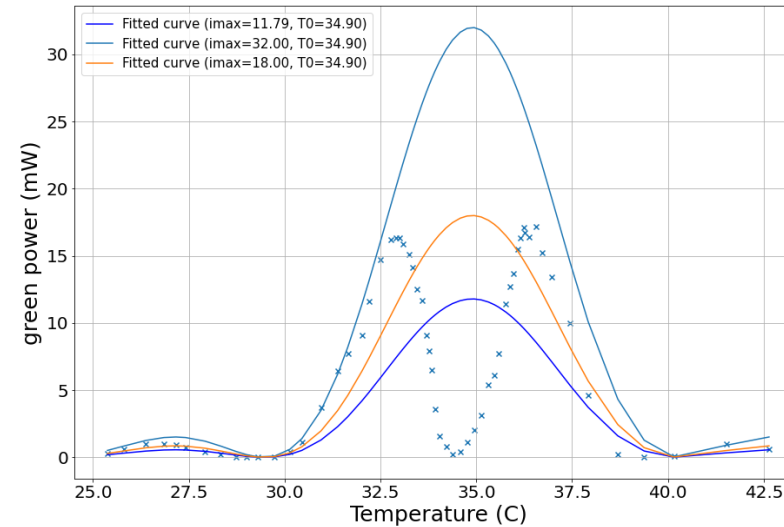
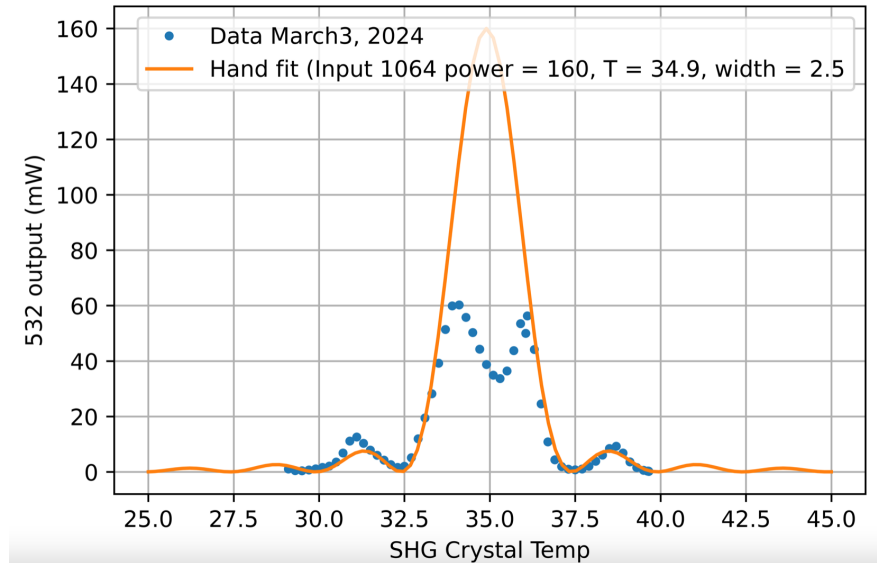


# PNW mountains



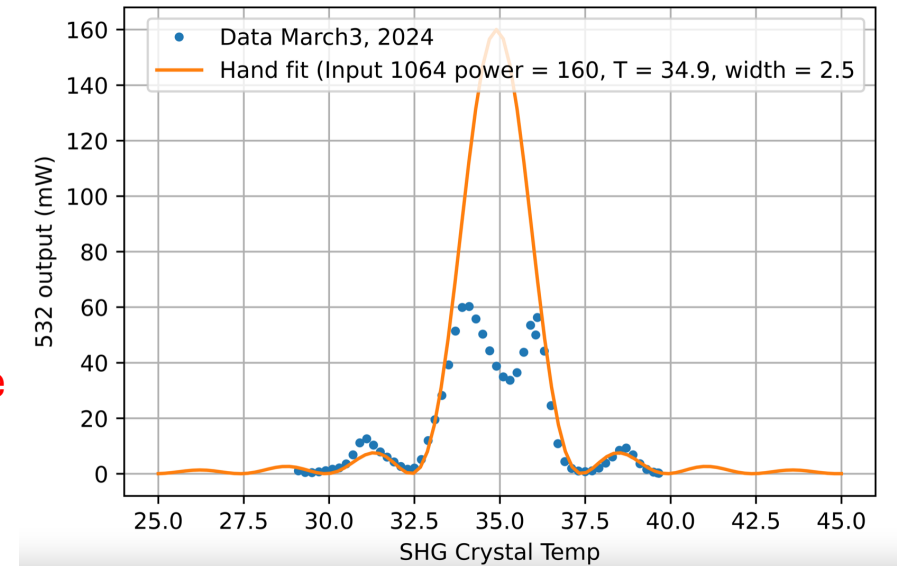
Not all of them are gray-track

Daniel, Nutsinee

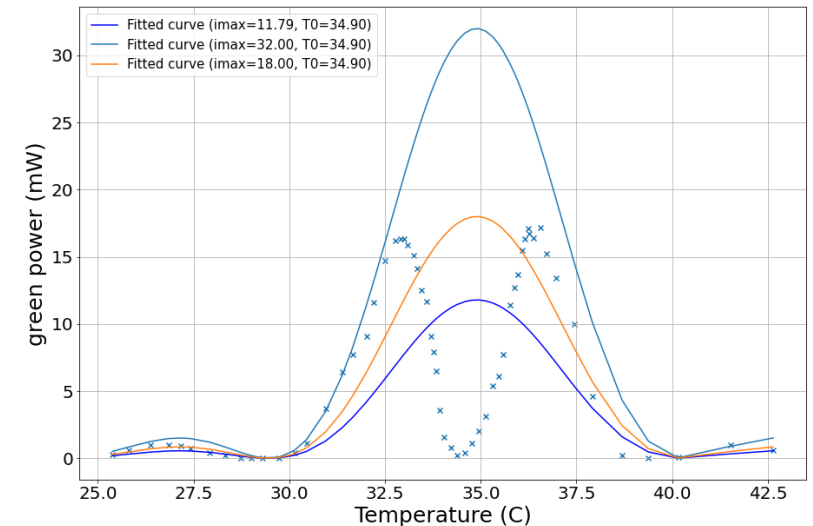
# In brand new SHGs, it's the phase mismatch!

- Well turns out it's the phase mismatch between the green and the red
- <https://alog.ligo-wa.caltech.edu/aLOG/index.php?callRep=78785>
- <https://alog.ligo-wa.caltech.edu/aLOG/index.php?callRep=78715>
- <https://alog.ligo-wa.caltech.edu/aLOG/index.php?callRep=78686>

Mount Saint Helens.  
This one can't be  
explained by the phase  
mismatch →



Twin Sisters Rock in a  
brand new SHG here  
This can't be the bloody  
gray-track now.



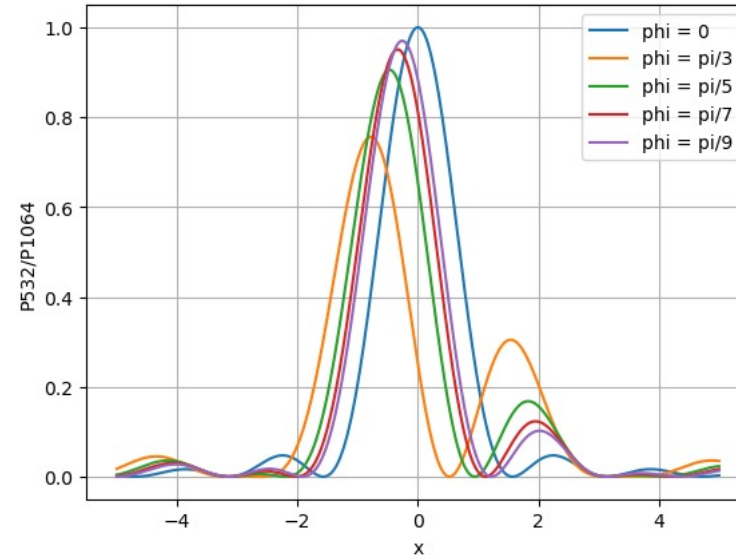
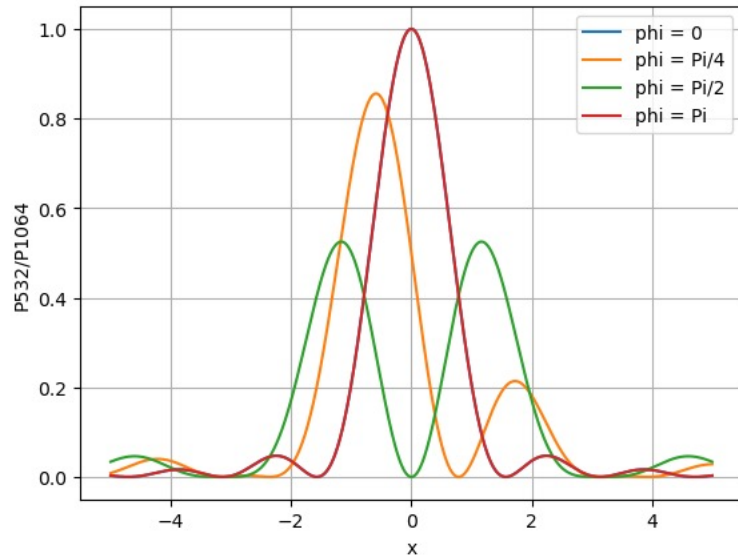
# Daniel's explanation

- “The dispersion that matters is between the first path and the second path in the crystal. In a simple dual path system, green light will be generated in phase with the red light in the first path, then the two frequencies propagate in air towards the rear mirror, where they are reflected with potentially different phases, and then propagate back to the crystal. According to Gonzalez et al. the dispersion in air for 1064/532 is  $27.4^\circ/\text{cm}$  (double passed). Our SHG length is about 5 cm long with a 1 cm crystal. So, the in-air path is of order 4 cm. You need a  $90^\circ$  phase shift to explain the double peak. However, the phase difference of our mirror reflectivity is unknown.” [alog78939](#)

# Virgo SHG paper (2018)

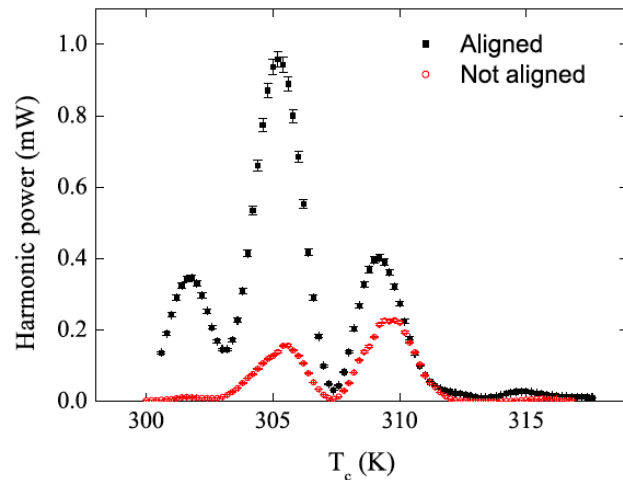
- Leonardi et al. 2018 eq. 2 taken into account a phase difference
- <https://iopscience.iop.org/article/10.1088/1555-6611/aad84d>

$$\frac{P_{2\omega}}{P_{\omega}^2} \propto \text{sinc}^2(x) \cos^2(x + \delta\phi). \quad (2)$$

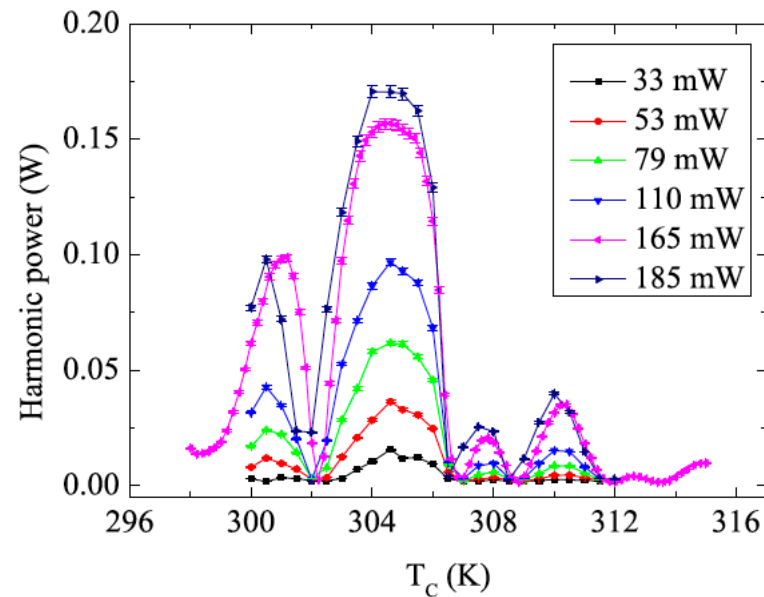


# Virgo SHG paper (2018)

- They saw similar things we did in the double pass



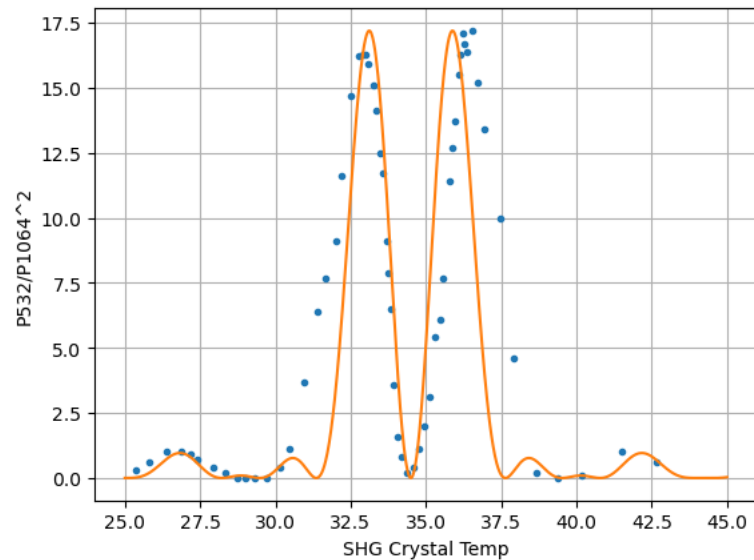
**Figure 3.** Second harmonic power in the double-pass configuration as a function of the PPKTP crystal temperature  $T_c$ , at two different beam alignments with respect to the PPKTP crystal: best overlap (black full squares) and slightly misaligned input beam (red open circles). The power data correspond to the time average of the PD3 signal, while the error bars represent the standard deviation. For each point we waited for the temperature to stabilize before acquiring the data. With the best alignment, maximum conversion is achieved at  $T_c = T_m \equiv 305.5$  K.



**Figure 7.** The phase-matching curve of the SHG cavity at various (mode matched) input fundamental powers as a function of the PPKTP crystal temperature  $T_c$ . In the legend: the input fundamental power for each curve.

# Virgo SHG paper

- An actual first attempt to fit to Karmeng's data



```
def SHGsincos(T, A, T0, width, phi):  
    return A*((np.sinc((T-T0)/(width*np.pi)))**2)*(np.cos(((T-T0)/width)+phi)**2)  
  
t = np.linspace(25, 45, 1000)
```

```
plt.plot(ktemp, kgreen, '.')  
  
#plt.plot(temp, green, '.', t, SHGsinc(t,*Popt))  
plt.plot(t, SHGsincos(t,23,34.5,1.7, np.pi/2))  
#plt.plot(t, SHGsinc(t,60,34.2,2))  
#plt.plot(t, SHGsinc(t,60,36,1.5))  
  
plt.grid()  
plt.xlabel('SHG Crystal Temp')  
plt.ylabel('P532/P1064^2')  
plt.rcParams["figure.dpi"] = 100
```

# Double pass using prism (1973)

- Ref 10 of the previous paper, Gonzalez, Nieh, and Steier 1973 took air dispersion into account
- <https://ieeexplore.ieee.org/stamp/stamp.jsp?tp=&arnumber=1077338>

$$P_2 = K_0 P_1^2 \sin^2 \left( \frac{\Delta k l_c}{2} \right) \cos^2 \left( \frac{\Delta k l_c}{2} + \frac{2\omega}{c} l \Delta n + \Delta \phi \right), \quad (1)$$

where

$$K_0 = 2\eta^3 \omega^2 (d^2 l_c^2 / \pi W^2),$$

$\omega$  angular frequency of fundamental,

$d$  nonlinear coefficient,

$\Delta n = n(2\omega) - n(\omega)$ —dispersion of air,

$\Delta \phi = (\phi/2)(2\omega) - \phi(\omega)$  phase shifts due to mirror coatings,

$W$  radius of fundamental beam,

$$\Delta k = k_1(\omega) - 2k_2(2\omega),$$

$$\eta = 377/n.$$

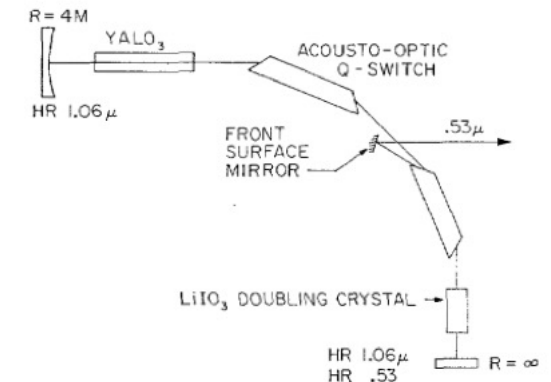


Fig. 1. Experimental configuration.

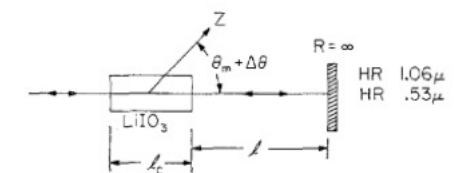


Fig. 2. Two-pass second-harmonic configuration.

# Double pass using prism (1973)

- These guys saw similar behavior we saw. And the measurements don't necessary match the model

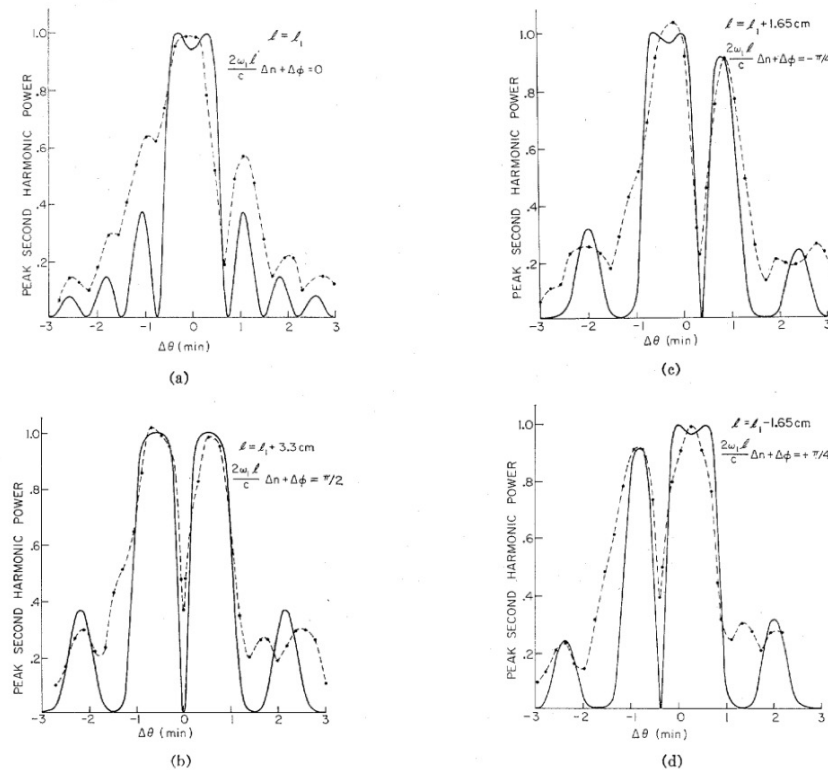


Fig. 3. Peak second-harmonic power versus crystal orientation.



# Kato and Takaoka 2002

- Eq 1 in the 1973 paper is a  $\text{sinc}^2$  function in terms of phase ( $\delta K \cdot l$ ).  $K$  is related to  $n$  which relates to  $T$ . We need this equation in terms of temperature.
- Kato and Takaoka 2002 gives you  $n$  of ppktp at 1064 and  $dn/dT$
- Kiyoshi Kato and Eiko Takaoka, "Sellmeier and thermo-optic dispersion formulas for KTP," Appl. Opt. **41**, 5040-5044 (2002)  
<https://opg.optica.org/ao/abstract.cfm?URI=ao-41-24-5040>

$$\begin{aligned}
n_x^2 &= 3.29100 + \frac{0.04140}{\lambda^2 - 0.03978} + \frac{9.35522}{\lambda^2 - 31.45571}, \\
n_y^2 &= 3.45018 + \frac{0.04341}{\lambda^2 - 0.04597} + \frac{16.98825}{\lambda^2 - 39.43799}, \\
n_z^2 &= 4.59423 + \frac{0.06206}{\lambda^2 - 0.04763} + \frac{110.80672}{\lambda^2 - 86.12171},
\end{aligned}
\tag{1}$$

This is PPKTP n at T=20C  
This is f(a) in the Taylor  
series expansion

$$\begin{aligned}
\frac{dn_x}{dT} &= \left( \frac{0.1717}{\lambda^3} - \frac{0.5353}{\lambda^2} + \frac{0.8416}{\lambda} + 0.1627 \right) \\
&\quad \times 10^{-5} (^\circ\text{C}^{-1}) \quad (0.43 \leq \lambda \leq 1.58), \\
\frac{dn_y}{dT} &= \left( \frac{0.1997}{\lambda^3} - \frac{0.4063}{\lambda^2} + \frac{0.5154}{\lambda} + 0.5425 \right) \\
&\quad \times 10^{-5} \quad (0.43 \leq \lambda \leq 1.58), \\
\frac{dn_z}{dT} &= \left( \frac{0.9221}{\lambda^3} - \frac{2.9220}{\lambda^2} + \frac{3.6677}{\lambda} - 0.1897 \right) \\
&\quad \times 10^{-5} \quad (0.53 \leq \lambda \leq 1.57) \\
&= \left( \frac{-0.5523}{\lambda} + 3.3920 - 1.7101\lambda + 0.3424\lambda^2 \right) \\
&\quad \times 10^{-5} \quad (1.32 \leq \lambda \leq 3.53),
\end{aligned}
\tag{2}$$

This is f'(a)

$$f(a) + \frac{f'(a)}{1!}(x - a) \cdot$$

(x-a) is (T-20)

Where T is the thing we  
want to sweep

Delta K is defined in Leonardi et al (the  
Virgo SHG paper), page 3 bottom right.

on the phase mismatch  $x = \Delta k L / 2$ . For crystals based on the  
quasi-phase-matching (QPM) technique, as in our PPKTP  
crystal,  $\Delta k = 4\pi / \lambda_\omega (n_{2\omega} - n_\omega) - \Delta k_{QPM}$ ,  $\Delta k_{QPM} = 2\pi / \Lambda$

deltaK and the sinc^2 function becomes

```
def deltaKz(T):
    lambdagr = 0.532
    lambdair = 1.064
    pollength = 8.99608

    ngr1 = np.sqrt(4.59423+(0.06206/(lambdagr**2-0.04763))+(110.80672/(lambdagr**2-86.12171)))
    ngr2 = (((0.9221/lambdagr**3)-(2.922/lambdagr**2)+(3.6677/lambdagr)-0.1897)*1e-5)*(T-20)
    nir1 = np.sqrt(4.59423+(0.06206/(lambdair**2-0.04763))+(110.80672/(lambdair**2-86.12171)))
    nir2 = (((0.9221/lambdair**3)-(2.922/lambdair**2)+(3.6677/lambdair)-0.1897)*1e-5)*(T-20)

    deltaKz = (4*np.pi/(lambdair))*((ngr1+ngr2)-(nir1+nir2))-(2*np.pi/pollength)
    return deltaKz

def SHGsincosair(T, A, n, phi):
    lcry = 10000 #crystal length 10000 um

    return A* np.sinc(deltaKz(T)*lcry/(2*np.pi))**2 * np.cos( (deltaKz(T)*lcry)/2 + 2*n + phi)**2
```

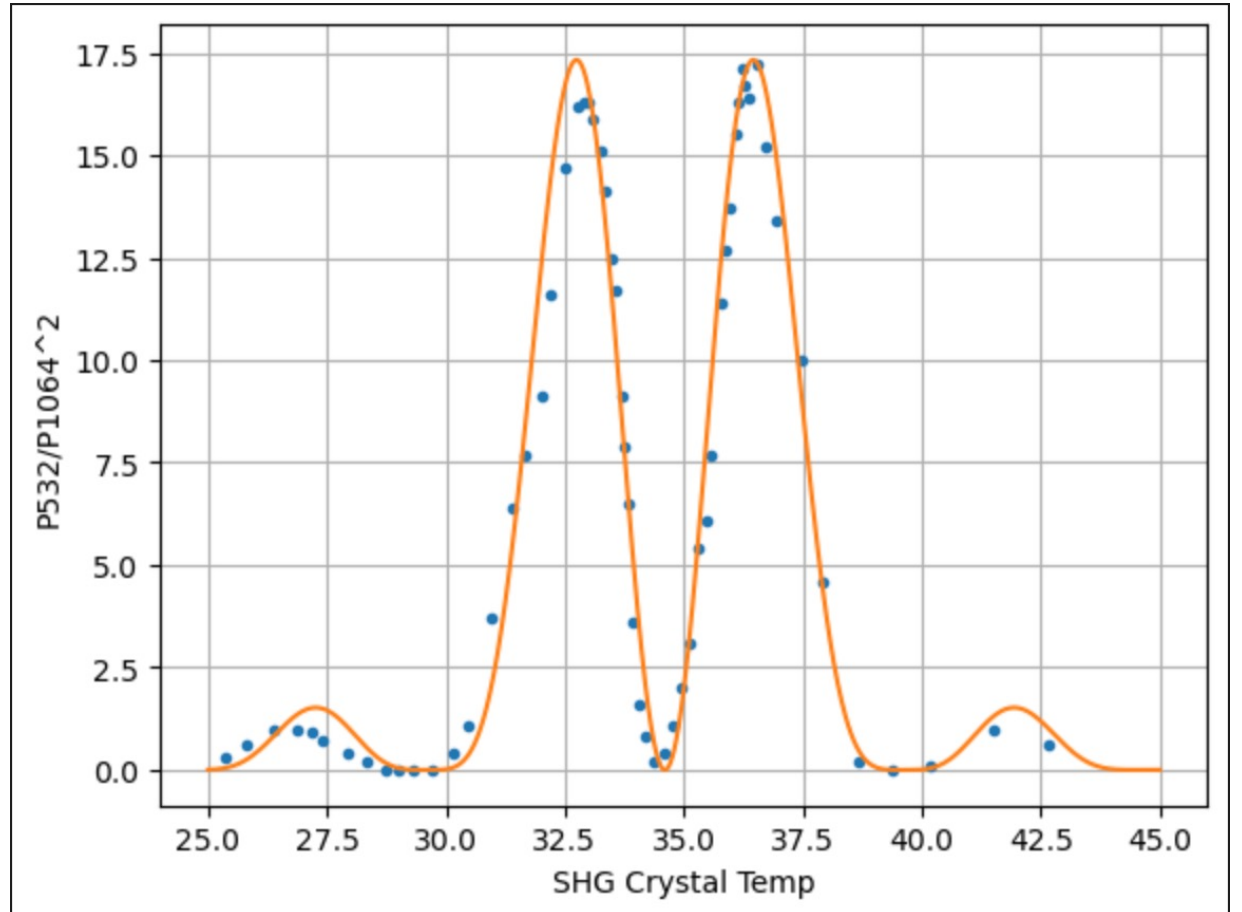
# Fitting the actual data

- The function is super sensitive to the polling length. Raicol claims 9um polling length but that's probably not exact.
- Karmeng's data supposed to peak at at 34.6 C. This corresponds to a polling length = 8.99608 um ( $\Delta K = 0$  at this T).
- Add a phase mismatch of  $\pi/2$  and you have a self-destruct  $\text{sinc}^2$  in the middle

# Fitting the actual data

```
plt.plot(ktemp, kgreen, '.')  
  
#plt.plot(temp, green, '.', t, SHGsinc(t,*Popt))  
plt.plot(t, SHGsincosair(t,33, 0, np.pi/2))  
  
plt.grid()  
plt.xlabel('SHG Crystal Temp')  
plt.ylabel('P532/P1064^2')  
plt.rcParams["figure.dpi"] = 100
```

✓ 0.1s



# The nonlinear part

- Right now the unit of  $K_0$  makes no sense.
- This paper sounds more sensible
- [https://www.sciencedirect.com/science/article/pii/S0030401897003386?ref=cra\\_js\\_challenge&fr=RR-1](https://www.sciencedirect.com/science/article/pii/S0030401897003386?ref=cra_js_challenge&fr=RR-1)

Green and ultraviolet quasi-phase-matched second harmonic generation in bulk periodically-poled  $\text{KTiOPO}_4$

A. Arie <sup>a</sup>, G. Rosenman <sup>a</sup>, V. Mahal <sup>a</sup>, A. Skliar <sup>a</sup>, M. Oron <sup>b</sup>, M. Katz <sup>b</sup>, D. Eger <sup>b</sup>

<sup>a</sup> Department of Electrical Engineering – Physical Electronics, Faculty of Engineering, Tel Aviv University, 69978 Tel Aviv, Israel

<sup>b</sup> NRC, 81800 Soreq, Israel

Received 20 March 1997; revised 12 June 1997; accepted 17 June 1997

$$\eta_{\text{SH}} = \frac{P_{2\omega}}{P_{\omega}} = \left( \frac{2\omega^2 d_{\text{eff}}^2 k_{\omega} P_{\omega}}{\pi n_{\omega}^2 n_{2\omega} \epsilon_0 c^3} \right) Lh(B, \xi). \quad (1)$$

# Boyd-Kleinman factor

- G. D. Boyd and D. A. Kleinman, “Parametric interactions of focused Gaussian light beams,”
- I don’t have access to J. Appl Phys. Daniel sent one to me. Why is Adelaide Library so shit?
- Apparently there’s a thing call the focusing parameter  $l/b = 2.84$  where  $l$  is the length of the crystal and  $b$  is the confocal parameter ( $2 \times \text{Rayleigh length}$ ) and the Boyd-Kleinman factor  $h(B, l/b)$  is 1 ish in an optimal SHG.

# Parametric Interaction of Focused Gaussian Light Beams

G. D. BOYD

*Bell Telephone Laboratories, Incorporated, Holmdel, New Jersey*

AND

D. A. KLEINMAN

*Bell Telephone Laboratories, Incorporated, Murray Hill, New Jersey*

(Received 5 February 1968)

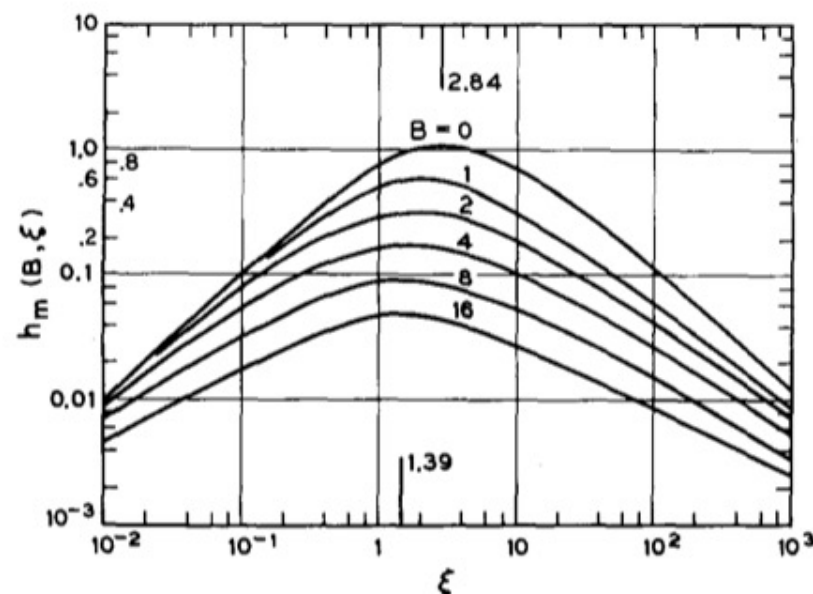


FIG. 2. SHG power (2.22) represented by the function  $h_m(B, \xi)$  (2.29) for optimum phase matching as a function of focusing parameter  $\xi = l/b$  for several values of double-refraction parameter  $B = \rho(lk_l)^{1/2}/2$ . Vertical lines indicate optimum focusing in the limits of small and large  $B$ .

# After everything was understood...

<https://alog.ligo-wa.caltech.edu/aLOG/index.php?callRep=78686> With nonlinear coefficient

```
def deltaKz(T):
    lambdagr = 0.532
    lambdair = 1.064
    pollength = 8.99608

    ngr1 = np.sqrt(4.59423+(0.06206/(lambdagr**2-0.04763))+(110.80672/(lambdagr**2-86.12171)))
    ngr2 = (((0.9221/lambdagr**3)-(2.922/lambdagr**2)+(3.6677/lambdagr)-0.1897)*1e-5)*(T-20)
    nir1 = np.sqrt(4.59423+(0.06206/(lambdair**2-0.04763))+(110.80672/(lambdair**2-86.12171)))
    nir2 = (((0.9221/lambdair**3)-(2.922/lambdair**2)+(3.6677/lambdair)-0.1897)*1e-5)*(T-20)

    deltaKz = (4*np.pi/(lambdair))*((ngr1+ngr2)-(nir1+nir2))-(2*np.pi/pollength)
    return deltaKz

def SHGsincosair(T, A, phi):
    lcry = 10000 #crystal length 10000 um

    return A* np.sinc(deltaKz(T)*lcry/(2*np.pi))**2 * np.cos( (deltaKz(T)*lcry)/2 + phi)**2

def SHGsincosKappa(T,deff,Pw, h, phi):
    lcry = 10000 #crystal length 10000 um
    lcry_m = 10e-3 #crystal length 10000 um
    nw = nir1+nir2
    n2w = ngr1+ngr2
    eta = 377/n
    lambda_m = 1064e-9
    c = 299792458
    f = c/lambda_m
    omega = 2*np.pi*f
    W = 140 #um
    kw = 2*np.pi/lambda_m
    eps = 8.8541878188e-12 #vacuum permittivity C/(V*m)

    #d = 10e-6 #10pm/V Virgo SHG paper
    #Kappa = 2*eta**3*omega**2*(deff**2*lcry**2/(np.pi*W**2)) #1973 paper
    Kappa = ((2*omega**2*deff**2*kw*Pw**2)/(np.pi*nw**2*n2w*eps*c**3))*lcry_m*h

    return Kappa*np.sinc(deltaKz(T)*lcry/(2*np.pi))**2 * np.cos( (deltaKz(T)*lcry)/2 + phi)**2
```

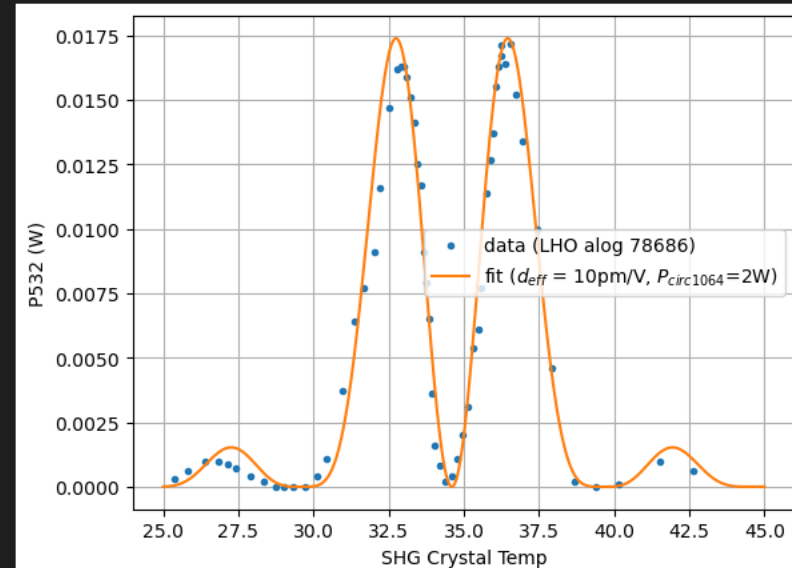
0.0s

```
plt.plot(ktemp, kgreen, '.')

plt.plot(temp, green, '.', t, SHGsinc(t,*Popt))
plt.plot(t, SHGsincosKappa(t, 10e-12, 2, 0.9, np.pi/2))

plt.grid()
plt.xlabel('SHG Crystal Temp')
plt.ylabel('P532 (W)')
plt.legend(['data (LHO alog 78686)', 'fit ($d_{eff}$ = 10pm/V, $P_{circ1064}$=2W)'],loc="best")
plt.rcParams["figure.dpi"] = 100
```

[691] ✓ 0.1s





# Update Jul 11 24

- Fit to a single pass measurement
- Alog <https://alog.ligo-wa.caltech.edu/aLOG/index.php?callRep=79017>
- Added a factor of 4 to  $K_0$  in double peak case (double pass power = 4 times the single pass)
- Need 1.5W circ to fit. Model suggests 1.7W circ with escape efficiency measurement taken into account
- Modulation depth unknown.

## SHG Cavity Response (1064)

```
In[ ]:= ClearAll["Global`*"]
```

```
In[325]:= R1 = .9;
R2 = 0.99850 - .014; (*Karmeng's escape efficiency measurement, alog 78571*)
(*R2 = 0.9985;*)
Rloss = R2 - 0.096;
T1 = 1 - R1;
T2 = 1 - R2;
t1 =  $\sqrt{T1}$ ;
t2 =  $\sqrt{T2}$ ;
r1 =  $\sqrt{R1}$ ;
r2 =  $\sqrt{R2}$ ;
rloss =  $\sqrt{Rloss}$ ;
```

```
In[335]:=  $\lambda cr = 1064 \times 10^{-9}$ ;
fcr = 0;
c = 299 792 458;
L = 0.05; (*cavity length*)
FSR =  $\frac{c}{2 L}$ ;
Fin =  $\frac{\text{Pi} \sqrt{r1 r2}}{1 - r1 r2}$ ; (*based on Finesse Living Review*)
Finwithloss =  $\frac{\text{Pi} \sqrt{r1 r2 rloss}}{1 - r1 r2 rloss}$ ;
FWHM =  $\frac{\text{FSR}}{\text{Fin}}$ ;
FWHM2024 =  $\frac{1.8 \times 3 \times 10^9}{54}$ ;
FWHMwithloss =  $\frac{\text{FSR}}{\text{Finwithloss}}$ ;
Pin =  $60 \times 10^{-3}$ ;
Ein =  $\sqrt{\text{Pin}}$ ;
```

```
Out[341]= 26.2516
```

```
Out[343]=  $1. \times 10^8$ 
```

```
Out[344]=  $1.142 \times 10^8$ 
```

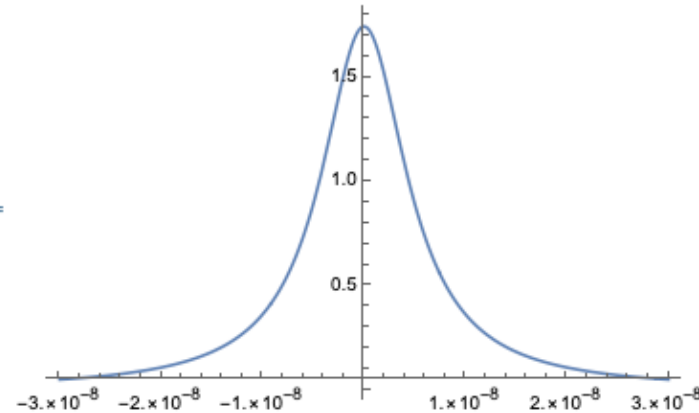
```
In[347]:= Ecirccr =  $\frac{\text{Ein} t1}{1 - r1 r2 E^{-2 + I \left( \text{Pi} \left( \frac{fcr}{FSR} + 2 \pi \frac{\delta l}{\lambda cr} \right) \right)}}$ ;
Etranscr =  $\frac{\text{Ein} t1 t2 E^{-I \left( \text{Pi} \left( \frac{fcr}{FSR} + 2 \pi \frac{\delta l}{\lambda cr} \right) \right)}}{1 - r1 r2 E^{-2 + I \left( \text{Pi} \left( \frac{fcr}{FSR} + 2 \pi \frac{\delta l}{\lambda cr} \right) \right)}}$ ;
Ereflcr =  $-r1 \text{Ein} + t1 r2 \text{Ecirccr} E^{-2 + I \left( \text{Pi} \left( \frac{fcr}{FSR} + 2 \pi \frac{\delta l}{\lambda cr} \right) \right)}$ ;

Pcirc = Ecirccr Ecirccr*;
Ptrans = Etranscr Etranscr*;
Prefl = Ereflcr Ereflcr*;
```

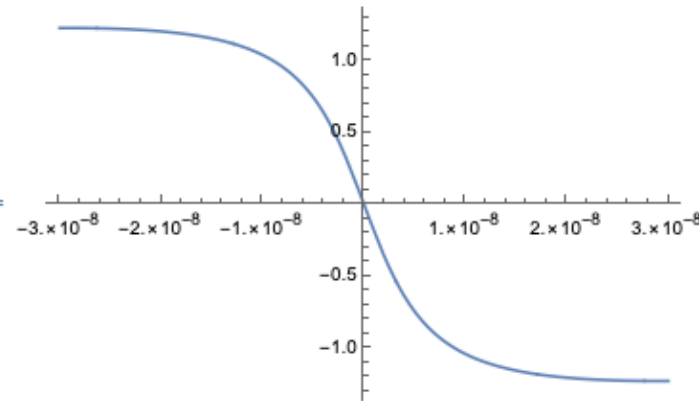
Circ

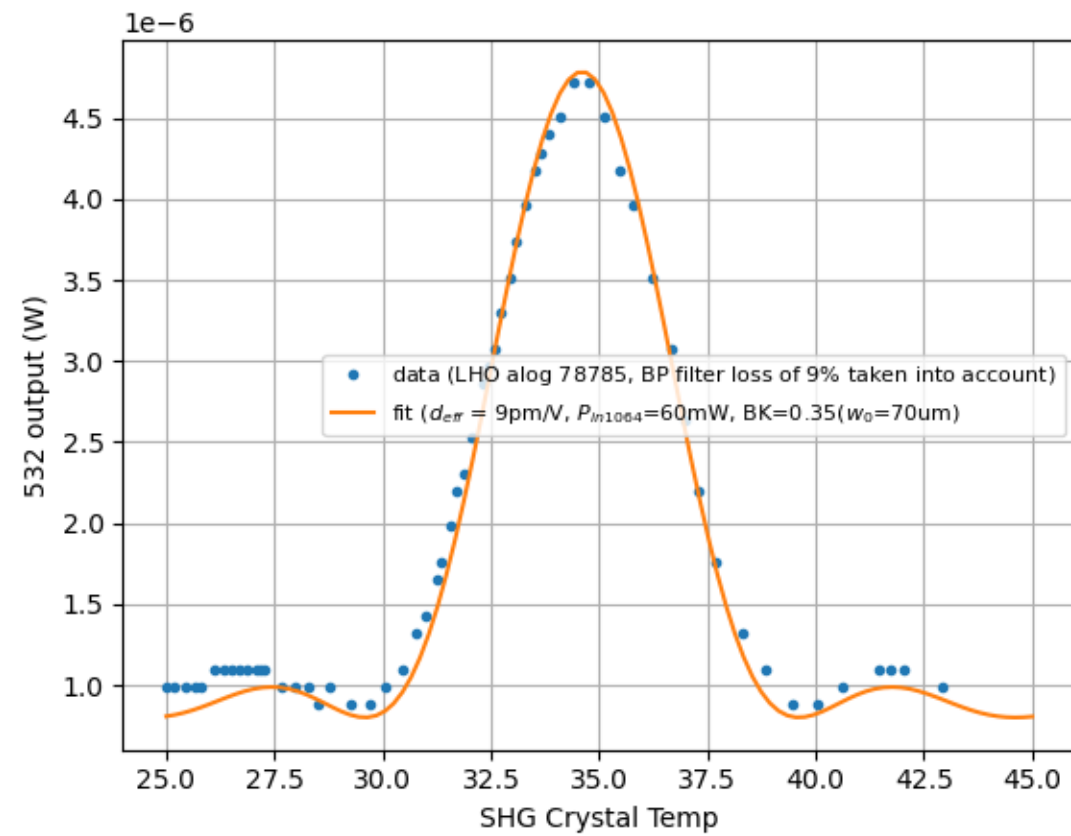
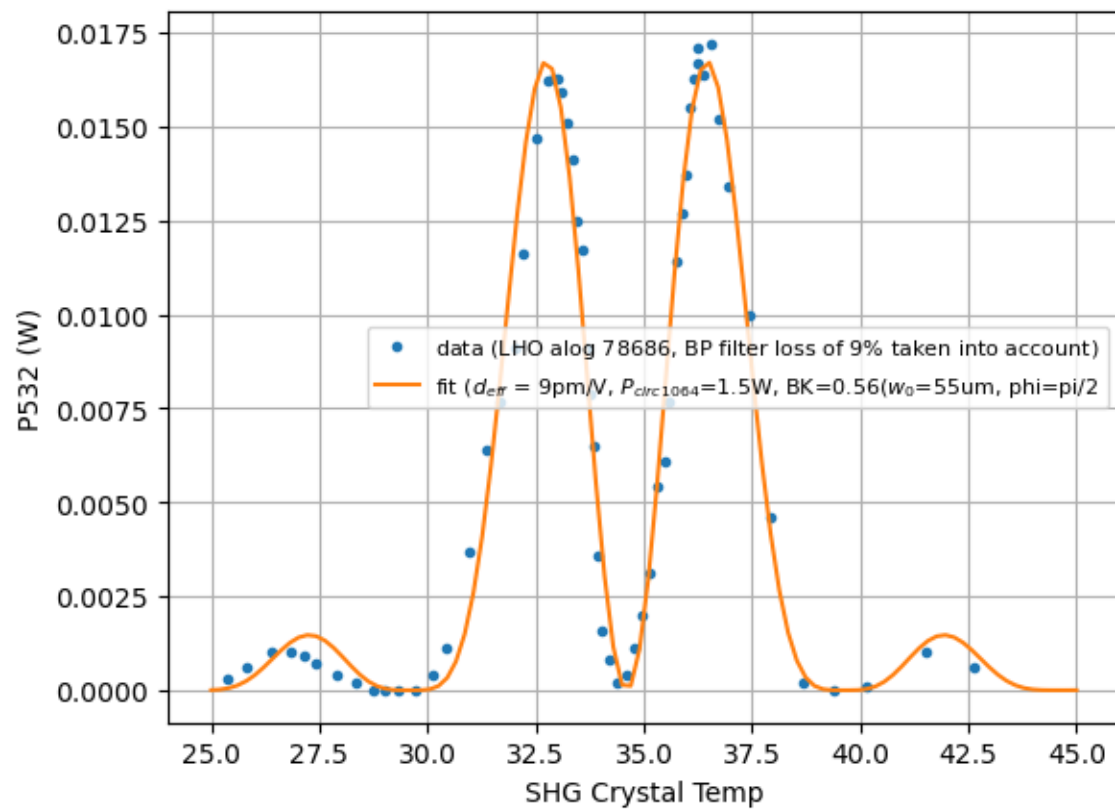
```
In[353]:= Plot[Pcirc, { $\delta l$ ,  $-3 \times 10^{-8}$ ,  $3 \times 10^{-8}$ }, PlotRange -> All]
Plot[Arg[Ecirccr], { $\delta l$ ,  $-3 \times 10^{-8}$ ,  $3 \times 10^{-8}$ }, PlotRange -> All]
```

Out[353]=



Out[354]=





Different Boyd-Klienman factor because cavity vs no cavity

# single pass sinc^2

```
lambdagr = 0.532
lambdair = 1.064
pollength = 8.99608
lcry = 10000 #crystal length 10000 um
lcry_m = 10e-3 #crystal length 10000 um

def deltaKz(T):
    ngr1 = np.sqrt(4.59423+(0.06206/(lambdagr**2-0.04763))+(110.80672/(lambdagr**2-86.12171)))
    ngr2 = (((0.9221/lambdagr**3)-(2.922/lambdagr**2)+(3.6677/lambdagr)-0.1897)*1e-5)*(T-20)
    nir1 = np.sqrt(4.59423+(0.06206/(lambdair**2-0.04763))+(110.80672/(lambdair**2-86.12171)))
    nir2 = (((0.9221/lambdair**3)-(2.922/lambdair**2)+(3.6677/lambdair)-0.1897)*1e-5)*(T-20)

    deltaKz = (4*np.pi/(lambdair))*((ngr1+ngr2)-(nir1+nir2))-(2*np.pi/pollength)
    return deltaKz
```

#single pass SHG

```
def SHGsincsingle(T,deff,Pw, h, DN):
    ngr1 = np.sqrt(4.59423+(0.06206/(lambdagr**2-0.04763))+(110.80672/(lambdagr**2-86.12171)))
    ngr2 = (((0.9221/lambdagr**3)-(2.922/lambdagr**2)+(3.6677/lambdagr)-0.1897)*1e-5)*(T-20)
    nir1 = np.sqrt(4.59423+(0.06206/(lambdair**2-0.04763))+(110.80672/(lambdair**2-86.12171)))
    nir2 = (((0.9221/lambdair**3)-(2.922/lambdair**2)+(3.6677/lambdair)-0.1897)*1e-5)*(T-20)
    nw = nir1+nir2
    n2w = ngr1+ngr2
    #eta = 377/n
    lambda_m = 1064e-9
    c = 299792458
    f = c/lambda_m
    omega = 2*np.pi*f
    W = 140 #um
    kw = 2*np.pi/lambda_m
    eps = 8.8541878188e-12 #vacuum permittivity C/(V*m)

    #d = 10e-6 #10pm/V Virgo SHG paper
    #Kappa = 2*eta**3*omega**2*(deff**2*lcry**2/(np.pi*W**2)) #1973 paper
    Kappa = ((2*omega**2*deff**2*kw*Pw**2)/(2*np.pi*nw**2*n2w*eps*c**3))*lcry_m*h

    return Kappa*np.sinc(deltaKz(T)*lcry)/(4*np.pi)**2 * np.cos((deltaKz(T)*lcry)/4)**2 +DN
```

# Double Pass Sinc^2

+ Code + Markdown

```
lambdagr = 0.532
lambdair = 1.064
pollength = 8.99608
lcry = 10000 #crystal length 10000 um
lcry_m = 10e-3 #crystal length 10000 um
l = 20000 # distance between crystal and back mirror
```

```
def deltaKz(T):
    ngr1 = np.sqrt(4.59423+(0.06206/(lambdagr**2-0.04763))+(110.80672/(lambdagr**2-86.12171)))
    ngr2 = (((0.9221/lambdagr**3)-(2.922/lambdagr**2)+(3.6677/lambdagr)-0.1897)*1e-5)*(T-20)
    nir1 = np.sqrt(4.59423+(0.06206/(lambdair**2-0.04763))+(110.80672/(lambdair**2-86.12171)))
    nir2 = (((0.9221/lambdair**3)-(2.922/lambdair**2)+(3.6677/lambdair)-0.1897)*1e-5)*(T-20)

    deltaKz = (4*np.pi/(lambdair))*((ngr1+ngr2)-(nir1+nir2))-(2*np.pi/pollength)
    return deltaKz
```

```
def SHGsincsair(T, A, phi):

    return A* np.sinc(deltaKz(T)*lcry/(2*np.pi))**2 * np.cos((deltaKz(T)*lcry)/2 + phi)**2
```

#double pass SHG

```
def SHGsincsKappa(T,deff,Pw, h, phi):
    ngr1 = np.sqrt(4.59423+(0.06206/(lambdagr**2-0.04763))+(110.80672/(lambdagr**2-86.12171)))
    ngr2 = (((0.9221/lambdagr**3)-(2.922/lambdagr**2)+(3.6677/lambdagr)-0.1897)*1e-5)*(T-20)
    nir1 = np.sqrt(4.59423+(0.06206/(lambdair**2-0.04763))+(110.80672/(lambdair**2-86.12171)))
    nir2 = (((0.9221/lambdair**3)-(2.922/lambdair**2)+(3.6677/lambdair)-0.1897)*1e-5)*(T-20)
    nw = nir1+nir2
    n2w = ngr1+ngr2
    #eta = 377/n
    lambda_m = 1064e-9
    c = 299792458
    f = c/lambda_m
    omega = 2*np.pi*f
    W = 140 #um
    kw = 2*np.pi/lambda_m
    eps = 8.8541878188e-12 #vacuum permittivity C/(V*m)

    #d = 10e-6 #10pm/V Virgo SHG paper
    #Kappa = 2*eta**3*omega**2*(deff**2*lcry**2/(np.pi*W**2)) #1973 paper
    Kappa = 4*((2*omega**2*deff**2*kw*Pw**2)/(np.pi*nw**2*n2w*eps*c**3))*lcry_m*h #extra factor of 4 in power dur to double pass

    return Kappa*np.sinc(deltaKz(T)*lcry/(2*np.pi))**2 * np.cos((deltaKz(T)*lcry)/2 + phi)**2
```

# Beam waist

- Used Finesse to determine beam waist inside of the SHG cavity with the crystal inside given known parameters
- A beam waist is required to compute Boyd-Klienman constant
- Single pass waist with or without the crystal is different by 2  $\mu\text{m}$ . Negligible.

```

kat = finesse.Model()
kat.parse(
    """
    # Add a Laser named L0 with a power of 1 W.
    l L0 P=1

    # Space attaching L0 <=> m1 with length of 0 m (default).
    s s0 L0.p1 m1.p1 L=1

    # Input mirror of cavity.
    m m1 R=0.9 T=0.0999999999999998 Rc=-0.025

    # m1 to c1 (crystal)
    s s1 m1.p2 c1.p1 L=0.0185

    # PPKTP crystal input c1
    m c1 R=0 T=1

    # PPKTP length
    s crystal c1.p2 c2.p1 L=0.01 nr=1.8298794813610717

    # PPKTP crystal output c2
    m c2 R=0 T=1

    # c2 to m2
    s s2 c2.p2 m2.p1 L=0.0185

    # End mirror of cavity.
    m m2 R=0.9985 T=.001499 Rc=0.025

    # Power detectors on reflection, circulation and transmission.
    pd refl m1.p1.o
    pd circ m2.p1.i
    pd trns m2.p2.o

    # Scan over the detuning DOF of m1 from -180 deg to +180 deg with 400 points.
    xaxis(m1.phi, lin, -180, 180, 10000)
    """
)

# Add a cavity object
kat.add(components.Cavity("SHG", kat.m1.p2.o, kat.m2.p1.i))

```

```

print(kat.SHG.draw())
[43]
...
o m1.p2.o
  o c1.p1.i
    o c1.p2.o
      o c2.p1.i
        o c2.p2.o
          o m2.p1.i
            o m2.p1.o
              o c2.p2.i
                o c2.p1.o
                  o c1.p2.i
                    o c1.p1.o
                      o m1.p2.i

```

```

(function) SHG: Any
kat.SHG.q
[96]
...
array([<BeamParam (w0=55.038 um, w=141.78 um, z=-21.232 mm, nr=1, λ=1.064 um) at 0x16e4f9990>,
      <BeamParam (w0=55.038 um, w=141.78 um, z=-21.232 mm, nr=1, λ=1.064 um) at 0x16e4f9ab0>],
      dtype=object)

```

