

Fast Digital Servo: DAC Converter Module T2400200-v1

Initialization

```
In[*]:= Needs["Controls`LinearControl`"]
```

```
In[*]:= $TextStyle = {FontFamily → "Helvetica", FontSize → 13};
```

```
In[*]:= plotopt = Sequence @@ {GridLines → Automatic, Frame → True,  
    FrameStyle → Thickness[0.0025], BaseStyle → {FontSize → 12}};
```

```
In[*]:= plotoptn[n_Integer? (# > 0 & # < 9 &)] :=  
    Sequence @@ {GridLines → Automatic, Frame → True, FrameStyle → Thickness[0.0025],  
        PlotStyle → Take[{Black, Gray, Darker[Yellow], Purple, Brown,  
            Darker[Green], Blue, Red}, -n], BaseStyle → {FontSize → 12}};  
plotoptn[n_Integer? (# ≤ 0 ∨ # ≥ 9 &)] := plotopt
```

```
In[*]:= mylegend[labels_List, pos_ : Right] :=  
    {Placed[LineLegend[labels, LabelStyle → {FontSize → 11}, LegendMargins → 2,  
        LegendFunction → (Framed[#, Background → White] &)], pos]}
```

Parallel and Serial Impedance

```
In[*]:=
par[r1_, r2_] :=  $\frac{1}{\frac{1}{r1} + \frac{1}{r2}}$ 

par[r1_, r2_, r3_] :=  $\frac{1}{\frac{1}{r1} + \frac{1}{r2} + \frac{1}{r3}}$ 

par[r1_, r2_, r3_, r4_] :=  $\frac{1}{\frac{1}{r1} + \frac{1}{r2} + \frac{1}{r3} + \text{Plus}@@\left(\frac{1}{\text{List}[r4]}\right)}$ 

ser[r1_, r2_] := r1 + r2
ser[r1_, r2_, r3_] := r1 + r2 + r3
ser[r1_, r2_, r3_, r4_] := r1 + r2 + r3 + Plus @@ List[r4]

fourkt = {FourKT → 1.62*^-20}; (* V^2/Hz/Ohm; room temperature 20C *)
```

Pole/Zero

```
In[*]:=
pole[f_, p_] :=  $\frac{1}{1 + i f / p}$ 
zero[f_, p_] :=  $1 + i f / p$ 

pole[f_, p_, Q_] :=  $\frac{1}{1 + i \frac{1}{Q} \frac{f}{p} - (f / p)^2}$ 
zero[f_, p_, Q_] :=  $1 + i \frac{1}{Q} \frac{f}{p} - (f / p)^2$ 
```

Parallel Capacitors

Transfer Function of an OpAmp

This function computes the transfer function of an idealized OpAmp circuit

g: +1 for non-inverting configuration or -1 for inverting configuration, 0 for differential configuration

z2: Impedance in feedback path [Ohm]

z1: Impedance of input path (inverting) or impedance to ground (non-inverting) [Ohm]

```
In[*]:=
OpAmp[g_, z1_, z2_] :=
  Which[g > 0, 1 +  $\frac{z2}{z1}$ , g < 0, - $\frac{z2}{z1}$ , True,  $\frac{z2}{z1}$ ]
```

Noise of an OpAmp

This function computes the equivalent input noise of an OpAmp circuit

g: +1 for non-inverting configuration or -1 for inverting configuration, 0 for differential configuration

z1: Impedance of input path (inverting) or impedance to ground (non-inverting) [Ohm]

z2: Impedance over feedback path [Ohm]

en: voltage noise [Volt]

in: current noise [Ampere]

```
In[*]:= OpAmpNoise[g_, z1_, z2_, en_, in_] :=
  Which[g > 0, If[z1 == Infinity,  $\sqrt{en^2 + 4 \text{FourKT Abs}[z2] + (in \text{Abs}[z2])^2}$ ,
     $\sqrt{en^2 + 4 \text{FourKT Abs}[\text{par}[z1, z2]] + (in \text{Abs}[\text{par}[z1, z2]])^2}$ ],
    g < 0,  $\sqrt{\left(\text{Abs}\left[1 + \frac{z1}{z2}\right]^2 en^2 + \text{Abs}[z1]^2 \left(in^2 + \text{Abs}\left[\frac{4 \text{FourKT}}{z1}\right] + \text{Abs}\left[\frac{4 \text{FourKT}}{z2}\right]\right)\right)}$ ,
    True,  $\sqrt{\left(\text{Abs}\left[1 + \frac{z1}{z2}\right]^2 en^2 + 2 \text{Abs}[z1]^2 \left(in^2 + \text{Abs}\left[\frac{4 \text{FourKT}}{z1}\right] + \text{Abs}\left[\frac{4 \text{FourKT}}{z2}\right]\right)\right)}$ ]
```

Flicker Noise: The variable \$Flicker determines if flicker noise is added or not. It can also be explicitly specified with the option Flicker.

```
In[*]:= $Flicker = True;
Clear[OpAmpNoiseFlicker];
Options[OpAmpNoiseFlicker] = {Flicker -> $Flicker};
OpAmpNoiseFlicker[f_, fknee_, opts___] :=
  If[Flicker /. {opts} /. Options[OpAmpNoiseFlicker],  $\sqrt{\frac{fknee}{f} + 1}$ , 1]
OpAmpNoiseFlicker[f_, fknee_, floor_, opts___] := floor OpAmpNoiseFlicker[f, fknee, opts]
```

Series Product of OpAmps

Computes the transfer function of several OpAmps circuits in series.

```
In[*]:= OpAmpProduct[t_, m_] := Product[t[i], {i, m}]
```

Computes the equivalent input noise of several OpAmps circuits in series.

```
In[*]:= NoiseSum[prev_, {t_, n_}] :=  $\sqrt{\text{prev}^2 + n^2}$  Abs[t]
OpAmpNoiseProduct[t_, n_, m_] :=  $\frac{\text{Fold}[\text{NoiseSum}, 0, \text{Table}[\{t[i], n[i]\}, \{i, m\}]]}{\text{Abs}[\text{OpAmpProduct}[t, m]]}$ 
OpAmpNoiseProductOut[t_, n_, m_] := Fold[NoiseSum, 0, Table[{t[i], n[i]}, {i, m}]]
```

Spectrum Math

Propagate noise spectrum

```
In[*]:= SpecProp[prev_, t_] := {#[[1]], Abs[t /. s → 2. π #[[1]] #[[2]]] & /@ prev}
SpecProp[noise_, t_, m_] := FoldList[SpecProp, noise, Table[t[[i]], {i, m}]]
```

RMS of spectrum

```
In[*]:= Clear[SpecRMS];
SpecRMS[l_List?(MatrixQ[#, NumberQ] &)] := Block[{i, sqr = 0},
  For[i = 1, i < Length[l], ++i,
    sqr += (l[[i + 1, 1]] - l[[i, 1]])  $\left(\frac{l[[i, 2]] + l[[i + 1, 2]]}{2}\right)^2$ ;
  Sqrt[sqr]]
```

Integrated RMS spectrum

```
In[*]:= Clear[RMSSpec];
RMSSpec[l_List?(MatrixQ[#, NumberQ] &), dir_ : (-1)] := Block[{i, sqr = 0, r = N[l]},
  If[dir ≥ 0,
    For[i = 2, i ≤ Length[l], ++i,
      r[[i, 2]] =  $\sqrt{r[[i - 1, 2]]^2 + r[[i, 2]]^2 (r[[i, 1]] - r[[i - 1, 1]])}$ ],
    For[i = Length[l] - 2, i ≥ 1, --i,
      r[[i, 2]] =  $\sqrt{r[[i + 1, 2]]^2 + r[[i, 2]]^2 (r[[i + 1, 1]] - r[[i, 1]])}$ ];
  r]
```

OpAmp Parameters

```
In[*]:= Clear[AD829, OP27]
AD829[f_] := {s → 2 π i f, en → enAD829, in → inAD829,
  enfloor → enfloorAD829, infloor → infloorAD829} //.
{enAD829 → OpAmpNoiseFlicker[f, ekneeAD829, enfloorAD829],
 inAD829 → OpAmpNoiseFlicker[f, ikneeAD829, infloorAD829],
 ekneeAD829 → 50, ikneeAD829 → 100, (*guess*)
 enfloorAD829 → 1.7*^-9, infloorAD829 → 1.5*^-12};
OP27[f_] := {s → 2 π i f, en → enOP27, in → inOP27,
  enfloor → enfloorOP27, infloor → infloorOP27} //.
{enOP27 → OpAmpNoiseFlicker[f, ekneeOP27, enfloorOP27],
 inOP27 → OpAmpNoiseFlicker[f, ikneeOP27, infloorOP27],
 ekneeOP27 → 2.7, ikneeOP27 → 140,
 enfloorOP27 → 3.0*^-9, infloorOP27 → 0.4*^-12};
LT1028[f_] := {s → 2 π i f, en → enLT1028, in → inLT1028,
  enfloor → enfloorLT1028, infloor → infloorLT1028} //.
```

```

{enLT1028 → OpAmpNoiseFlicker[f, ekneeLT1028, enfloorLT1028],
 inLT1028 → OpAmpNoiseFlicker[f, ikneeLT1028, infloorLT1028],
 ekneeLT1028 → 3.5, ikneeLT1028 → 250,
 enfloorLT1028 → 0.85*^-9, infloorLT1028 → 1*^-12};
LT1128[f_] := {s → 2 π i f, en → enLT1128, in → inLT1128,
 enfloor → enfloorLT1128, infloor → infloorLT1128} //.
{enLT1128 → OpAmpNoiseFlicker[f, ekneeLT1128, enfloorLT1128],
 inLT1128 → OpAmpNoiseFlicker[f, ikneeLT1128, infloorLT1128],
 ekneeLT1128 → 3.5, ikneeLT1128 → 250,
 enfloorLT1128 → 0.85*^-9, infloorLT1128 → 1*^-12};
LT1007[f_] := {s → 2 π i f, en → enLT1007, in → inLT1007,
 enfloor → enfloorLT1007, infloor → infloorLT1007} //.
{enLT1007 → OpAmpNoiseFlicker[f, ekneeLT1007, enfloorLT1007],
 inLT1007 → OpAmpNoiseFlicker[f, ikneeLT1007, infloorLT1007],
 ekneeLT1007 → 2.0, ikneeLT1007 → 120,
 enfloorLT1007 → 2.5*^-9, infloorLT1007 → 0.4*^-12};
LT1037[f_] := {s → 2 π i f, en → enLT1037, in → inLT1037,
 enfloor → enfloorLT1037, infloor → infloorLT1037} //.
{enLT1037 → OpAmpNoiseFlicker[f, ekneeLT1037, enfloorLT1037],
 inLT1037 → OpAmpNoiseFlicker[f, ikneeLT1037, infloorLT1037],
 ekneeLT1037 → 2.0, ikneeLT1037 → 120,
 enfloorLT1037 → 2.5*^-9, infloorLT1037 → 0.4*^-12};
AD797[f_] := {s → 2 π i f, en → enAD797, in → inAD797,
 enfloor → enfloorAD797, infloor → infloorAD797} //.
{enAD797 → OpAmpNoiseFlicker[f, ekneeAD797, enfloorAD797],
 inAD797 → OpAmpNoiseFlicker[f, ikneeAD797, infloorAD797],
 ekneeAD797 → 50, ikneeAD797 → 100, (*guess*)
 enfloorAD797 → 0.9*^-9, infloorAD797 → 2*^-12};
LT1012[f_] := {s → 2 π i f, en → enLT1012, in → inLT1012,
 enfloor → enfloorLT1012, infloor → infloorLT1012} //.
{enLT1012 → OpAmpNoiseFlicker[f, ekneeLT1012, enfloorLT1012],
 inLT1012 → OpAmpNoiseFlicker[f, ikneeLT1012, infloorLT1012],
 ekneeLT1012 → 2.5, ikneeLT1012 → 120, (*guess*)
 enfloorLT1012 → 14*^-9, infloorLT1012 → 6*^-15};
LT1792[f_] := {s → 2 π i f, en → enLT1792, in → inLT1792,
 enfloor → enfloorLT1792, infloor → infloorLT1792} //.
{enLT1792 → OpAmpNoiseFlicker[f, ekneeLT1792, enfloorLT1792],
 inLT1792 → OpAmpNoiseFlicker[f, ikneeLT1792, infloorLT1792],
 ekneeLT1792 → 30, ikneeLT1792 → 0, (*guess*)
 enfloorLT1792 → 4.2*^-9, infloorLT1792 → 10*^-15};
ADA4625[f_] := {s → 2 π i f, en → enADA4625, in → inADA4625,
 enfloor → enfloorADA4625, infloor → infloorADA4625} //.
{enADA4625 → OpAmpNoiseFlicker[f, ekneeADA4625, enfloorADA4625],
 inADA4625 → OpAmpNoiseFlicker[f, ikneeADA4625, infloorADA4625],
 ekneeADA4625 → 15, ikneeADA4625 → 0, (*guess*)
 enfloorADA4625 → 3.3*^-9, infloorADA4625 → 4.5*^-15};
ADA4522[f_] := {s → 2 π i f, en → enADA4522, in → inADA4522,

```

```

enfloor → enfloorADA4522, infloor → infloorADA4522} //.
{enADA4522 → OpAmpNoiseFlicker[f, ekneeADA4522, enfloorADA4522],
 inADA4522 → OpAmpNoiseFlicker[f, ikneeADA4522, infloorADA4522],
 ekneeADA4522 → 0, ikneeADA4522 → 0, (*chopper*)
 enfloorADA4522 → 7*^-9, infloorADA4522 → 1.2*^-12};
ADA4898[f_] := {s → 2 π i f, en → enADA4898, in → inADA4898,
 enfloor → enfloorADA4898, infloor → infloorADA4898} //.
{enADA4898 → OpAmpNoiseFlicker[f, ekneeADA4898, enfloorADA4898],
 inADA4898 → OpAmpNoiseFlicker[f, ikneeADA4898, infloorADA4898],
 ekneeADA4898 → 10, ikneeADA4898 → 20,
 enfloorADA4898 → 0.9*^-9, infloorADA4898 → 2.4*^-12};
PA98A[f_] := {s → 2 π i f, en → enPA98A, in → inPA98A,
 enfloor → enfloorPA98A, infloor → infloorPA98A} //.
{enPA98A → OpAmpNoiseFlicker[f, ekneePA98A, enfloorPA98A],
 inPA98A → OpAmpNoiseFlicker[f, ikneePA98A, infloorPA98A],
 ekneePA98A → 100(*guess*), ikneePA98A → 120, (*guess*)
 enfloorPA98A → 4*^-9, infloorPA98A → 1*^-12 (*guess*)};

```

ADA4898

DAC Whitening and Gain

Parameters

```

dacdewhite = {w1 → False, w2 → False};
(*ADA4898[f] or AD829[f] *)

```

DAC (AD3552R) & Driver (AD8065)

Assume this is all part of the DAC output noise which is specified at ~95dB THD for ±10V range.

```

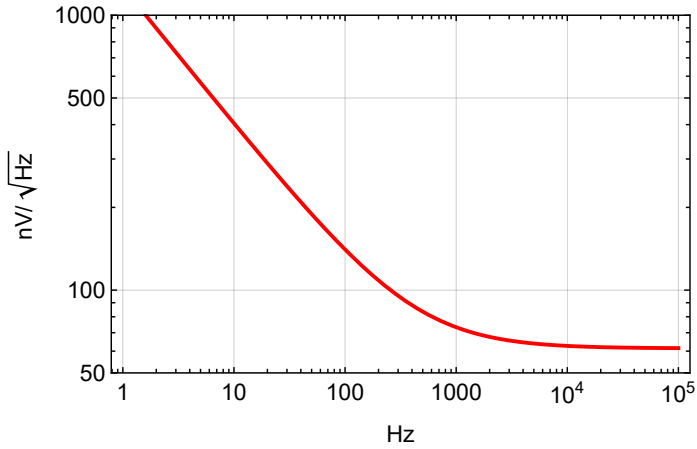
In[*]:= prmAD3552R = {FS → 10, THD → 1095/20, BW → 222, flicker10 → 400*^-9};

```

$$In[*]:= \text{dacnoise}[f_]:= \sqrt{\frac{\text{flicker10}^2}{f / 10} + \left(\frac{FS}{\sqrt{2} \text{ THD}} \frac{1}{\sqrt{BW}} \right)^2} /. \text{prmAD3552R} (* \text{ nV} / \sqrt{\text{Hz}} *)$$

```
In[*]:= LogLogPlot[1*^9 dacnoise[f], {f, 1, 100*^3}, PlotRange -> {50, 1000},
  FrameLabel -> {"Hz", "nV/√Hz"}, Evaluate[plotoptn[1]]]
```

```
Out[*]=
```



Snubber

First Stage: Dewhitening

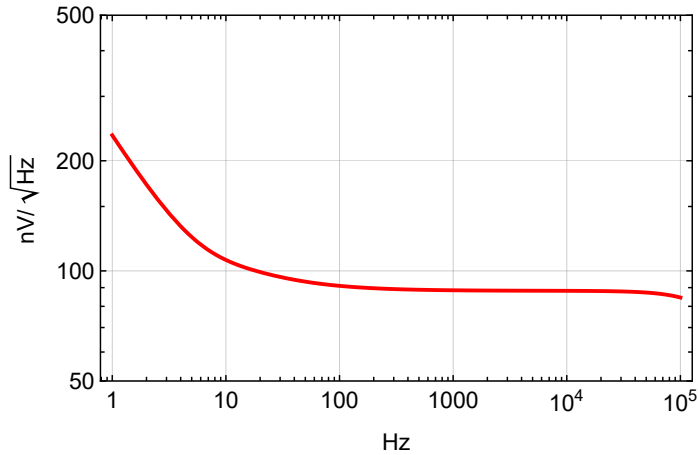
```
In[*]:= z1A[1] := 1580 +  $\frac{1}{s \cdot 10^{-6}}$ 
z2A[1] := par[15000, 4990 +  $\frac{1}{s \cdot 24.7 \cdot 10^{-12}}$ ]
z1B[1] := ∞
z2B[1] := 50
opamp[1] := If[w1,  $\frac{z1A[1]}{z1A[1] + z2A[1]}$  OpAmp[1, z1B[1], z2B[1]], 1]
opampnoise[1] := If[w1, Abs[ $\frac{z1A[1] + z2A[1]}{z1A[1]}$ ]]
 $\sqrt{\text{OpAmpNoise}[1, z1A[1], z2A[1], \text{en}, \text{in}]^2 + \text{FourKT Abs}[z3] + (\text{in Abs}[z3])^2} / .$ 
z3 -> par[z1A[1], z2A[1]], 0]
```

```

In[ ]:= LogLogPlot[1*^9 opampnoise[1] /. w1 → True /. ADA4898[f] /. fourkt, {f, 1, 100*^3},
  PlotRange → {50, 500}, FrameLabel → {"Hz", "nV/√Hz"}, Evaluate[plotoptn[1]]]

```

Out[]:=



Second Stage: Dewhitening

```

In[ ]:= z1A[2] := 1580 +  $\frac{1}{s \cdot 10^{-6}}$ 
z2A[2] := par[15000, 4990 +  $\frac{1}{s \cdot 24.7 \cdot 10^{-12}}$ ]
z1B[2] := ∞
z2B[2] := 50
opamp[2] := If[w2,  $\frac{z1A[2]}{z1A[2] + z2A[2]}$  OpAmp[1, z1B[2], z2B[2]], 1]
opampnoise[2] := If[w2, Abs[ $\frac{z1A[2] + z2A[2]}{z1A[2]}$ ]
   $\sqrt{\text{OpAmpNoise}[1, z1A[2], z2A[2], \text{en}, \text{in}]^2 + \text{FourKT Abs}[z3] + (\text{in Abs}[z3])^2}$  /.
  z3 → par[z1A[2], z2A[2]], 0]

```

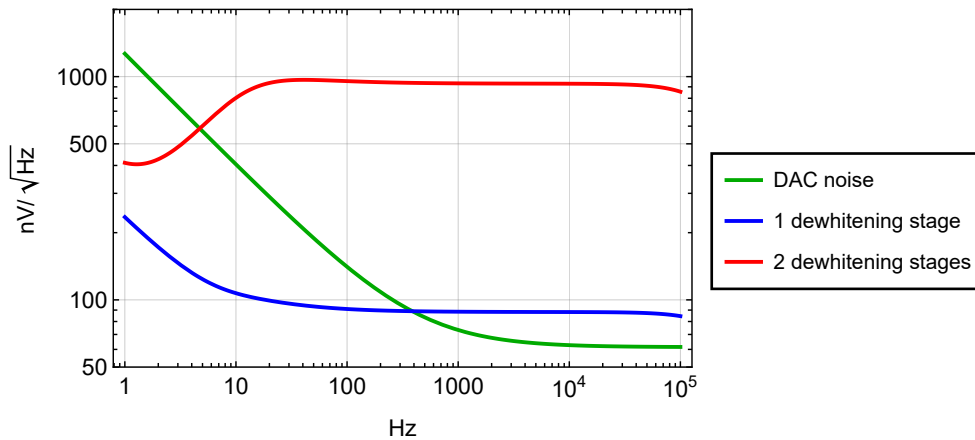
Input Referred Noise

```

In[ ]:= LogLogPlot[
  Evaluate[1*^9 {dacnoise[f], opampnoise[1], OpAmpNoiseProduct[opamp, opampnoise, 2]} /.
    {w1 → True, w2 → True} /. ADA4898[f] /. fourkt], {f, 1, 100*^3},
  PlotRange → {50, 2000}, FrameLabel → {"Hz", "nV/√Hz"}, Evaluate[plotoptn[3]],
  PlotLegends → mylegend[{"DAC noise", "1 dewatering stage", "2 dewatering stages"}]]

```

Out[]:=



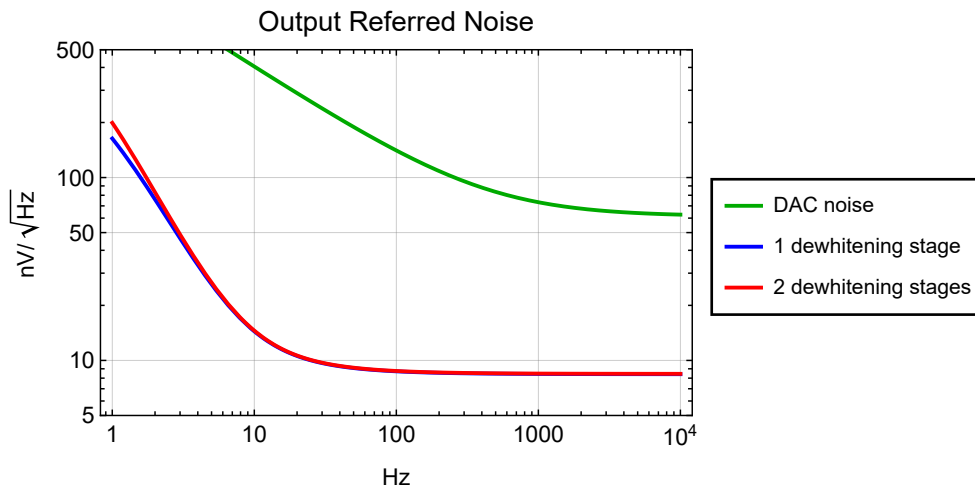
Output Referred Noise

```

In[*]:= LogLogPlot[Evaluate[1*^9 {dacnoise[f],
    OpAmpNoiseProductOut[opamp, opampnoise, 2] /. {w1 → True, w2 → False},
    OpAmpNoiseProductOut[opamp, opampnoise, 2] /. {w1 → True, w2 → True}} /.
    ADA4898[f] /. fourkt], {f, 1, 10*^3}, PlotRange → {5, 500},
    PlotLabel → "Output Referred Noise", FrameLabel1 → {"Hz", "nV/  $\sqrt{\text{Hz}}$ "},
    Evaluate[plotoptn[3]],
    PlotLegends → mylegend[{"DAC noise", "1 dewatering stage", "2 dewatering stages"}]]

```

Out[*]=

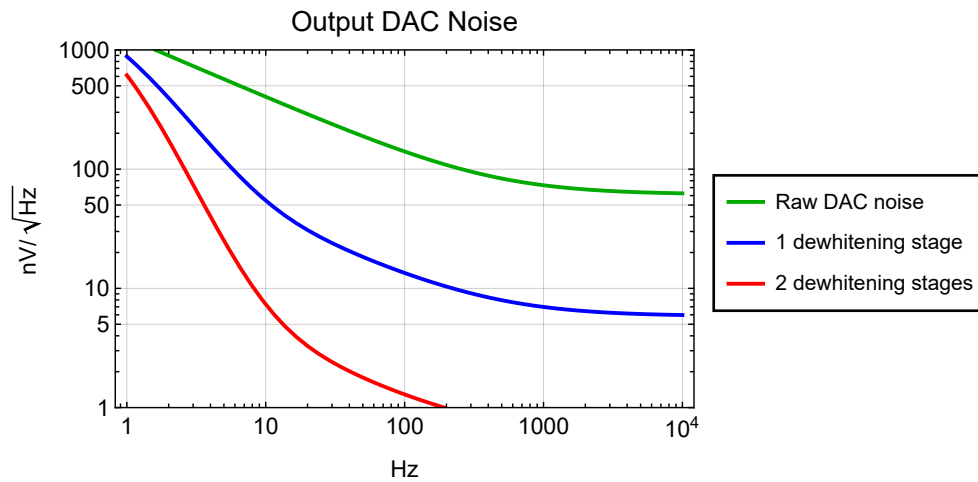


```

In[ ]:= LogLogPlot[Evaluate[
  1*^9 {dacnoise[f], Abs[OpAmpProduct[opamp, 2]] dacnoise[f] /. {w1 → True, w2 → False},
    Abs[OpAmpProduct[opamp, 2]] dacnoise[f] /. {w1 → True, w2 → True}} /. ADA4898[f] /.
    fourkt], {f, 1, 10*^3}, PlotRange → {1, 1000}, PlotLabel → "Output DAC Noise",
  FrameLabel → {"Hz", "nV/√Hz"}, Evaluate[plotoptn[3]], PlotLegends →
  mylegend[{"Raw DAC noise", "1 dewatering stage", "2 dewatering stages"}]]

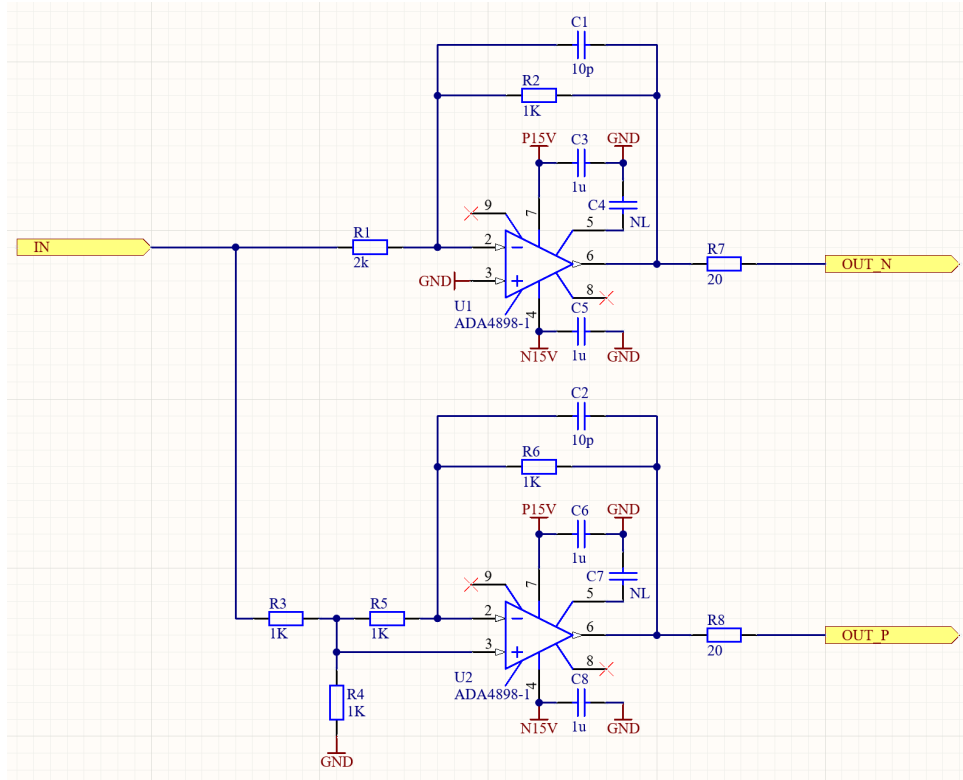
```

Out[]:=



Differential Driver

Schematics



Negative Leg

```

In[*]:= zz1[1] := R1
        zz2[1] := R2
        oopamp[1] := OpAmp[-1, zz1[1], zz2[1]]
        oopampnoise[1] := OpAmpNoise[-1, zz1[1], zz2[1], en, in]

```

```

In[*]:= PowerExpand[OpAmpNoise[-1, zz1[1], zz2[1], 0, 0]^2,
  Assumptions -> {R1 > 0, R2 > 0, FourKT > 0}]
Simplify[% /. R1 -> 2 R2]

```

Out[*]=

$$4 \text{FourKT} R1 + \frac{4 \text{FourKT} R1^2}{R2}$$

Out[*]=

$$6 \text{FourKT} R2$$

```
In[*]:= PowerExpand[OpAmpNoise[-1, zz1[1], zz2[1], en, 0]^2 /. FourKT → 0,
  Assumptions → {R1 > 0, R2 > 0}]
Simplify[% /. R1 → 2 R2]
```

```
Out[*]=

$$en^2 \left(1 + \frac{R1}{R2}\right)^2$$

```

```
Out[*]=

$$9 en^2$$

```

```
In[*]:= PowerExpand[OpAmpNoise[-1, zz1[1], zz2[1], 0, in]^2 /. FourKT → 0,
  Assumptions → {R1 > 0, R2 > 0}]
Simplify[% /. R1 → 2 R2]
```

```
Out[*]=

$$in^2 R1^2$$

```

```
Out[*]=

$$4 in^2 R2^2$$

```

Positive Leg

Equations

```
In[*]:= eq1 =  $\frac{vin - v1}{R3} + \frac{-v1}{R4} + \frac{v2 - v1}{R5} == 0$ 
eq2 =  $\frac{vout - v2}{R6} + \frac{v1 - v2}{R5} == 0$ 
Solve[{eq1, eq2, v1 == v2}, {vout}, {v1, v2}]
 $\frac{vout}{vin}$  /. %[[1]]
```

```
Out[*]=

$$-\frac{v1}{R4} + \frac{-v1 + v2}{R5} + \frac{-v1 + vin}{R3} == 0$$

```

```
Out[*]=

$$\frac{v1 - v2}{R5} + \frac{-v2 + vout}{R6} == 0$$

```

```
Out[*]=

$$\left\{ \left\{ vout \rightarrow \frac{R4 vin}{R3 + R4} \right\} \right\}$$

```

```
Out[*]=

$$\frac{R4}{R3 + R4}$$

```

Noise

$$i_{pp} = \frac{v_{in} - v_1}{R_3} + \frac{-v_1}{R_4} + \frac{v_2 - v_1}{R_5} + g_3 \sqrt{\frac{FourKT}{R_3}} + g_4 \sqrt{\frac{FourKT}{R_4}} + g_5 \sqrt{\frac{FourKT}{R_5}} == 0;$$

$$i_{nn} = \frac{v_{out} - v_2}{R_6} + \frac{v_1 - v_2}{R_5} + g_5 \sqrt{\frac{FourKT}{R_5}} + g_6 \sqrt{\frac{FourKT}{R_6}} == 0;$$

`sol = Solve[{ipp, inn, v1 == v2}, {vout}, {v1, v2}] [[1]]`

$$gain = \frac{v_{out}}{v_{in}} /. sol /. \{g_3 \rightarrow 0, g_4 \rightarrow 0, g_5 \rightarrow 0, g_6 \rightarrow 0\}$$

$$t_3 = \text{Simplify}\left[\frac{v_{out}}{gain} /. sol /. v_{in} \rightarrow 0 /. \{g_3 \rightarrow 1, g_4 \rightarrow 0, g_5 \rightarrow 0, g_6 \rightarrow 0\}\right];$$

$$t_4 = \text{Simplify}\left[\frac{v_{out}}{gain} /. sol /. v_{in} \rightarrow 0 /. \{g_3 \rightarrow 0, g_4 \rightarrow 1, g_5 \rightarrow 0, g_6 \rightarrow 0\}\right];$$

$$t_5 = \text{Simplify}\left[\frac{v_{out}}{gain} /. sol /. v_{in} \rightarrow 0 /. \{g_3 \rightarrow 0, g_4 \rightarrow 0, g_5 \rightarrow 1, g_6 \rightarrow 0\}\right];$$

$$t_6 = \text{Simplify}\left[\frac{v_{out}}{gain} /. sol /. v_{in} \rightarrow 0 /. \{g_3 \rightarrow 0, g_4 \rightarrow 0, g_5 \rightarrow 0, g_6 \rightarrow 1\}\right];$$

`FullSimplify[t32 + t42 + t52 + t62]`

`% /. {R3 → R6, R4 → R6, R5 → R6}`

`%% /. {R3 →  $\frac{4}{3} R_6$ , R4 →  $\frac{4}{3} R_6$ , R5 →  $\frac{4}{3} R_6$ }`

`Out[⌘]=`

$$\left\{ v_{out} \rightarrow -\frac{1}{R_3 + R_4} \left(-g_3 \sqrt{\frac{FourKT}{R_3}} R_3 R_4 - g_4 R_3 \sqrt{\frac{FourKT}{R_4}} R_4 - g_5 R_3 R_4 \sqrt{\frac{FourKT}{R_5}} + g_5 R_3 \sqrt{\frac{FourKT}{R_5}} R_6 + g_5 R_4 \sqrt{\frac{FourKT}{R_5}} R_6 + g_6 R_3 \sqrt{\frac{FourKT}{R_6}} R_6 + g_6 R_4 \sqrt{\frac{FourKT}{R_6}} R_6 - R_4 v_{in} \right) \right\}$$

`Out[⌘]=`

$$\frac{R_4}{R_3 + R_4}$$

`Out[⌘]=`

$$FourKT \left(R_3 + \frac{R_3^2}{R_4} + \frac{(R_3 + R_4)^2 R_6}{R_4^2} + \frac{(R_3 R_4 - (R_3 + R_4) R_6)^2}{R_4^2 R_5} \right)$$

`Out[⌘]=`

$$7 FourKT R_6$$

`Out[⌘]=`

$$7 FourKT R_6$$

```

In[*]:= ipp =  $\frac{v_{in} - v_1}{R_3} + \frac{-v_1}{R_4} + \frac{v_2 - v_1}{R_5} == 0;$ 
inn =  $\frac{v_{out} - v_2}{R_6} + \frac{v_1 - v_2}{R_5} + in == 0;$ 
sol = Solve[{ipp, inn, v1 == v2 + en}, {vout}, {v1, v2}] [[1]]
gain =  $\frac{v_{out}}{v_{in}}$  /. sol /. {in → 0, en → 0}

t1 = Simplify[ $\frac{v_{out}}{gain}$  /. sol /. vin → 0 /. {en → 0}];
t2 = Simplify[ $\frac{v_{out}}{gain}$  /. sol /. vin → 0 /. {in → 0}];
FullSimplify[t12 + t22]
PowerExpand[% /. {R3 → R6, R4 → R6, R5 → R6}, Assumptions → R6 > 0]
PowerExpand[%% /. {R3 →  $\frac{4}{3} R_6$ , R4 →  $\frac{4}{3} R_6$ , R5 →  $\frac{4}{3} R_6$ }, Assumptions → R6 > 0]

Out[*]=

$$\left\{ v_{out} \rightarrow - \frac{en R_3 R_4 + en R_3 R_5 + en R_4 R_5 + en R_3 R_6 + en R_4 R_6 + in R_3 R_5 R_6 + in R_4 R_5 R_6 - R_4 R_5 v_{in}}{(R_3 + R_4) R_5} \right\}$$


Out[*]=

$$\frac{R_4}{R_3 + R_4}$$


Out[*]=

$$\frac{in^2 (R_3 + R_4)^2 R_6^2 + \frac{en^2 (R_4 (R_5 + R_6) + R_3 (R_4 + R_5 + R_6))^2}{R_5^2}}{R_4^2}$$


Out[*]=

$$25 en^2 + 4 in^2 R_6^2$$


Out[*]=

$$\frac{81 en^2}{4} + 4 in^2 R_6^2$$


```

Total

```

In[*]:= OpAmpNoiseDiffDriverPos[r3_, r4_, r5_, r6_, en_, in_] :=

$$\sqrt{\left( \frac{(r_4 (r_5 + r_6) + r_3 (r_4 + r_5 + r_6))^2}{r_5^2 r_4^2} en^2 + in^2 \frac{(r_3 + r_4)^2}{r_4^2} r_6^2 + \right.}$$


$$\left. FourKT \left( r_3 + \frac{r_3^2}{r_4} + \frac{(r_3 + r_4)^2 r_6}{r_4^2} + \frac{(r_3 r_4 - (r_3 + r_4) r_6)^2}{r_4^2 r_5} \right) \right)}$$

OpAmpNoiseDiffDriver[r1_, r2_, r3_, r4_, r5_, r6_, en_, in_] :=

$$\sqrt{OpAmpNoise[-1, r1, r2, en, in]^2 + OpAmpNoiseDiffDriverPos[r3, r4, r5, r6, en, in]^2}$$


```

Gain $\frac{1}{2}$ Differential Driver

```

In[ ]:= noise = FullSimplify[PowerExpand[
  OpAmpNoiseDiffDriver[2 R, R, R, R, R, R, en, in], Assumptions → {R > 0, FourKT > 0}]]

Out[ ]:=

$$\sqrt{34 \text{ en}^2 + R (13 \text{ FourKT} + 8 \text{ in}^2 R)}$$


In[ ]:= Evaluate[1*^9 {OpAmpNoise[-1, R, R, en, in], noise /. R → 1000} /. ADA4898[f] /. fourkt]

Out[ ]:=

$$\left\{ 1000000000 \sqrt{3.24 \times 10^{-18} \left(1 + \frac{10}{f}\right) + \left(5.76 \times 10^{-24} \left(1 + \frac{20}{f}\right) + \frac{3.24 \times 10^{-20}}{\text{Abs}[R]}\right) \text{Abs}[R]^2}, \right.$$

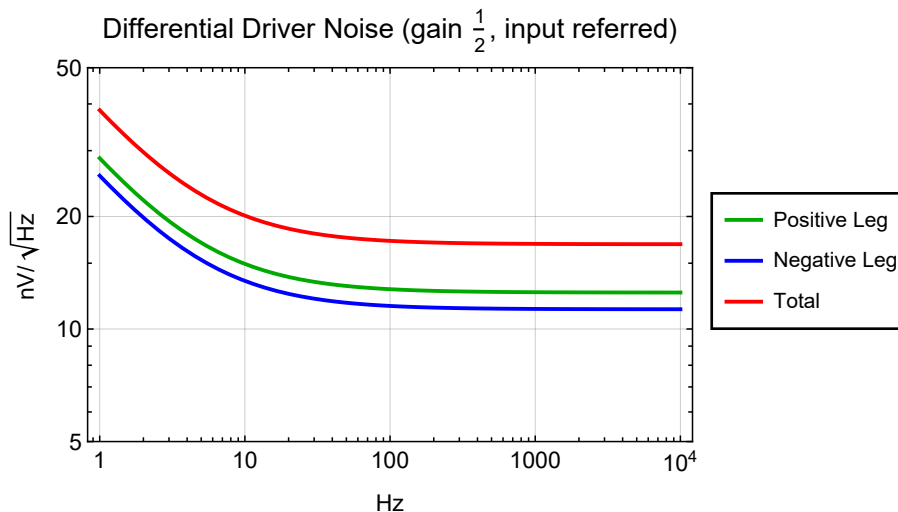

$$\left. 1000000000 \sqrt{1000 \left(2.106 \times 10^{-19} + 4.608 \times 10^{-20} \left(1 + \frac{20}{f}\right)\right) + 2.754 \times 10^{-17} \left(1 + \frac{10}{f}\right)} \right\}$$


In[ ]:= 1*^9 noise /. R → 1000 /. ADA4898[f] /. fourkt /. f → 1000
LogLogPlot[
  Evaluate[1*^9 {OpAmpNoiseDiffDriverPos[R, R, R, R, en, in], OpAmpNoise[-1, 2 R, R, en, in],
    noise} /. R → 1000 /. ADA4898[f] /. fourkt], {f, 1, 10*^3}, PlotRange → {5, 50},
  PlotLabel → "Differential Driver Noise (gain  $\frac{1}{2}$ , input referred)",
  FrameLabel → {"Hz", "nV/√Hz"}, Evaluate[plotoptn[3]],
  PlotLegends → mylegend[{"Positive Leg", "Negative Leg", "Total"}]]

Out[ ]:=
16.8943

Out[ ]:=

```



Gain 1 Differential Driver

```
In[ ]:= noise1 = FullSimplify[PowerExpand[
  OpAmpNoiseDiffDriver[R, R, 0, r4, R, R, en, in], Assumptions → {R > 0, FourKT > 0}]]
```

```
Out[ ]:= 
$$\sqrt{8 en^2 + 2 R (2 \text{FourKT} + in^2 R)}$$

```

```
In[ ]:= Evaluate[
  1*^9 {OpAmpNoiseDiffDriverPos[0, r4, R, R, en, in], OpAmpNoise[-1, R, R, en, in], noise1} /.
  R → 2000 /. ADA4898[f] /. fourkt]
```

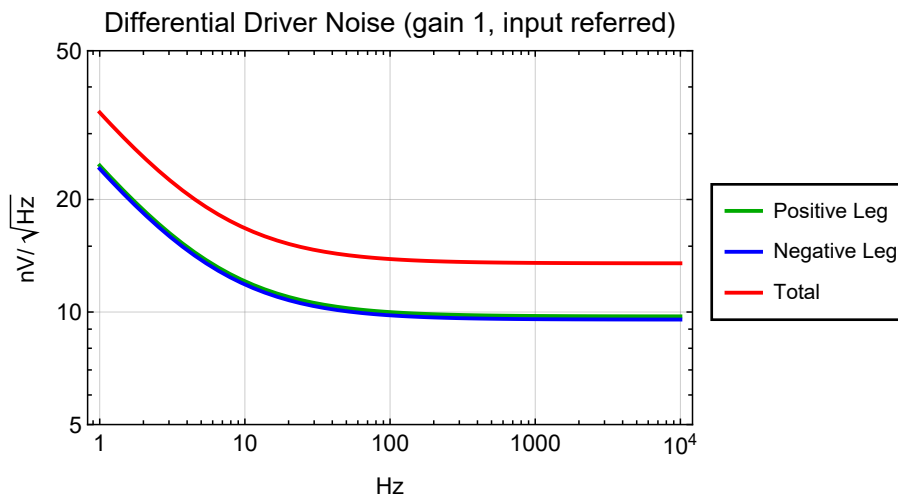
```
Out[ ]:= 
$$\begin{aligned} & \left\{ 1000000000 \sqrt{6.48 \times 10^{-17} + 3.24 \times 10^{-18} \left(1 + \frac{10}{f}\right) + 2.304 \times 10^{-17} \left(1 + \frac{20}{f}\right)}, \right. \\ & 1000000000 \sqrt{4000000 \left(1.62 \times 10^{-23} + 5.76 \times 10^{-24} \left(1 + \frac{20}{f}\right)\right) + 3.24 \times 10^{-18} \left(1 + \frac{10}{f}\right)}, \\ & \left. 1000000000 \sqrt{4000 \left(3.24 \times 10^{-20} + 1.152 \times 10^{-20} \left(1 + \frac{20}{f}\right)\right) + 6.48 \times 10^{-18} \left(1 + \frac{10}{f}\right)} \right\} \end{aligned}$$

```

```
In[ ]:= 1*^9 noise /. R → 2000 /. ADA4898[f] /. fourkt /. f → 1000
LogLogPlot[Evaluate[1*^9 {1.02 ×
  OpAmpNoiseDiffDriverPos[0, r4, R, R, en, in], OpAmpNoise[-1, R, R, en, in], noise1} /
  R → 2000 /. ADA4898[f] /. fourkt}, {f, 1, 10*^3}, PlotRange → {5, 50},
  PlotLabel → "Differential Driver Noise (gain 1, input referred)",
  FrameLabel → {"Hz", "nV/√Hz"}, Evaluate[plotoptn[3]],
  PlotLegends → mylegend[{"Positive Leg", "Negative Leg", "Total"}]]
```

```
Out[ ]:= 13.5332
```

```
Out[ ]:=
```



Whitening/Dewhitening Filters

Whitening

```
In[ ]:= prmwWhitening = {r1 → 15*^3, c1 → 33*^-12, r2 → 1.58*^3, c2 → 10*^-6};
```

$$\text{sol} = \text{Together} \left[1 + \frac{\text{par} \left[r1, \frac{1}{s \, c1} \right]}{r2 + \frac{1}{s \, c2}} \right]$$

```
Solve[Numerator[sol] == 0, s];
```

$$\frac{-s}{2. \pi} /. \% /. \text{prmwWhitening}$$

```
Solve[Denominator[sol] == 0, s];
```

$$\frac{-s}{2. \pi} /. \% /. \text{prmwWhitening}$$

```
Out[ ]:=
```

$$\frac{1 + c1 \, r1 \, s + c2 \, r1 \, s + c2 \, r2 \, s + c1 \, c2 \, r1 \, r2 \, s^2}{(1 + c1 \, r1 \, s) (1 + c2 \, r2 \, s)}$$

```
Out[ ]:=
```

$$\{3.37399 \times 10^6, 0.959919\}$$

```
Out[ ]:=
```

$$\{321525., 10.0731\}$$

Dewhitening

```

In[*]:= prmdewhitening = {r1 → 15*^3, r3 → 5*^3, c1 → 22*^-12 + 2.7*^-12, r2 → 1.58*^3, c2 → 10*^-6};

sol = Simplify[
$$\frac{r2 + \frac{1}{s c2}}{\text{par}[r1, \frac{1}{s c1} + r3] + r2 + \frac{1}{s c2}}$$
]

Solve[Numerator[sol] == 0, s]

$$\frac{-s}{2. \pi} /. \% /. \text{prmdewhitening}$$

Solve[Denominator[sol] == 0, s];

$$\frac{-s}{2. \pi} /. \% /. \text{prmdewhitening}$$


Out[*]=

$$\frac{(1 + c2 r2 s) (1 + c1 (r1 + r3) s)}{1 + c2 (r1 + r2) s + c1 s (r1 + r3 + c2 r2 r3 s + c2 r1 (r2 + r3) s)}$$


Out[*]=

$$\left\{ \left\{ s \rightarrow -\frac{1}{c2 r2} \right\}, \left\{ s \rightarrow -\frac{1}{c1 (r1 + r3)} \right\} \right\}$$


Out[*]=
{10.0731, 322.176.}

Out[*]=
{1.00219 × 106, 0.959919}

```

Plots

```

In[*]:= Show[BodePlotEx[
$$\left\{ \text{Together} \left[ 1 + \frac{\text{par}[r1, \frac{1}{s c1}]}{r2 + \frac{1}{s c2}} \right] /. s \rightarrow 2 \pi i f /. \text{prmdewhitening}, \right.$$


Simplify[
$$\frac{r2 + \frac{1}{s c2}}{\text{par}[r1, \frac{1}{s c1} + r3] + r2 + \frac{1}{s c2}}$$
] /. s → 2 π i f /. prmdewhitening,


$$\left( \text{Together} \left[ 1 + \frac{\text{par}[r1, \frac{1}{s c1}]}{r2 + \frac{1}{s c2}} \right] /. s \rightarrow 2 \pi i f /. \text{prmdewhitening} \right)$$



$$\left( \text{Simplify} \left[ \frac{r2 + \frac{1}{s c2}}{\text{par}[r1, \frac{1}{s c1} + r3] + r2 + \frac{1}{s c2}} \right] /. s \rightarrow 2 \pi i f /. \text{prmdewhitening} \right) \}, \{f, 0.1, 1*^8\},$$


PlotRange → {5, 50}, PlotLabel → "Whitening/Dewhitening Transfer Function",
Evaluate[plotoptn[3]],
PlotLegends → mylegend[{"Whitening", "Dewhitening", "Combined"}],
ImageSize → 350], ImageSize → 500]

Whitening/Dewhitening Transfer Function

```

`Out[n]=`

