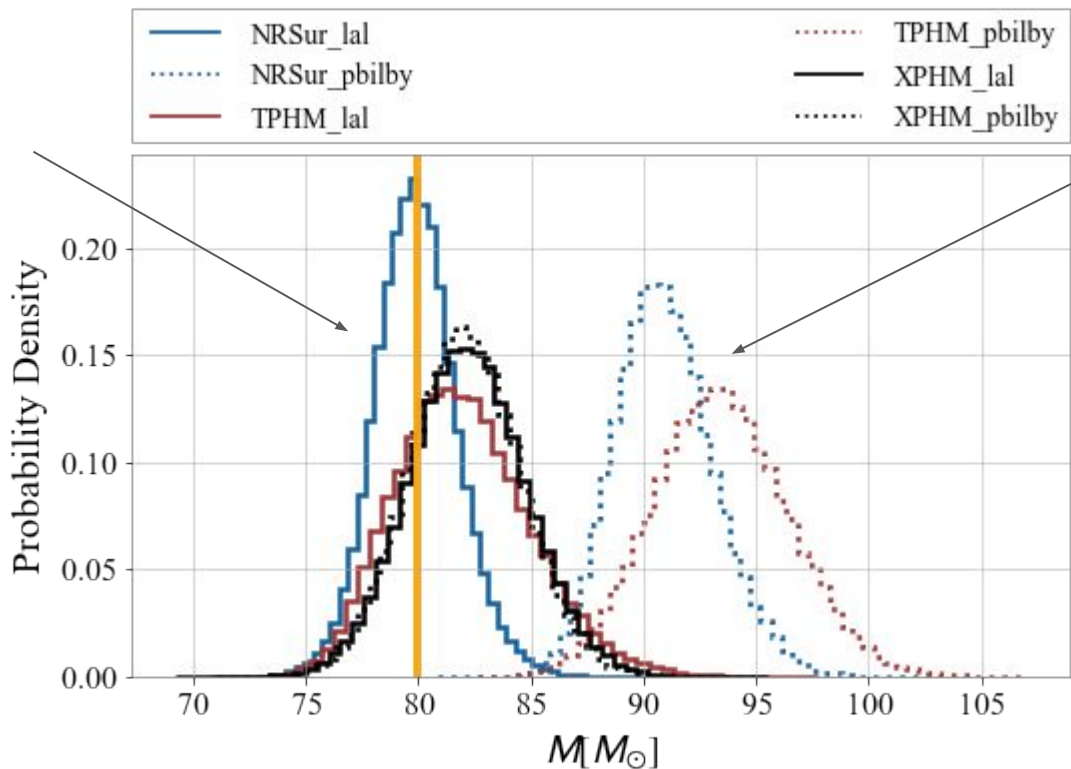
# Setup

Our study involved performing parameter estimation on a set of NR injection files. We,

- Used PyCBC to generate NR injection gwfs for H1, L1, V1 in zero-noise
- Used LALInference MCMC and pBilby for the inference. Use the same settings where possible
- Used  $f_{\text{low}} = 20\text{Hz}$  and  $f_{\text{final}} = 896\text{Hz}$  to remain consistent with GWTC-3
- Recovered with IMRPhenomXPHM, IMRPhenomTPHM and NRSur7dq4 using only  $l < 4$  multipoles

# Zero-noise NR injection

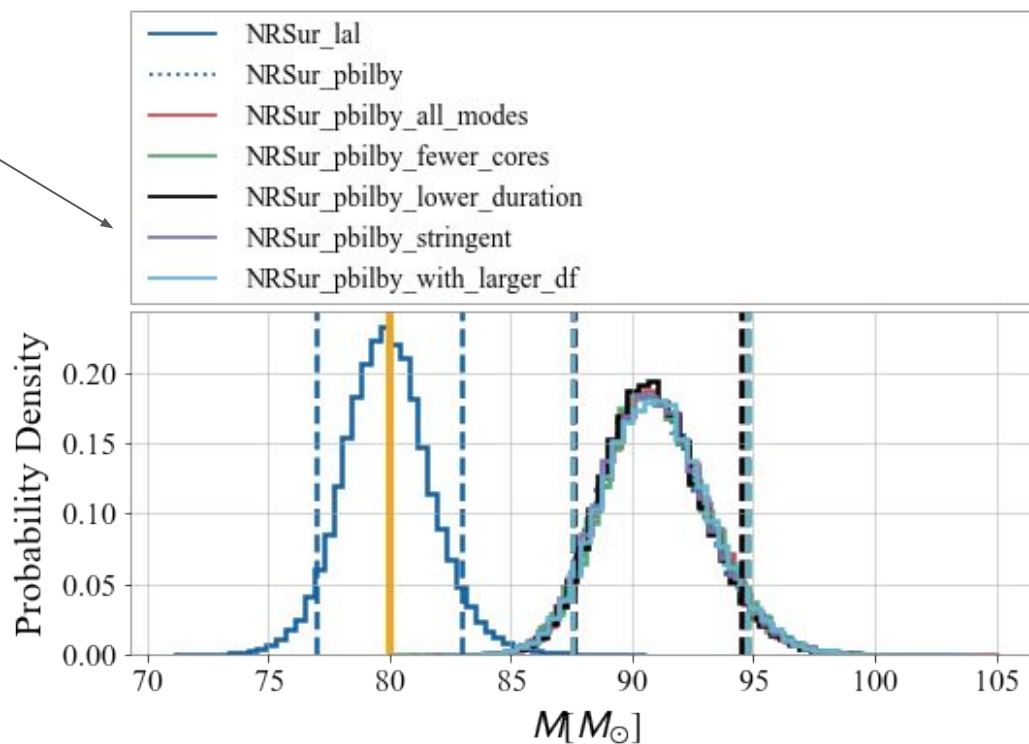
Excellent agreement between pBilby and LALInference for FD models (IMRPhenomXPHM). This is expected from the pBilby review: see e.g. [this page](#)



See bias in the total mass from pBilby with TD models. Only LALInference recovers the injected parameters

# Tested various settings, all gave similar posteriors

Increased number of live points from 1500 to 2000, increased nact from 20 to 50, increased maxmcmc from 5000 to 20000. Not a convergence issue.

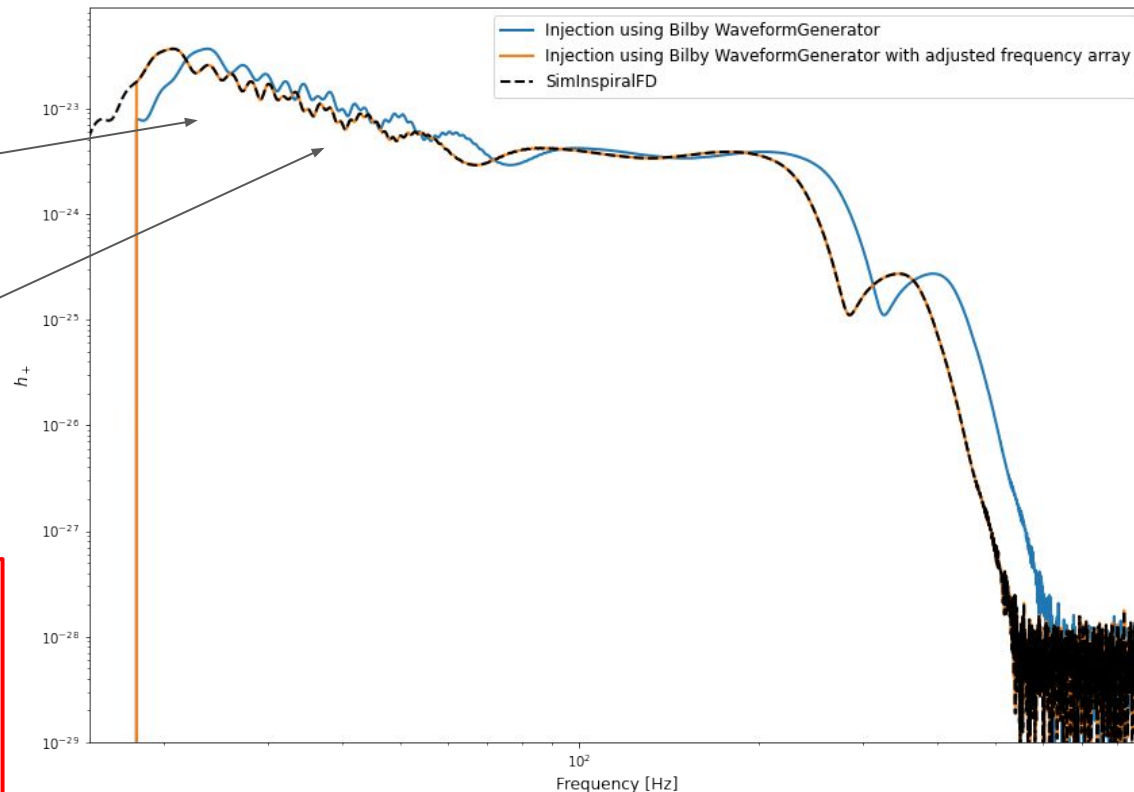


# Compare waveforms generated with Bilby and LALSimInspiraldFD

When plotting NR injection, we see a difference between Bilby and LALSimInspiraldFD

By adjusting the frequency array to account for change in  $\Delta f$ , Bilby and LALSimInspiraldFD agree

Issue resolved if  $f_{\text{max}} = \text{sampling\_frequency} / 2$  or if frequency array adjusted for change in  $\Delta f$  from SimInspiraldFD



# Issue explained

```
108 def create_frequency_series(sampling_frequency, duration):
109     """ Create a frequency series with the correct length and spacing.
110
111     Parameters
112     =====
113     sampling_frequency: float
114     duration: float
115
116     Returns
117     =====
118     array_like: frequency series
119
120     """
121     _check_legal_sampling_frequency_and_duration(sampling_frequency, duration)
122     number_of_samples = int(np.round(duration * sampling_frequency))
123     number_of_frequencies = int(np.round(number_of_samples / 2) + 1)
124
125     return np.linspace(start=0,
126                       stop=sampling_frequency / 2,
127                       num=number_of_frequencies)
```

Bilby assigns a frequency array according to sampling frequency and duration. This means that  $\Delta f = 0.125\text{Hz}$  for our setup

```
362 if lalsim.SimInspiralImplementedFDApproximants(approximant):
363     wf_func = lalsim_SimInspiralChooseFDWaveform
364 else:
365     wf_func = lalsim_SimInspiralFD
366
367 try:
368     hplus, hcross = wf_func(
369         mass_1, mass_2, spin_1x, spin_1y, spin_1z, spin_2x, spin_2y,
370         spin_2z, luminosity_distance, iota, phase,
371         longitude_ascending_nodes, eccentricity, mean_per_ano, delta_frequency,
372         start_frequency, maximum_frequency, reference_frequency,
373         waveform_dictionary, approximant)
```

Issue resolved if  $f_{\text{max}} = \text{sampling\_frequency} / 2$   
or if frequency array adjusted for change in  $\Delta f$  from SimInspiralFD

Bilby passes  $\Delta f = 0.125\text{Hz}$ ,  $\text{start\_frequency} = 20\text{Hz}$ ,  $\text{maximum\_frequency} = 896\text{Hz}$ , and LALSimInspiralFD outputs strain sampled at a *different*  $\Delta f = 0.109375\text{Hz}$ . Bilby does not correct for this change in  $\Delta f$

# Issue explained

```
laldict_eob = lal.CreateDict()
```

```
q=1./0.28  
Mtotal=38.4
```

```
m1 = q * Mtotal / (1.+q)  
m2 = Mtotal / (1. + q)
```

```
distance=740*1e6*lal.PC_SI
```

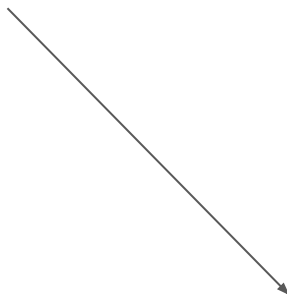
```
siminspiralfd_eob_params = {  
    'm1':m1*lal.MSUN_SI,  
    'm2':m2*lal.MSUN_SI,  
    'S1x':0.1,'S1y':0.1,'S1z':0.1,  
    'S2x':0.,'S2y':0.,'S2z':0.,  
    'distance':distance,'inclination':0.,'longAscNodes':0.,  
    'eccentricity':0.,'meanPerAno':0.,'deltaF':0.125,  
    'f_min':10.,'f_ref':20.,'phiRef':0.,  
    'LALparams':laldict_eob,'approximant':ls.SEOBNRv4P  
}
```

```
hp_eob_fmax896, _ = ls.SimInspiralFD(f_max=896.,**siminspiralfd_eob_params)  
hp_eob_fmax1024, _ = ls.SimInspiralFD(f_max=1024.,**siminspiralfd_eob_params)
```

```
print (hp_eob_fmax896.deltaF)  
print (hp_eob_fmax1024.deltaF)
```

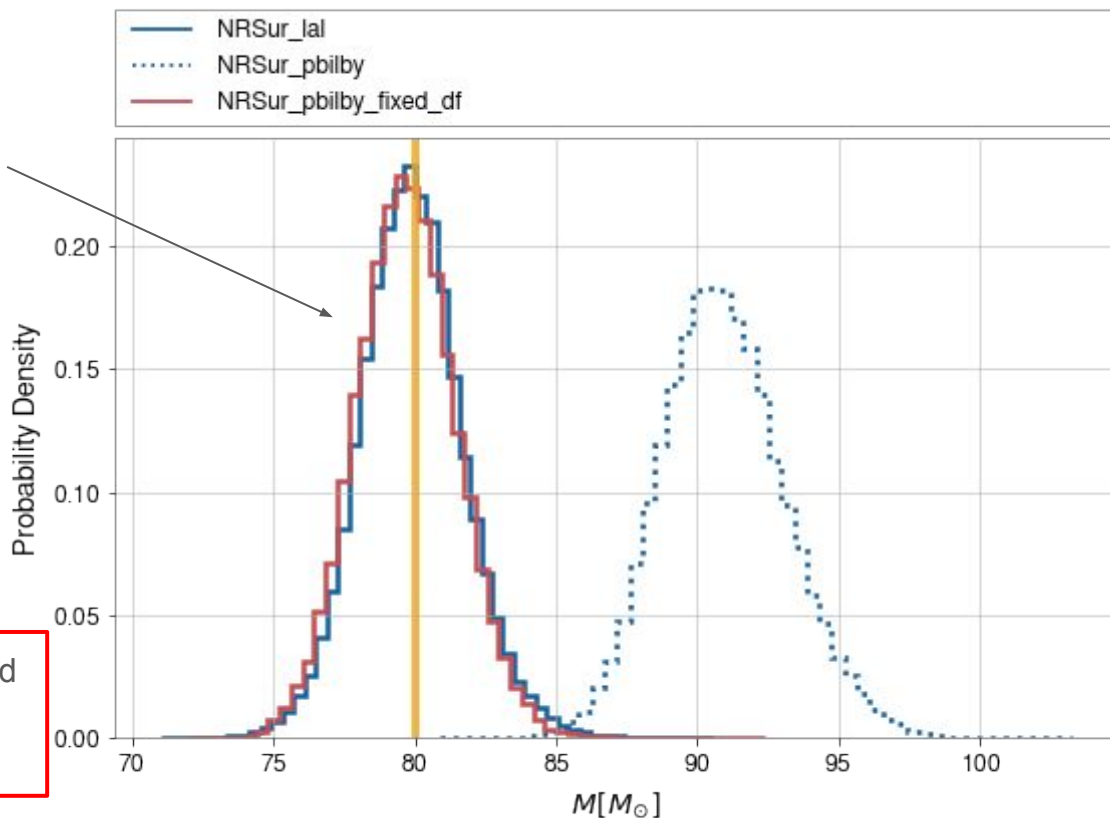
In this example:

hp\_eob\_fmax896.deltaF=0.109375Hz  
hp\_eob\_fmax1024.deltaF=0.125Hz



# Rerun with consistent Bilby and LALSimInspiraldFD

We now see excellent agreement between LALInference and pBilby for the NRSur7dq4 case. We would expect to see the same level of improvement for all TD models



Our “quick” fix is not optimised and should not be used as a solution to the problem.



# Summary

- We see a difference in the inferred posteriors between LALInference and pBilby for TD models but we see excellent agreement for FD models.
- When  $f_{\text{final}}$  does not equal  $\text{sampling\_frequency} / 2$  there is a potential discrepancy between the  $\text{delta\_f}$  used in LALSIMInspiralFD and the  $\text{delta\_f}$  used in the Bilby frequency array.
- Correcting for the change in  $\text{delta\_f}$  produces excellent agreement between LALInference and pBilby for TD models.
- Does not affect FD models because ChooseFDWaveform outputs the data at the given input  $\text{delta\_f}$ .
- Could be an issue for some O3 results if Bilby ran TD approximants. Could also be an issue in O4 for TD models if frequency spacing isn't made consistent.