

LIGO-T2300145

sga46@cornell.edu

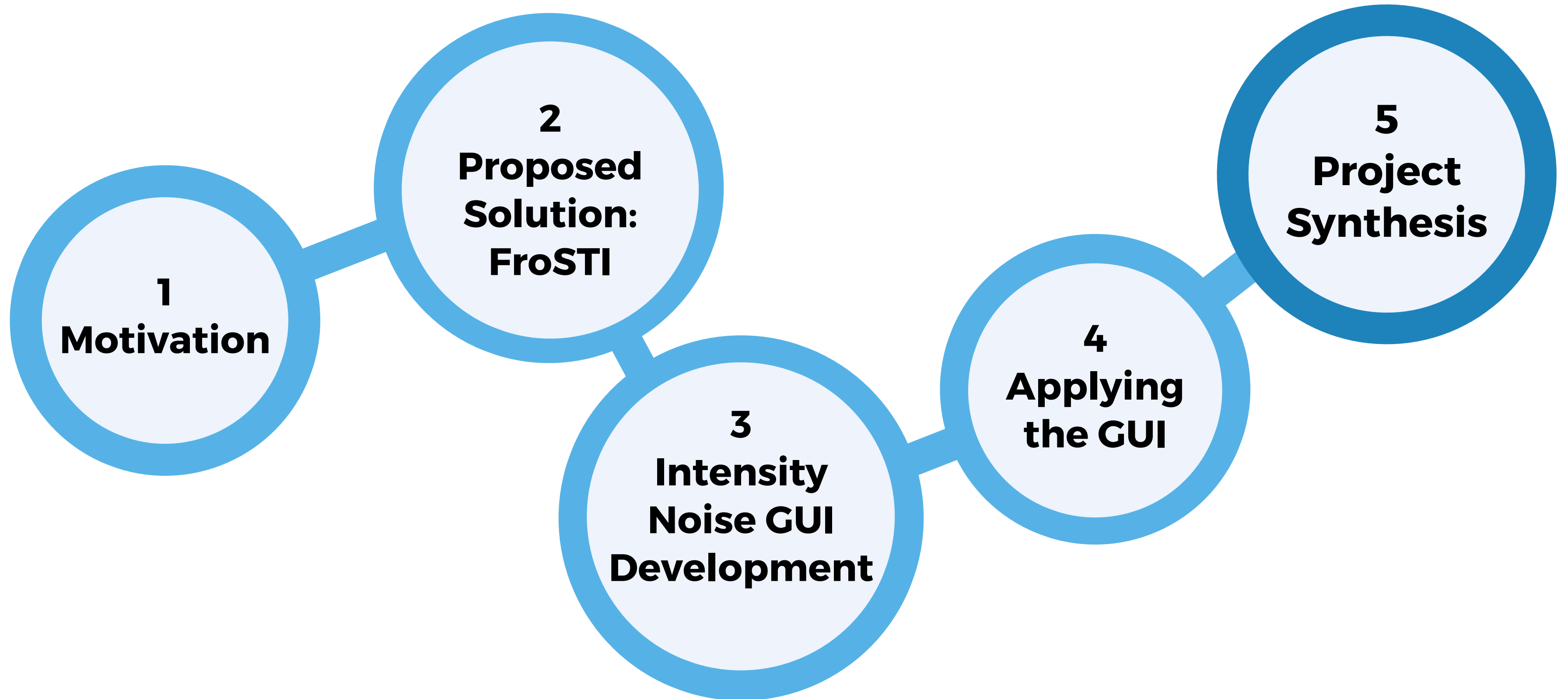
LIGO SURF

NOISE ANALYSIS FOR THE FROSTI ADAPTIVE OPTIC

Sophia Arnold, Cornell University

Mentors: Jonathan Richardson and Tyler Rosauer, UC Riverside

Presentation Outline



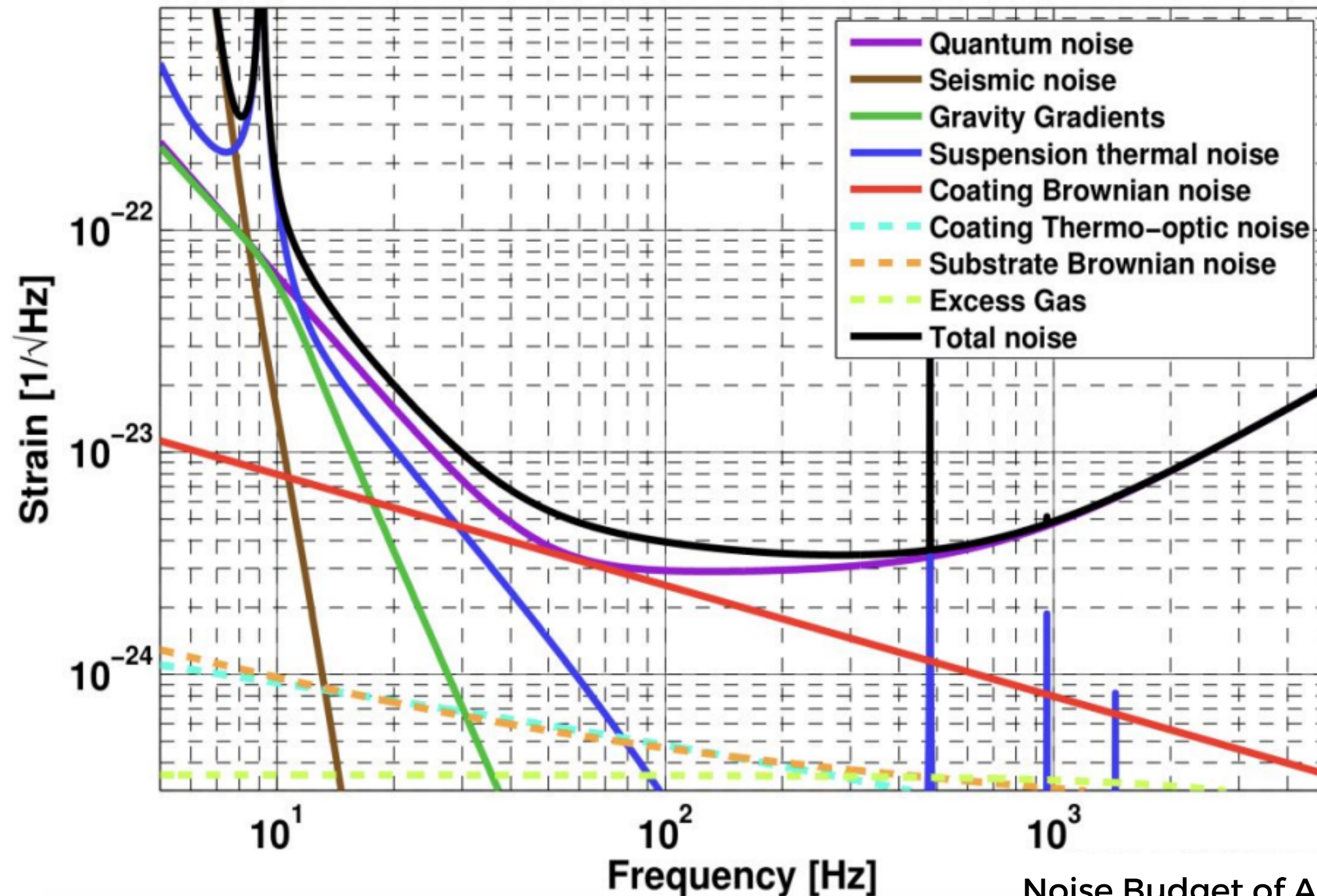
1) MOTIVATION FUTURE IMPROVEMENTS TO LIGO

Motivation

Higher laser power

Answer

AdvLIGO Noise Curve: $P_{in} = 125.0 \text{ W}$



Notice:

At **frequencies** higher than **100Hz**, **quantum noise** **dominates** the **total noise**!

Lowering the **photon shot noise** will lower **quantum noise**.

The amplitude of the spectral density of **shot noise** decreases with $\frac{1}{\sqrt{N}}$ where N = number of photons.

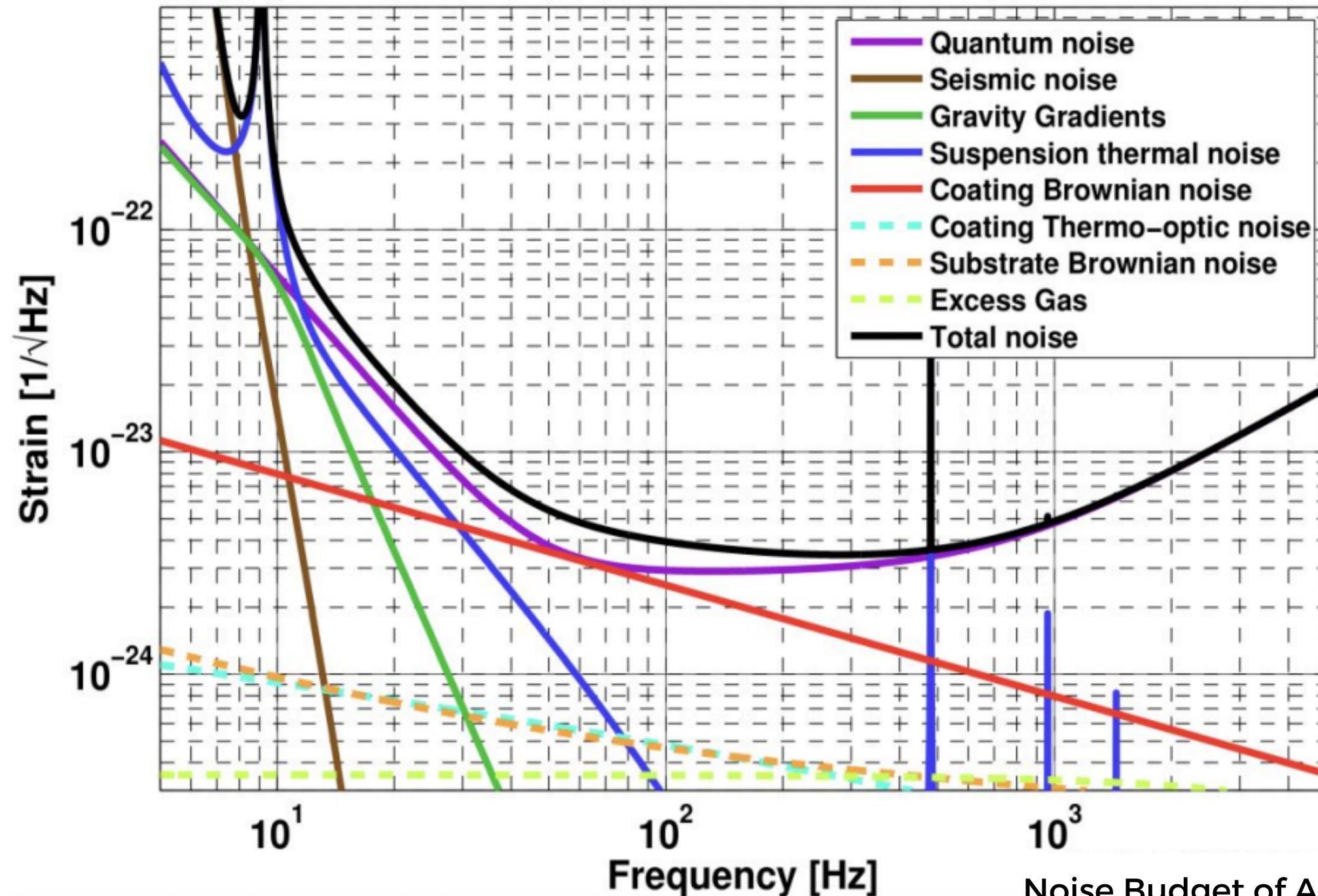
Noise Budget of AdvLIGO
(Hild 2017, G1200598)

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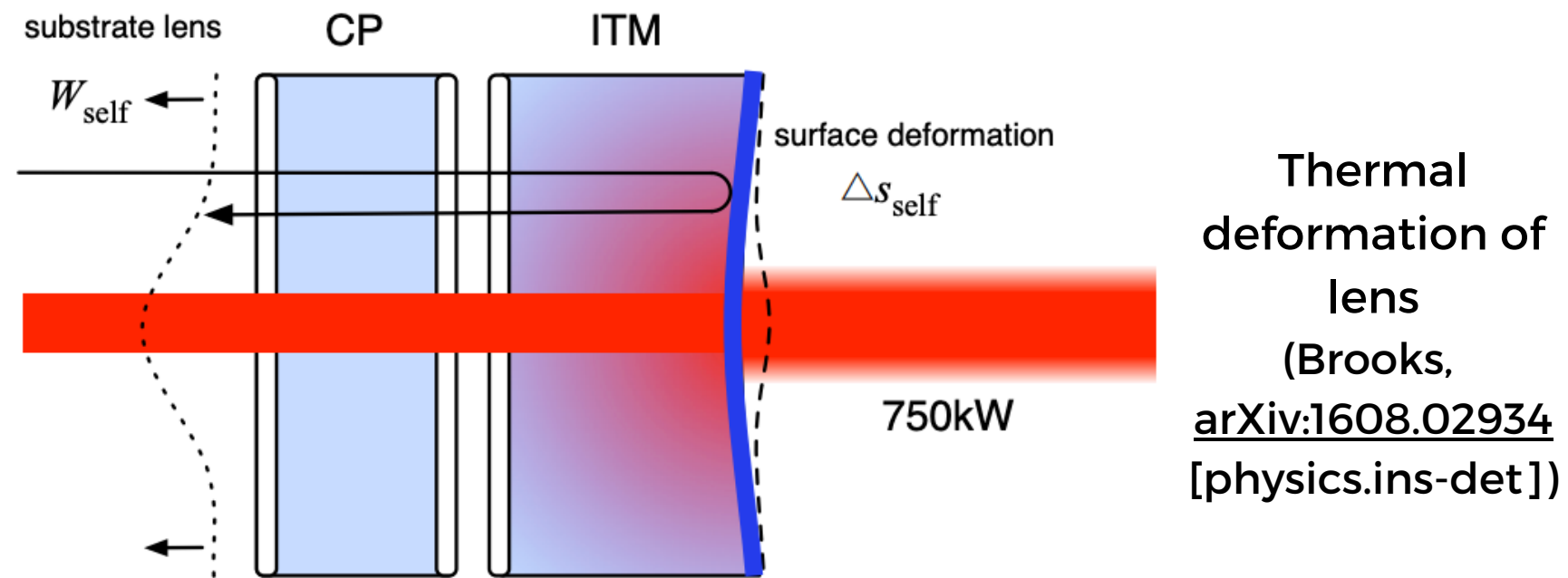
Lowering the **photon shot noise** will lower **quantum noise**.

The amplitude of the spectral density of **shot noise** decreases with $\frac{1}{\sqrt{N}}$ where N = number of photons.

Solution: Higher laser power!

Motivation

Higher laser power and the associated costs

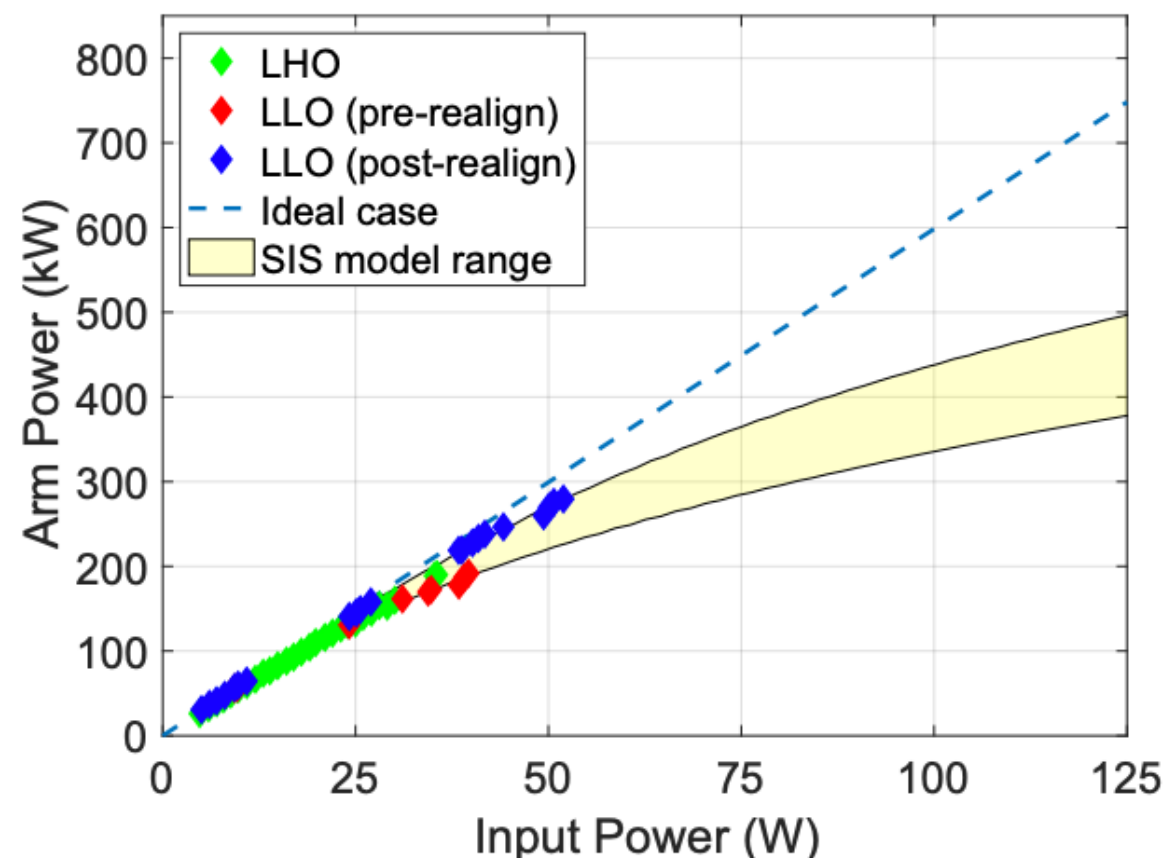


The **Thermal Compensation System (TCS)** is not equipped for higher laser power.

Worse effects from **uniform absorption**. **TCS augments** the problem.

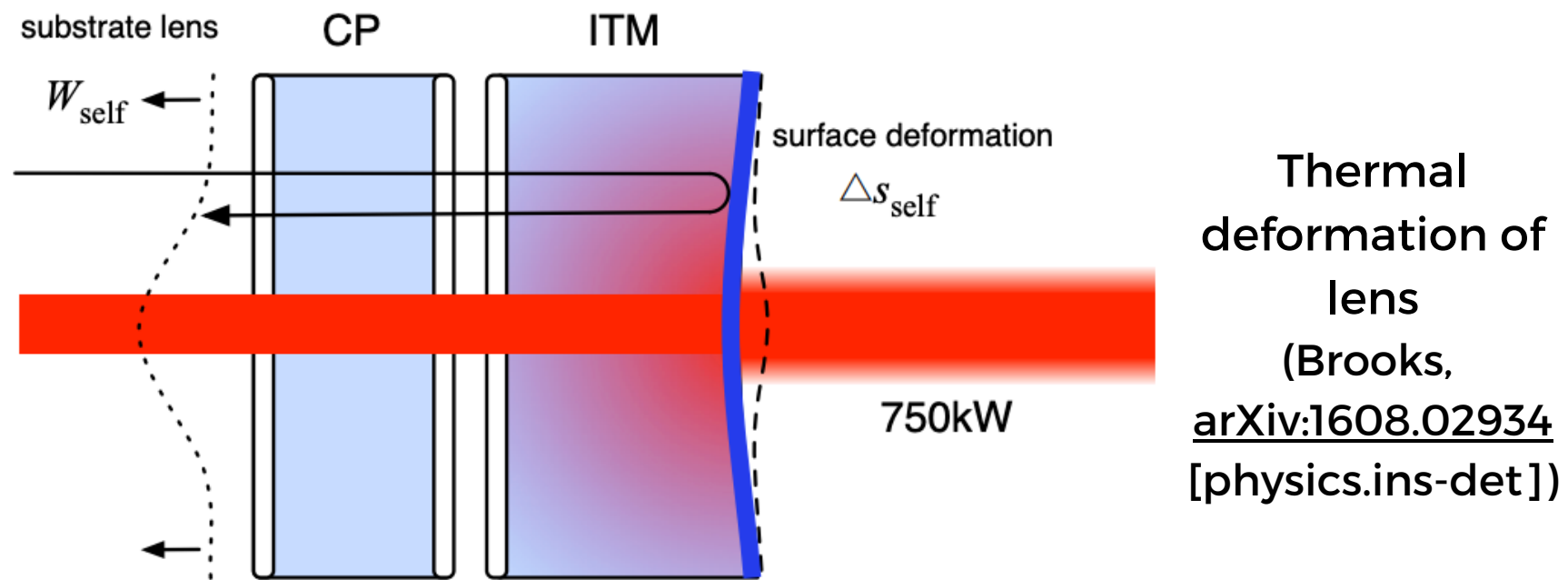
Larger effects from point absorbers. **TCS is still not able to compensate.**

aLIGO ideal vs. actual arm power vs. input power circa O3 (Brooks et al., P1900287)



Motivation

Higher laser power and the associated costs



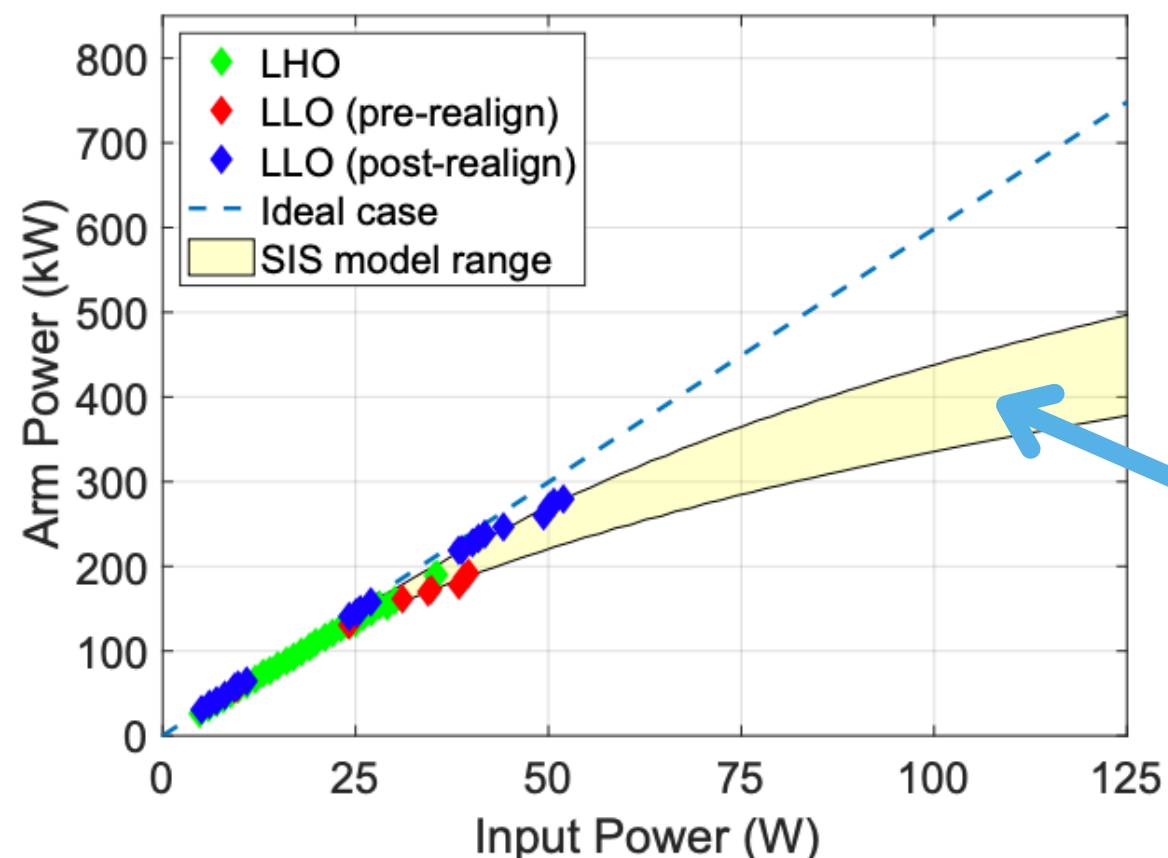
The **Thermal Compensation System (TCS)** is not equipped for higher laser power.

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Larger effects from point absorbers. **TCS is still not able to compensate.**

Predicted losses due to point absorbers

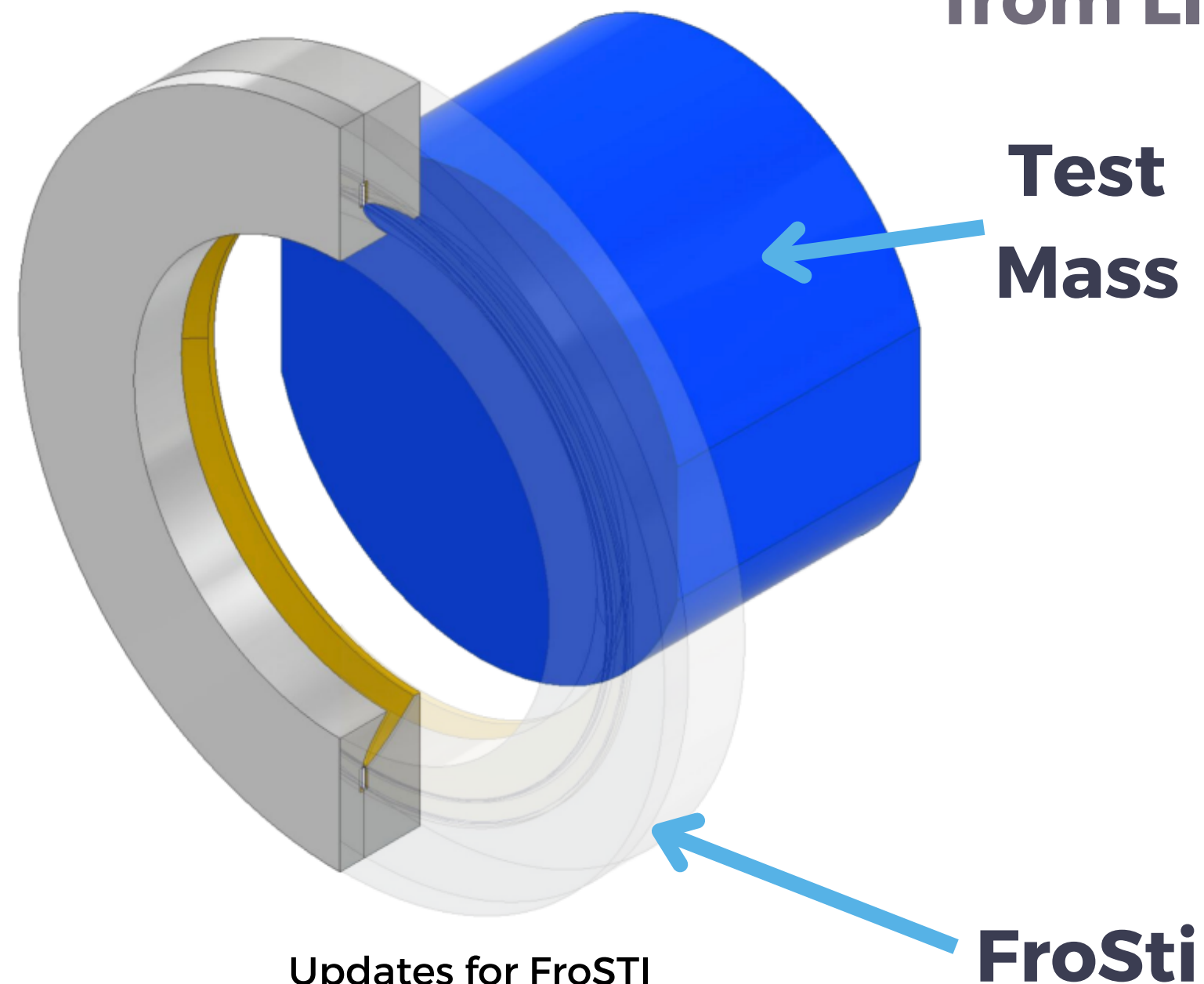
aLIGO ideal vs. actual arm power vs. input power circa O3 (Brooks et al., P1900287)



**2) PROPOSED
SOLUTION: FROSTI
ELIMINATING TEST MASS
LOSSES**

Front Surface Type Irradiator (FroSTI) Richardson lab

A next generation, annular ring heater, designed to combat power losses from LIGO's test masses



Updates for FroSTI
(Richardson 2022, G2200399)

Purpose:

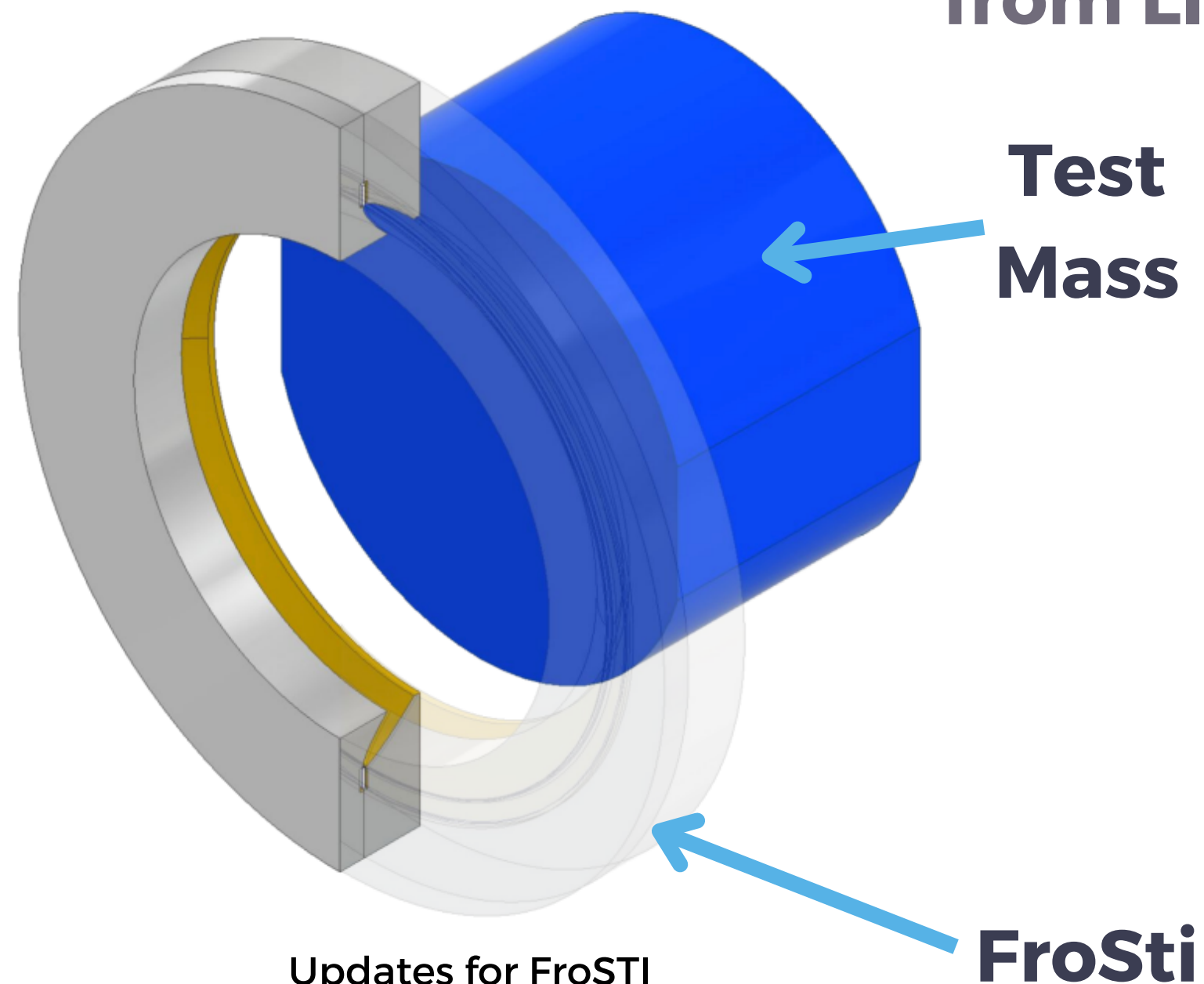
Correct problems posed by both **thermal deformity of test masses**, and **point absorbers** by:

Creating precise wavefront control technology that reduces power loss.

Front Surface Type Irradiator (FroSTI)

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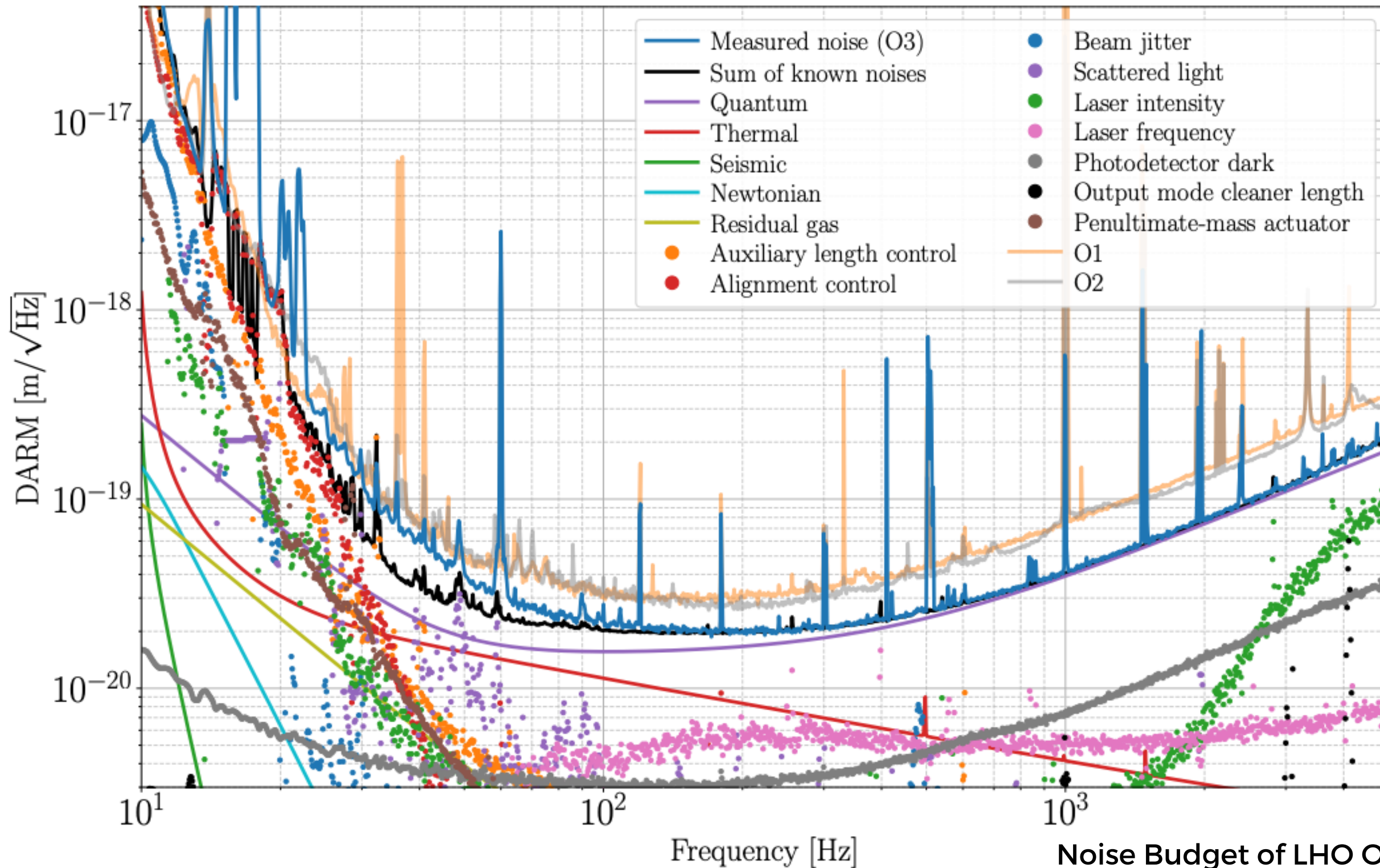
Correct problems posed by both **thermal deformity of test masses**, and **point absorbers** by:

Creating precise wavefront control technology that reduces power loss.

Still needs to be experimentally tested

Proposed Solution: FroSTI

Installing FroSTI in LIGO



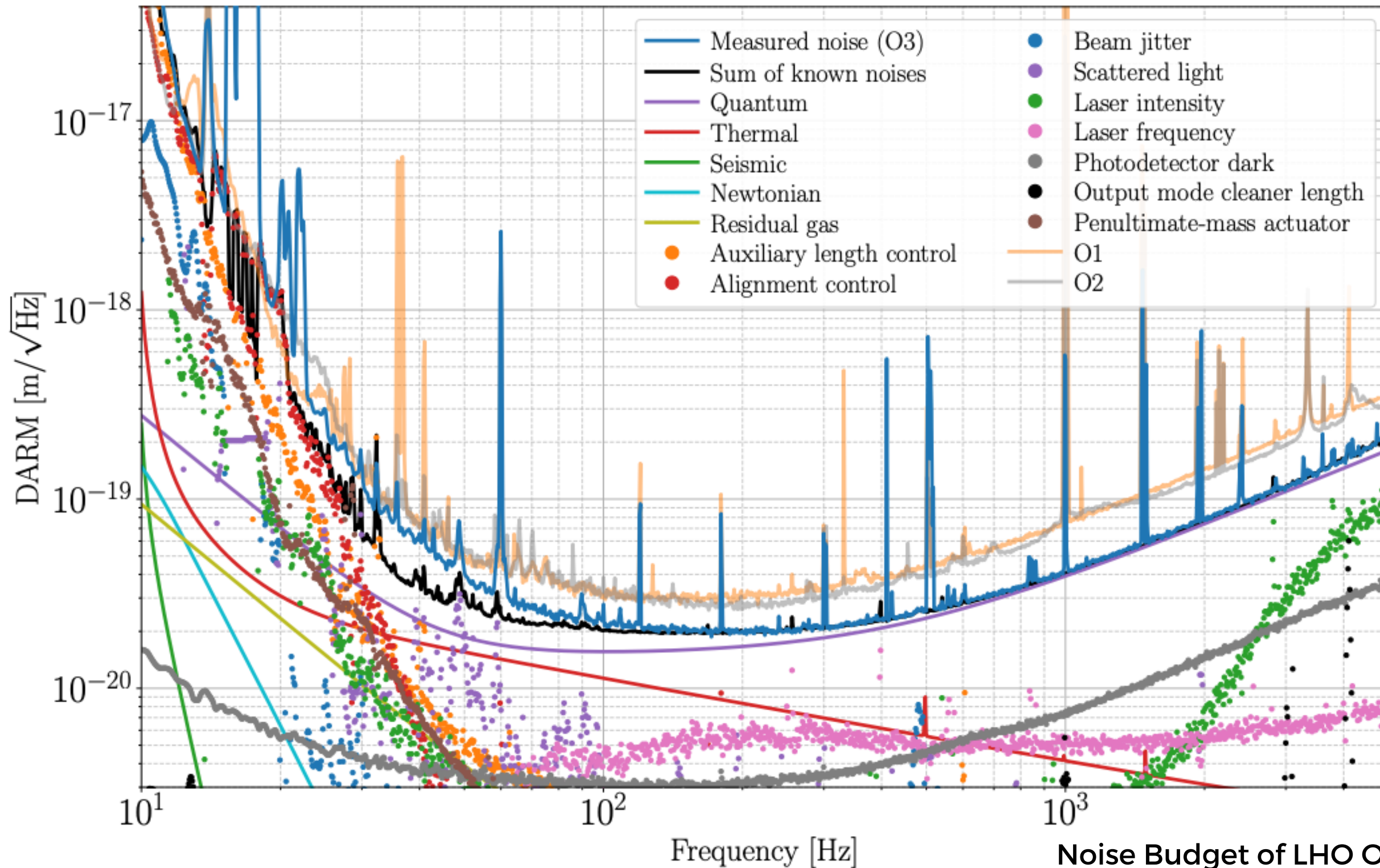
Noise Budget of LHO O3
(G. L. Mansell 2020, P2000122-v)

The Challenge

Noise in FroSTI's heating elements must be **100x less** than the quantum noise of a photodetector!

Proposed Solution: FroSTI

Installing FroSTI in LIGO



Noise Budget of LHO O3
(G. L. Mansell 2020, P2000122-v)

The Challenge

Noise in FroSTI's heating elements must be **100x less** than the quantum noise of a photodetector!

How can we measure noise on this scale?

Proposed Solution: FroSTI

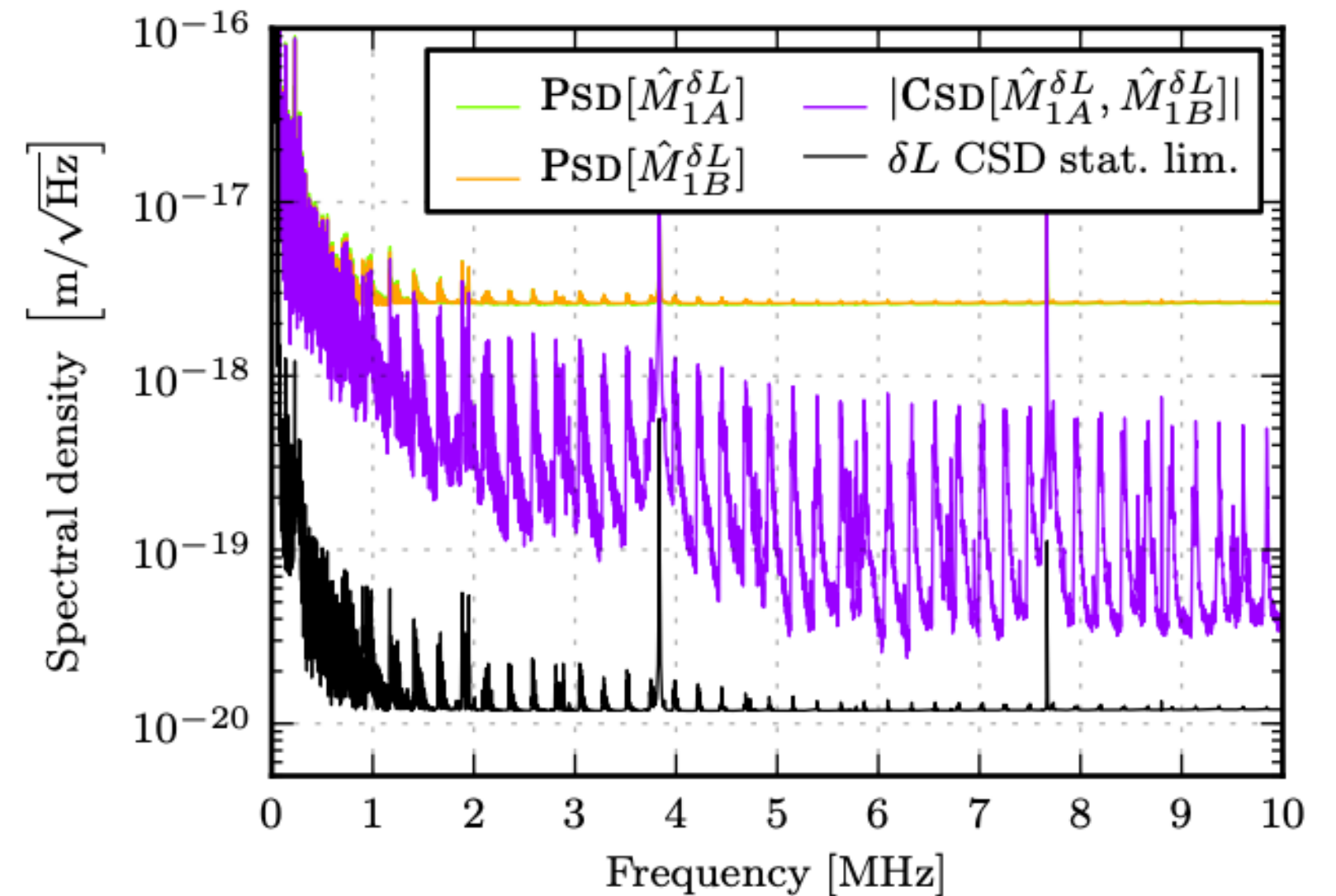
Installing FroSTI in LIGO

The Solution:

Use the **Power Spectral Density (PSD)** and **Cross Spectral Density (CSD)**.

Use the **rolling time average** of these values computed from a **continuous signal** to find noise **below LIGO's desired threshold**.

Fermilab Holometer Paper



Thermal noise of one interferometer. The Holometer: An Instrument to Probe Planckian Quantum Geometry (Chou: [arXiv:1611.08265](https://arxiv.org/abs/1611.08265) [physics.ins-det])

Proposed Solution: FroSTI

SURF Project Objectives

My Goals:

Create a program which will **dynamically** find the **intensity noise performance** of FroSTI's heating elements.

Plot both the **CSD amplitude and phase** for **real-time noise analysis** of the heating elements.

The Red Pitaya

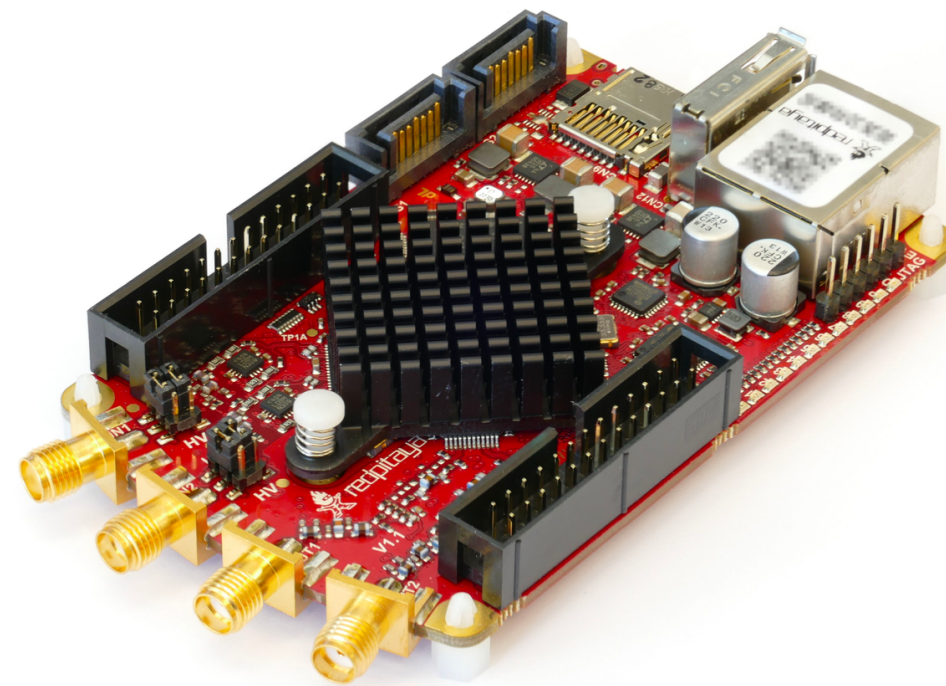
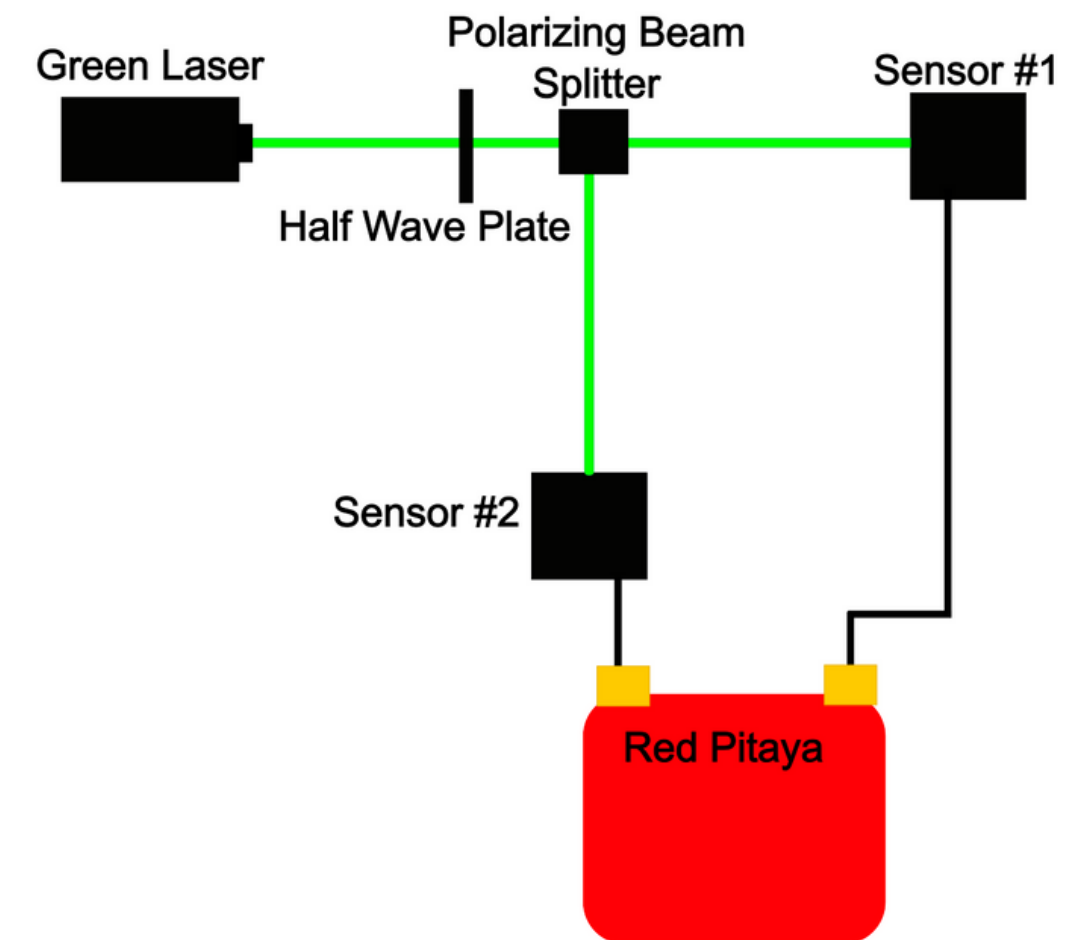


Image of a Red Pitaya
(Image from:
<https://redpitaya.com/product/stemlab-125-14/>)



Proposed Solution: FroSTI SURF Project Objectives

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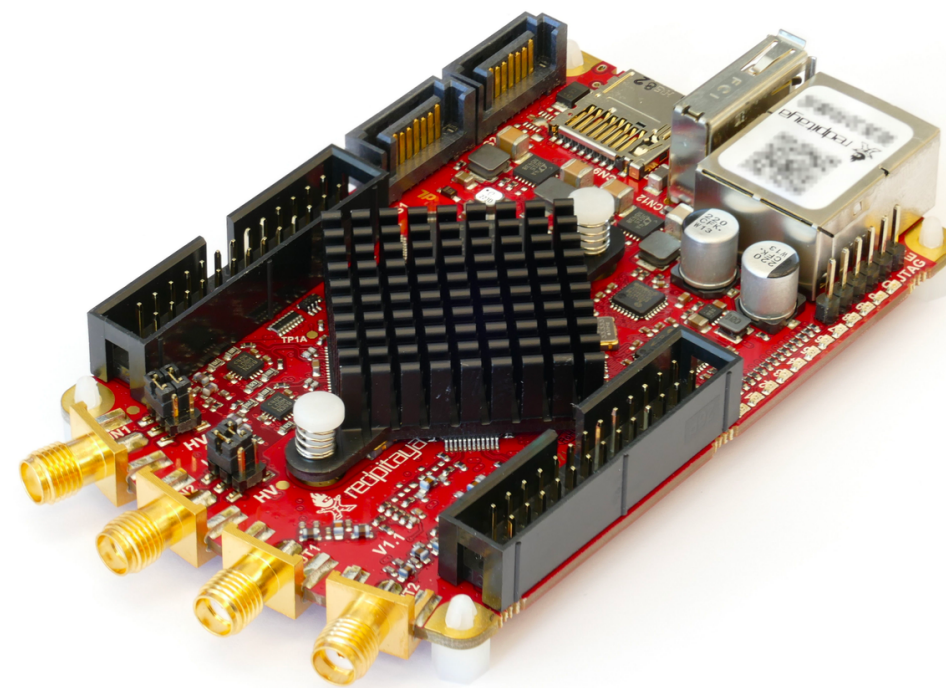
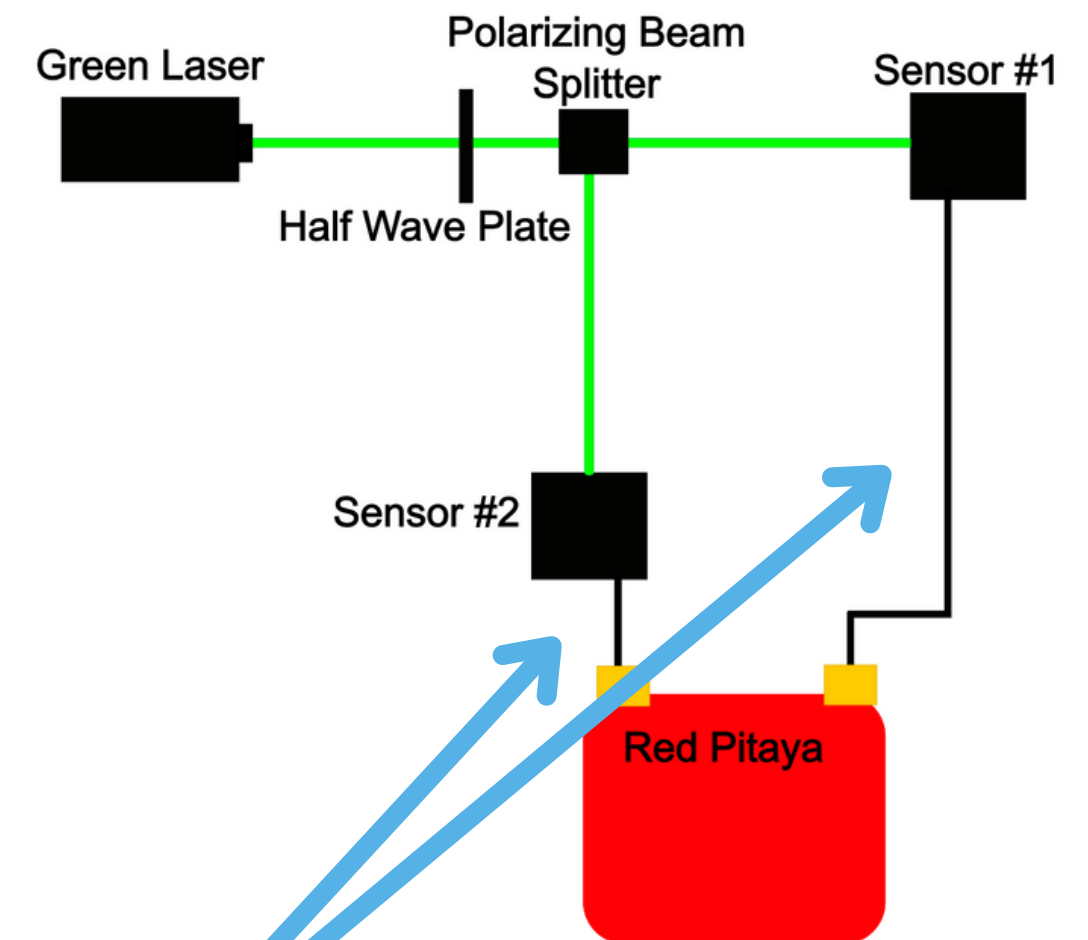


Image of a Red Pitaya
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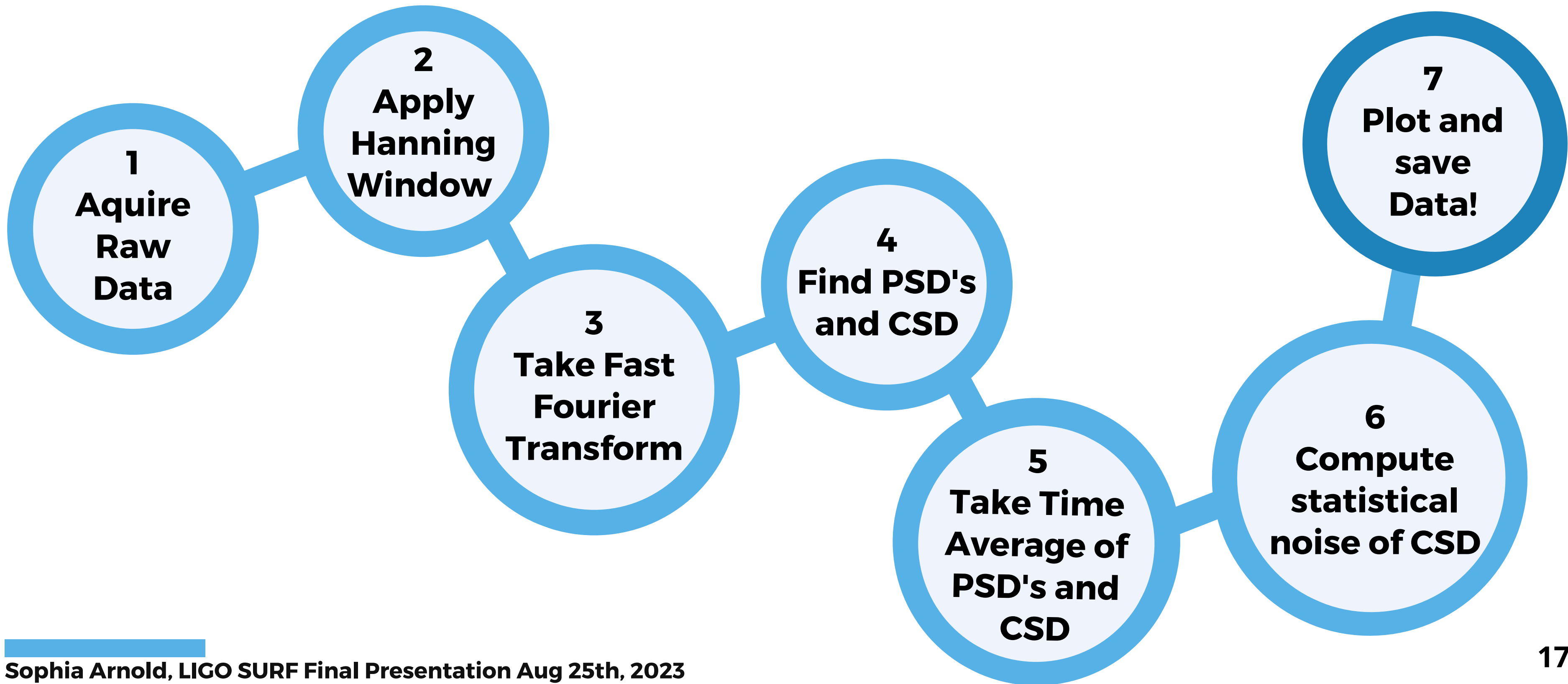


In our experiment, cables connecting sensors to Red Pitaya were the same length

**3) INTENSITY NOISE
GUI DEVELOPMENT
A WAY TO MEASURE
INTRINSIC ELECTRICAL
NOISE**

Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI



Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

1
Acquire
Raw
Data

To acquire the **raw data**, we needed to communicate with the **Red Pitaya**.

Communicating with the **Red Pitaya** was the **primary cause** of the **issues** I faced when developing this GUI.

7
Plot and
save
Data!

Transform

5
Take Time
Average of
PSD's and
CSD

6
Compute
statistical
noise of CSD

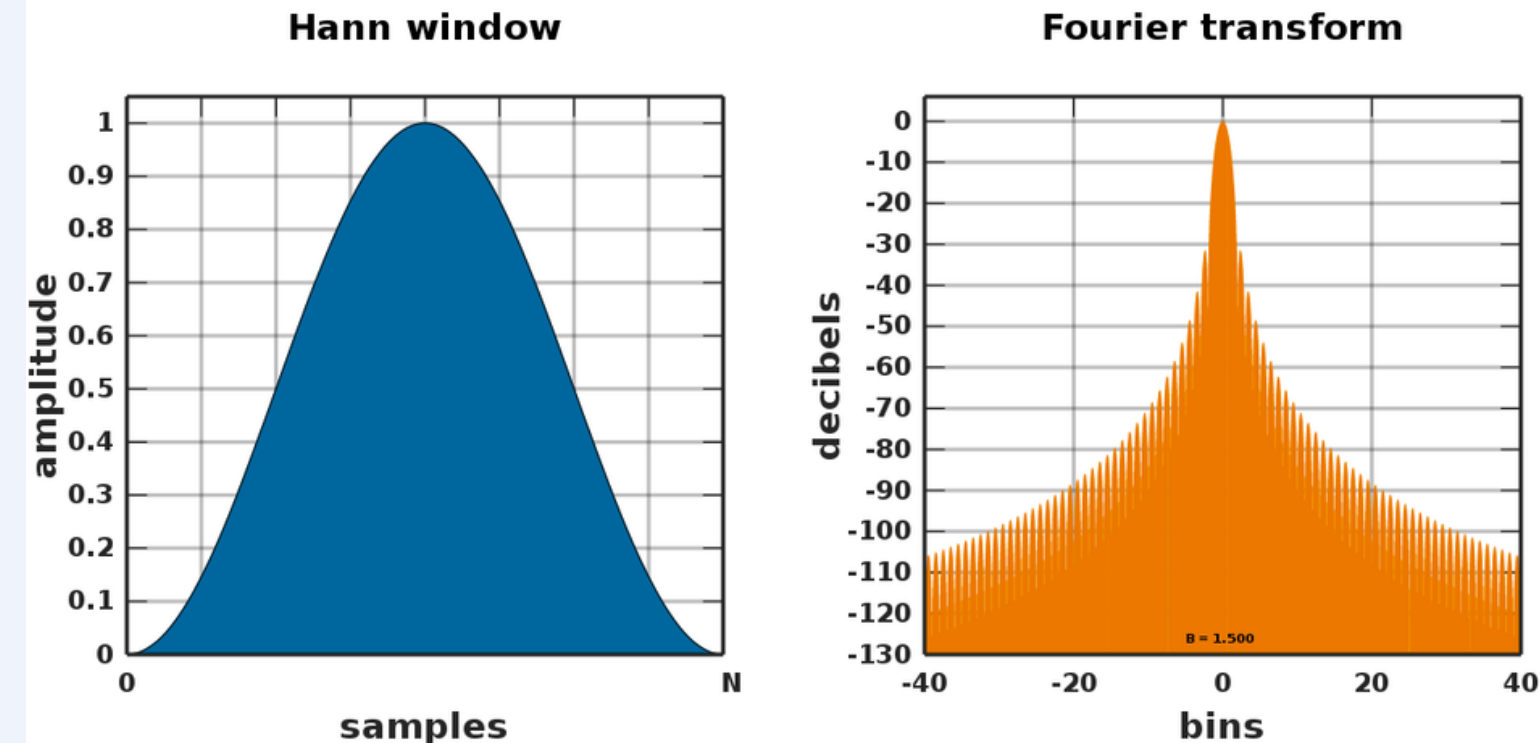
Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

1
Acquire
Raw
Data

2
Apply
Hanning
Window

3
Take Fast
Fourier
Transform



Hann Window in Time (left) and Frequency (right) domains
(image from: https://en.wikipedia.org/wiki/Hann_function)

The **Hann window** is a **filter** which is can be applied to samples **prior** to performing an **FFT** to **clean** the FFT process up, and **prevent spillage** of signals into **unwanted frequency bins**.

Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

1
Acquire
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Transform

$$X(k) = \sum_{n=0}^{N-1} x(n)e^{-j2\pi kn/N}$$

Equation for Fast Fourier Transform

(Image from: <https://speech.zone/forums/topic/explaining-dft-formula/>)

Fast Fourier Transform: A process which takes a **finite list** of **time-series data**, and transforms it into the **frequency domain**.

Useful for: **Signal Processing** and **noise signal identification**.

CSD

Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

PSD: Power Spectral Density

The distribution of the power received from a signal over the frequency range computed from an FFT.

$$\text{PSD}[\hat{M}_1^{\text{ex}}; f, t] = H_1^A(f, t) \cdot \overline{H_1^A(f, t)}$$

CSD: Cross Spectral Density

The distribution of power for two signals over the frequency range.

$$\text{CSD}[\hat{M}_1^{\text{ex}}, \hat{M}_2^{\text{ex}}; f, t] = H_1^A(f, t) \cdot \overline{H_2^A(f, t)}$$

4
Find PSD's
and CSD

Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

In order to achieve **sensitivity levels** at the detection limit needed to confirm we can **install FroSTI in LIGO**, we must average our **PSD and CSD** values through time.

5
Take Time
Average of
PSD's and
CSD

6
Compute
statistical
noise of CSD

7
Plot and
save
Data!

Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

1
Aquire
Raw
Data

2
Apply
Hanning
Window

4

7
Plot and
save
Data!

Statistical Noise: The **statistical noise of the CSD** gives us a measure of how **well we can trust** our **CSD** and **PSD** values.

6
**Compute
statistical
noise of CSD**

PSD's and
CSD

Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

1
Acquire
Raw
Data

2
Apply
Hanning
Window

I implemented functions in the GUI which would be able to:

Dynamically plot, display, and save the **peak noise frequency** values given from the **PSD's and CSD**.

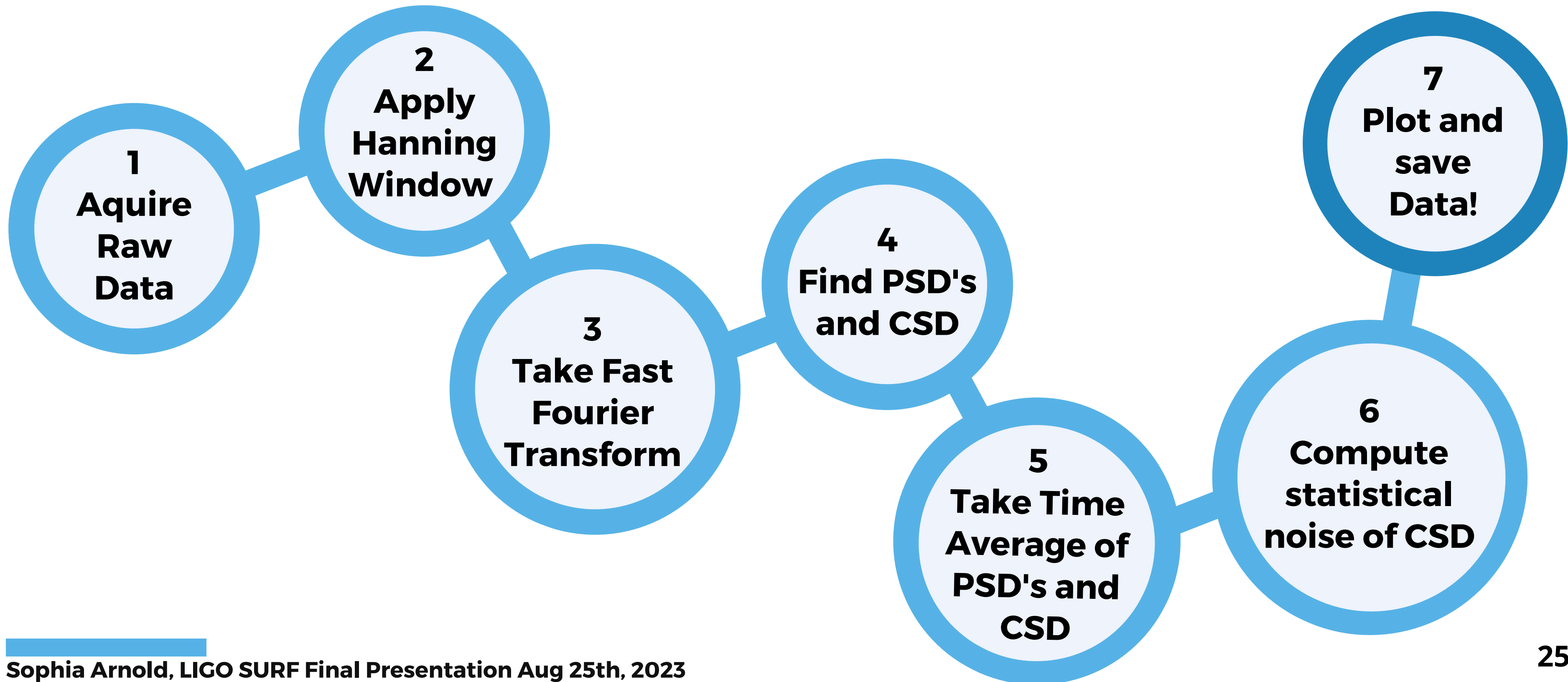
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Intensity Noise GUI Development

Pipeline for Intensity Noise Calculation GUI

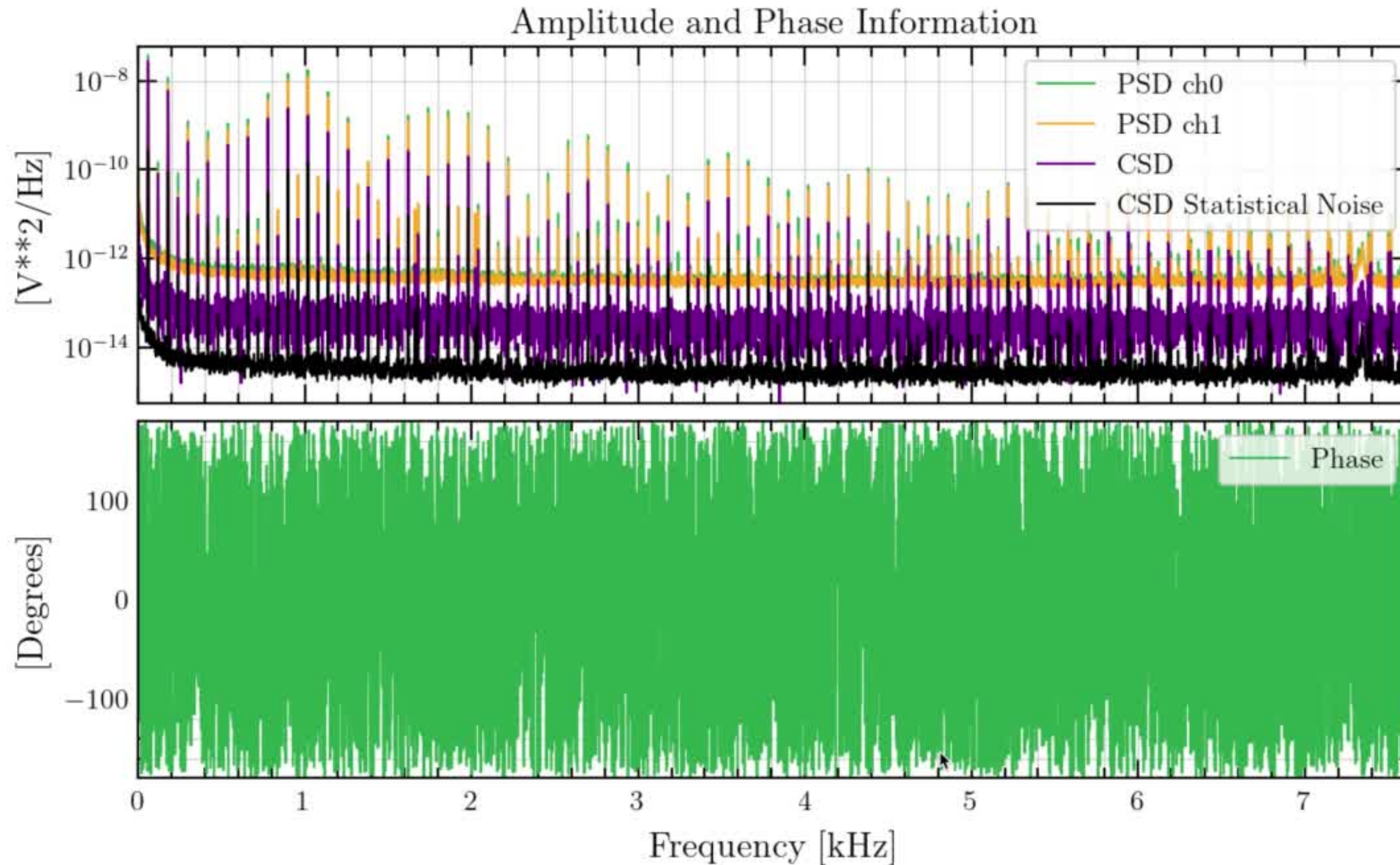


4) APPLYING THE GUI PERFORMANCE AND ACCURACY TESTS

Applying the GUI

Final GUI Interface

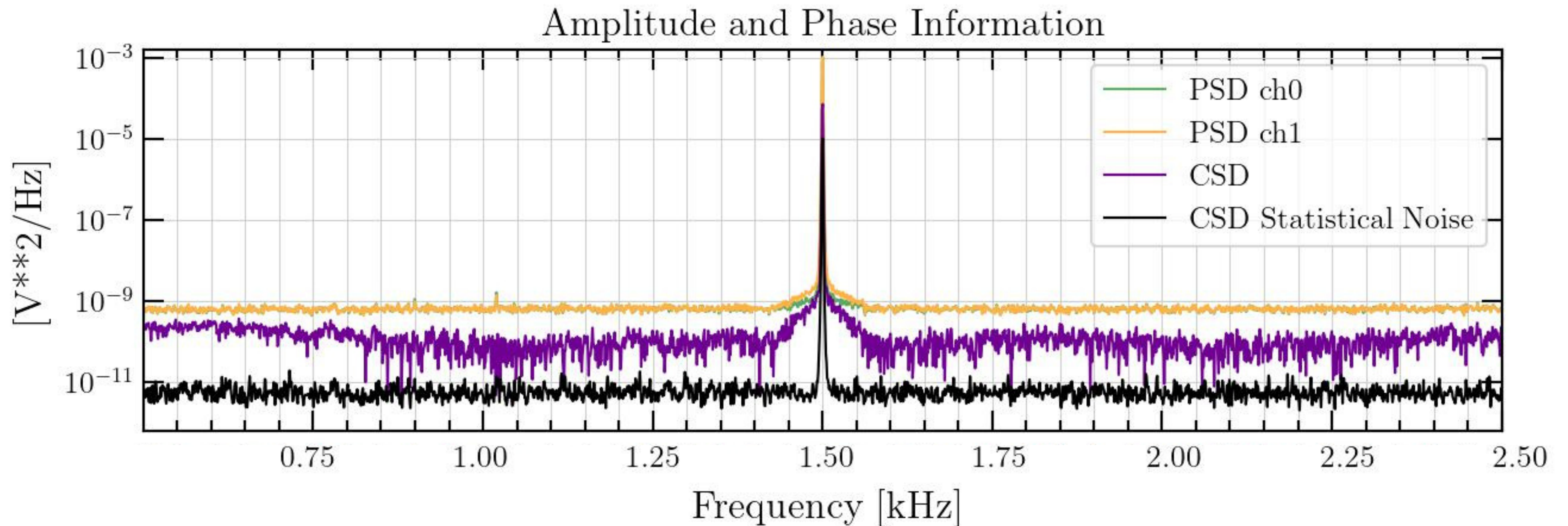
Click to Capture! Ch0: 0.00231874 V Ch1: 0.00193004 V P0 Peak: 0.0596015625 kHz P1 Peak: 0.0596015625 kHz CSD Peak: 0.0596015625 kHz Peak Phase: -169.16143098287972 [deg]



Applying the GUI

Function Generator Tests: Noise and Long Duration

Click to Capture! Ch0: 0.0161024 V Ch1: 0.0160837 V P0 Peak: 1.5002830810546874 kHz P1 Peak: 1.5002830810546874 kHz CSD Peak: 1.5002830810546874 kHz Peak Phase: -26.54383850060999 [deg]



Expected Voltage: **15mV**

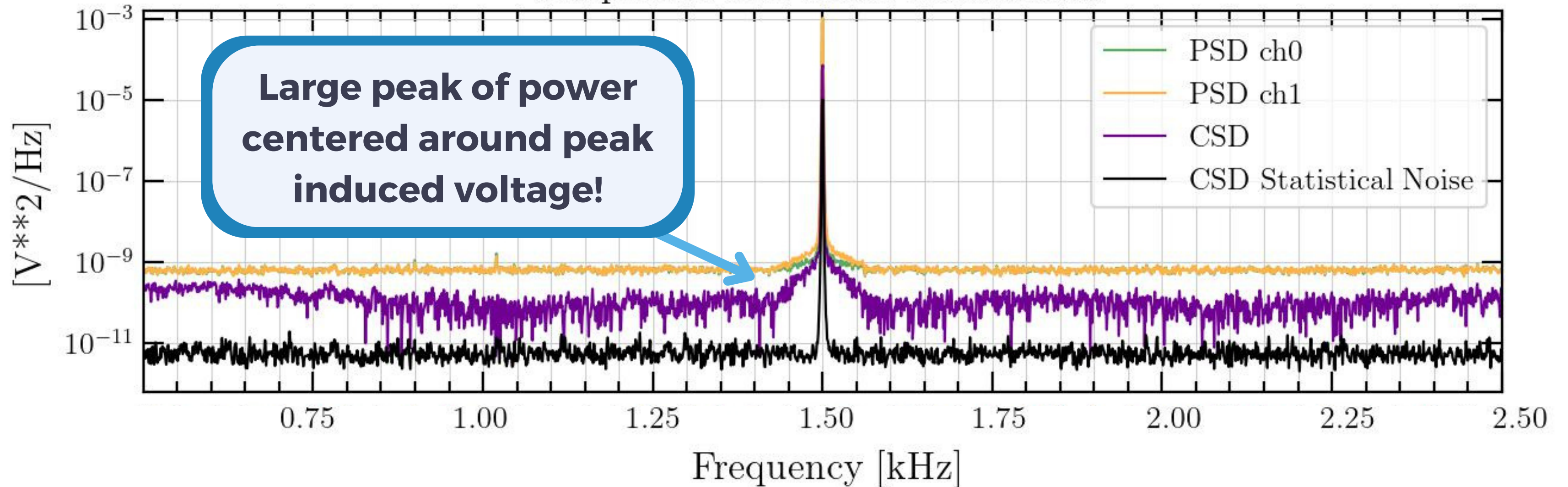
Expected Frequency: **1.5kHz**

Applying the GUI

Function Generator Tests: Noise and Long Duration

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Amplitude and Phase Information



Expected Voltage: **15mV**

Expected Frequency: **1.5kHz**

5) PROJECT SYNTHESIS

THE CULMINATION OF MY WORK

Results and Summary

Where will this GUI be applied?

This **GUI** will be used to test the **heater elements** of FroSTI, but it has the **potential for many other applications!**

This is a **universal program** which can be **updated** and used to find **electrical noise** in any **electrical system!**

ACKNOWLEDGEMENTS

Thank you **Tyler, Dr. Richardson**, and all students and faculty who have supported me throughout this program!

Additionally, thank you to the **NSF, UC Riverside**, the **LIGO Laboratory**, and the **Caltech SURF Program** for an incredible experience and opportunity!

Use my GUI for your own work at: [GitHub Link](#)

My email for any inquiries: sga46@cornell.edu



THANK YOU!

Caltech

UCR

