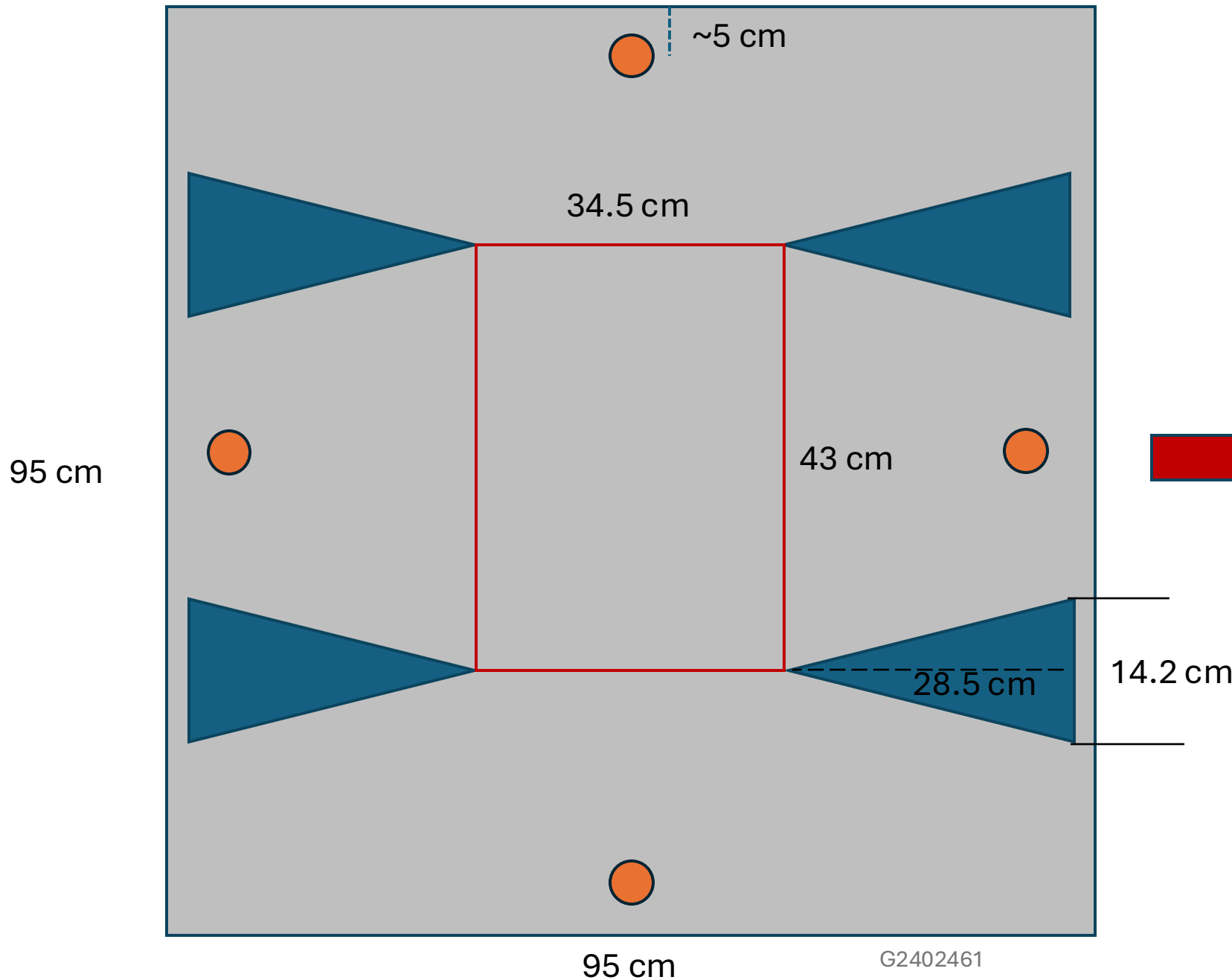


3rd BHQS Workshop Slides

Edgard Bonilla

Outline

- Design refresher
- Numbers for the design
- Show the LSC | ASC loops
 - It works easily at 800 kW
 - Challenging at 1.5 MW
- Uncertainty analysis
 - 0.25 mm seems like the d-value uncertainty
 - At 1 mm we would just get more low-f RMS
- How good do the sensors need to be?
 - 1 e-11 is good enough for all dofs.
 - 1 e-12 for UIM sensors would get most of the design where we want it.
- Anything we missed?
 - Roll mode estimate – 9.5 Hz? – Let's not cut the PUM
 - Smaller PUM – Depends on Roll
 - Higher resonance in Pitch – I think it is worth it, but only helps above 1 MW power

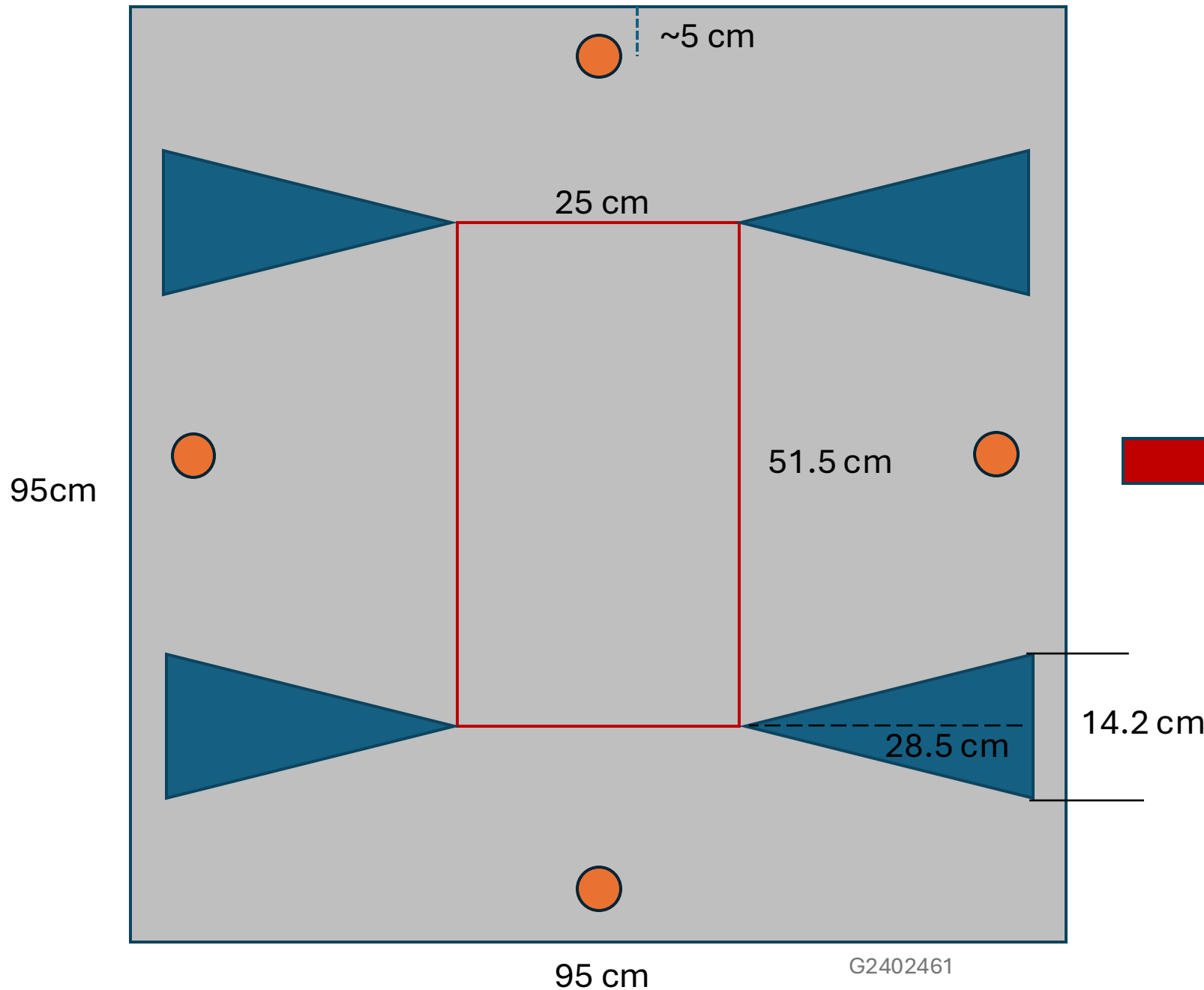


Top Mass (top view)

Beam tube direction



- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)

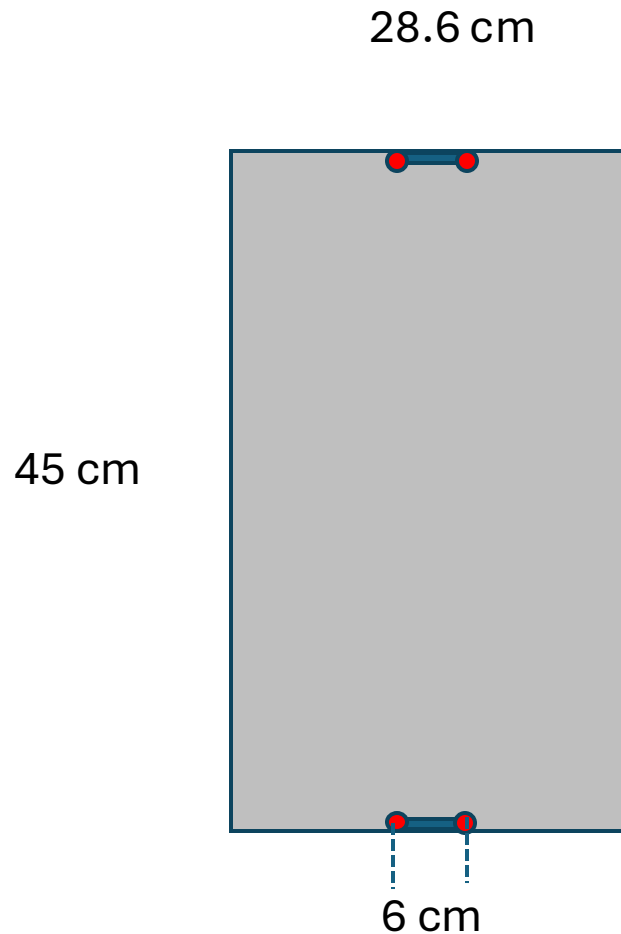


UIM (top view)

Beam tube direction



- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)

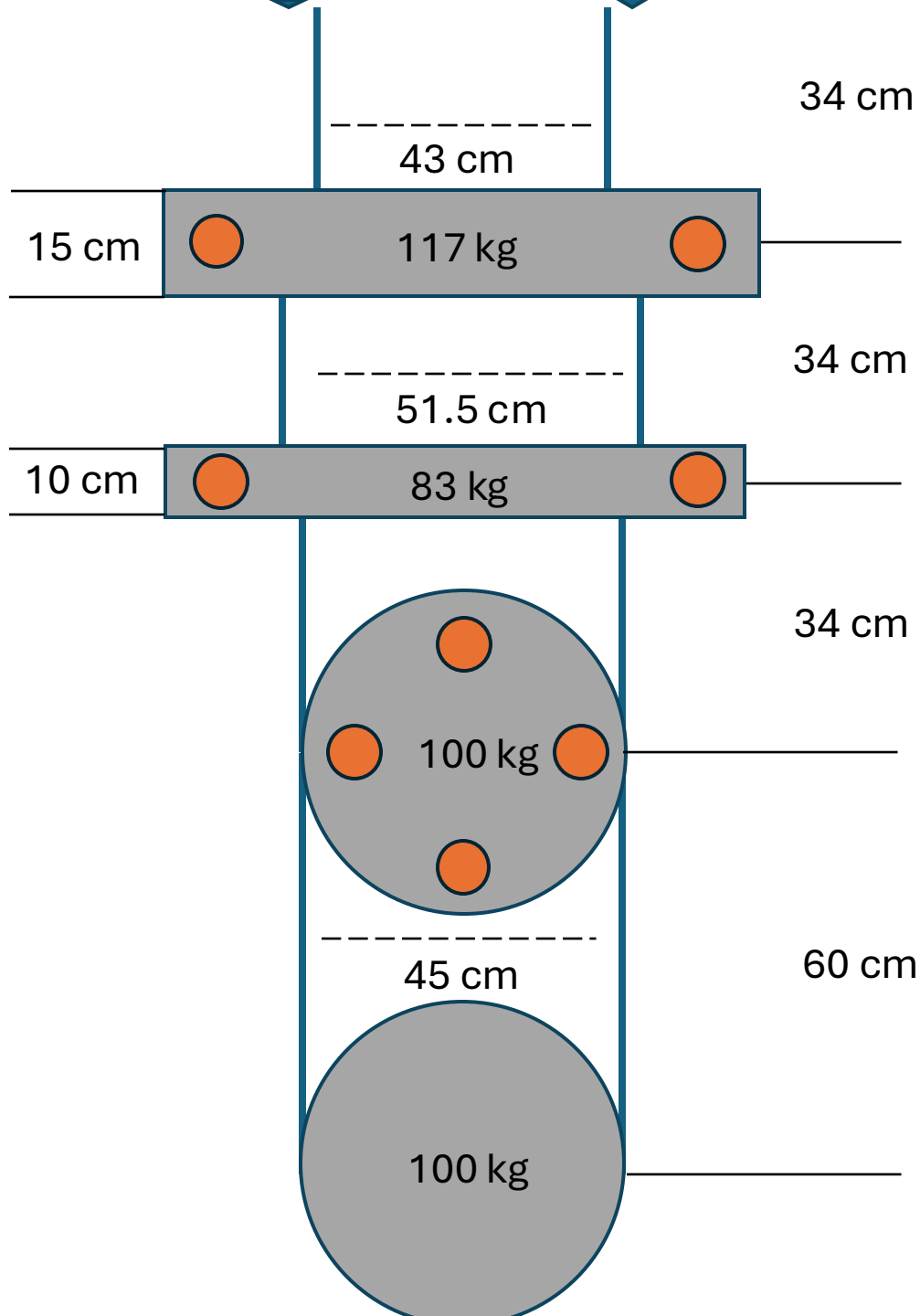


PUM (top view)

Beam tube direction

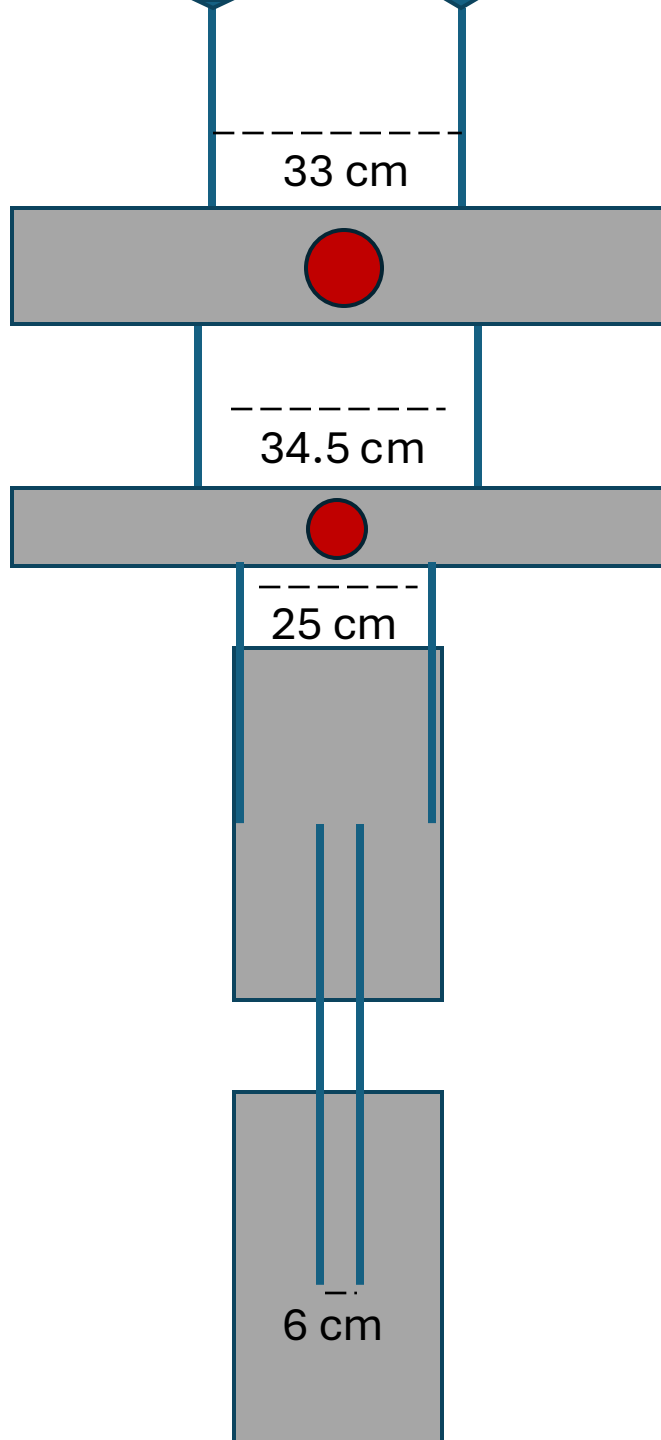


- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)



BHQS (front view)

- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)



BHQS

(side view)

- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)

Design parameters (full)

Symbols	Description	Units	TOP	UIM	PUM	TST
$m_n/m_1/m_2/m_3$	Mass	[kg]	117	83	100	100
$I_{n,x}/I_{1,x}/I_{2,x}/I_{3,x}$	Roll moment of inertia	[kg·m ²]	9.7	5.9	2.6	2.6
$I_{n,y}/I_{1,y}/I_{2,y}/I_{3,y}$	Pitch moment of inertia	[kg·m ²]	10.3	6.3	1.9	1.9
$I_{n,z}/I_{1,z}/I_{2,z}/I_{3,z}$	Yaw moment of inertia	[kg·m ²]	17.6	10	1.9	1.9
$I_{n,xy}/I_{1,xy}/I_{2,xy}/I_{3,xy}$	R-P cross moment of inertia	[kg·m ²]	0	0	0	0
$I_{n,yz}/I_{1,yz}/I_{2,yz}/I_{3,yz}$	P-Y cross moment of inertia	[kg·m ²]	0	0	0	0
$I_{n,zx}/I_{1,zx}/I_{2,zx}/I_{3,zx}$	Y-R cross moment of inertia	[kg·m ²]	0	0	0	0
$k_{cn}/k_{c1}/k_{c2}$	Vertical spring stiffness (per side)	[kN/m]	6.5	9.3	5.2	N/A
$k_{xn}/k_{x1}/k_{x2}$	Lateral spring stiffness (per side)	[kN/m]	2500	2600	2200	N/A
$Y_n/Y_1/Y_2/Y_3$	Young's moduli of wires	[GPa]	212	212	212	72
$l_n/l_1/l_2/l_3$	Stretched wire length	[m]	0.34	0.34	0.34	0.60
$r_n/r_1/r_2/r_3$	radii of wires	[μm]	1400	1200	1000	220
$d_{top}/d_n/d_1/d_3$	(upper) wire vertical attachment distance	[mm]	0	0	0	0
$d_m/d_0/d_2/d_4$	(lower) wire vertical attachment distance	[mm]	0	0	0	0
$s_n/s_u/s_i/s_l$	front-back wire attachment distance	[cm]	16.5	17	12.5	2.95
$n_{n0}/n_0/n_2/n_4$	(upper) wire transverse attachment distance	[cm]	21.6	25.7	22.5	22.5
$n_{n1}/n_1/n_3/n_5$	(lower) wire transverse attachment distance	[cm]	21.6	25.7	22.5	22.5

Design parameters (full)

Description	Units	ST2	TOP	UIM
Length	[cm]	44.0	28.5	28.5
Width	[cm]	22.0	14.2	14.2
Thickness	[mm]	3.4	2.9	2.4
Stress	[MPa]	1000	1000	1000
Deflection	[cm]	23.8	22.0	24.0
Radius of curvature	[cm]	31.6	26	22.8
Internal mode	[Hz]	74	80.1	73.5

Blade Springs:

These were changed in Dec 2023 so the TOP|UIM fit within 1 square meter.

It makes the vertical plant stiffer.

[G2302370](#)

Fiber stress: 1.6 Gpa - [Double that of Advanced LIGO]

Thin radius: 220 μm

Thick radius: 650 μm - [For nulling thermoelastic]

Nulling length: 4 mm - [On each end]

Design parameters (Simplified)

Symbols	Description	Units	TOP	UIM	PUM	TST
L	Distance to the previous stage	[cm]	34	34	34	60
m	Mass of the stage	[kg]	117	83	100	100
I_{RR}	Stage moment of inertia (Roll)	[kg·m ²]	9.7	5.9	2.6	2.6
I_{PP}	Stage moment of inertia (Pitch)	[kg·m ²]	10.3	6.3	1.9	1.9
I_{YY}	Stage moment of inertia (Yaw)	[kg·m ²]	17.6	10	1.9	1.9
k_L	Longitudinal stiffness above stage	[kN/m]	11.5	8.1	5.7	1.6
k_T	Transverse stiffness above stage	[kN/m]	11.5	8.1	5.7	1.6
k_V	Vertical stiffness above stage	[kN/m]	13	18.6	11	84.9
k_R	Roll rotational stiffness above stage	[N·m]	610	1200	560	4300
k_P	Pitch rotational stiffness above stage	[N·m]	355	550	170	74
k_Y	Yaw rotational stiffness above stage	[N·m]	852	785	380	84

Design parameters (Simplified)

Degree of freedom	Units	f_1	f_2	f_3	f_4
Longitudinal	[Hz]	0.45	0.96	1.7	2.6
Transverse	[Hz]	0.45	0.96	1.7	2.6
Vertical	[Hz]	0.67	1.91	3.6	6.7
Roll	[Hz]	0.77	1.86	3.3	9.4
Pitch	[Hz]	0.55	0.93	1.77	2.23
Yaw	[Hz]	0.68	1.05	1.86	2.72

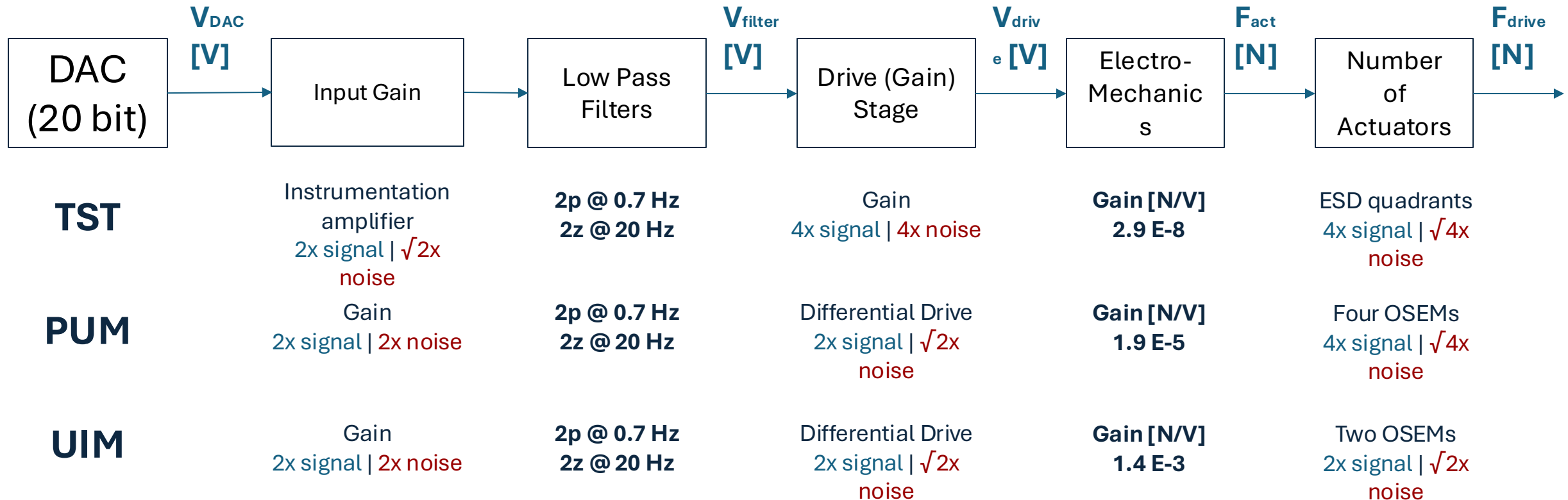
Bounce and roll
recalculated to account
for fiber nulling region
[4 cm on each side]

LSC | ASC loops

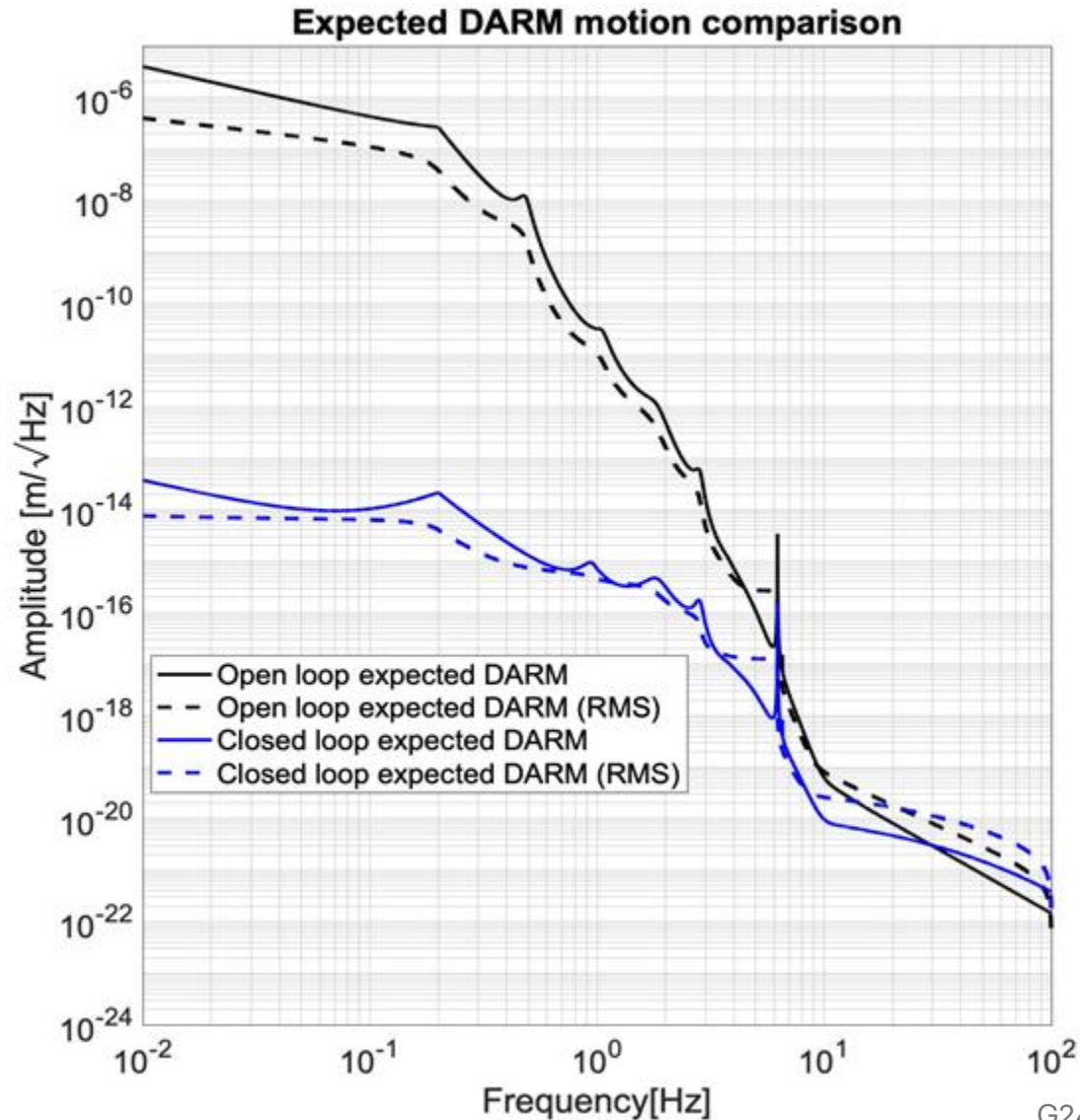
LSC Loops



Full strawman design: [G2401425](#)



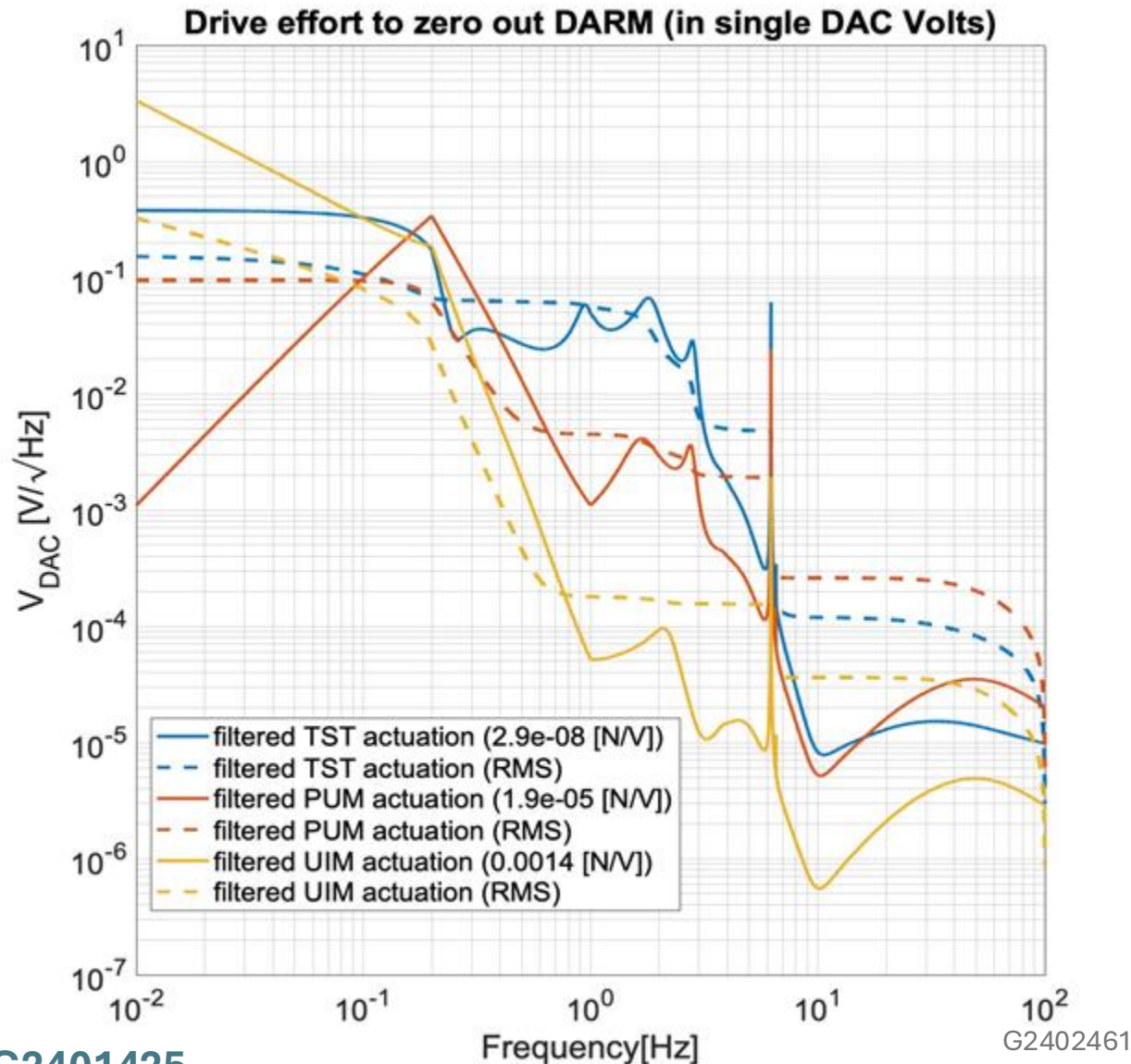
LSC Loops



Strawman controller performance

- 70 Hz unity gain frequency.
- Conditionally stable (but that's ok)
- 10^{-14} m RMS in closed loop (as required)

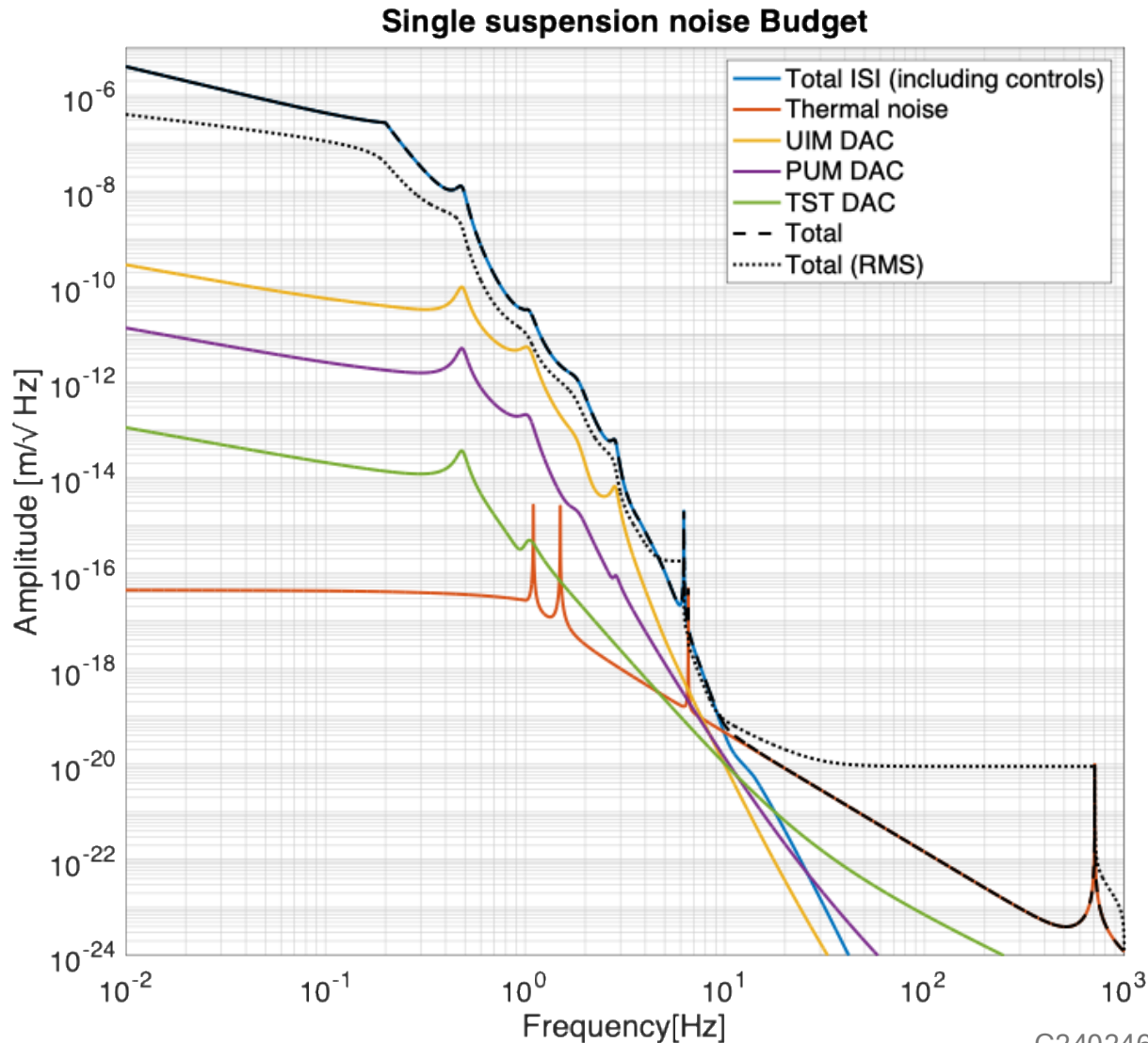
LSC Loops



Strawman controller performance

- 70 Hz unity gain frequency.
- Conditionally stable (but that's ok)
- 10^{-14} m RMS in closed loop (as required)
- The drive effort is distributed among the UIM, PUM and TST stages.
- The RMS voltage for all three does not exceed 1 V.

LSC Loops



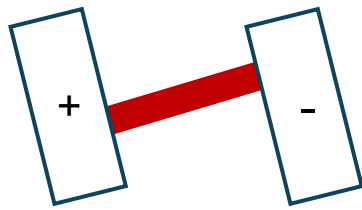
Strawman controller performance

- 70 Hz unity gain frequency.
- Conditionally stable (but that's ok)
- 10^{-14} m RMS in closed loop (as required)
- The drive effort is distributed among the UIM, PUM and TST stages.
 - The RMS voltage for all three does not exceed 1 V.
- The DAC noise is consistently 5x below the ISI+Thermal noise contribution above 4 Hz.

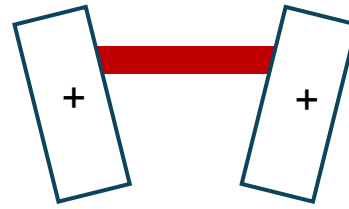
ASC loops

ASC Loops

- They are actuated from the PUM in the hard/soft basis



Hard DOF



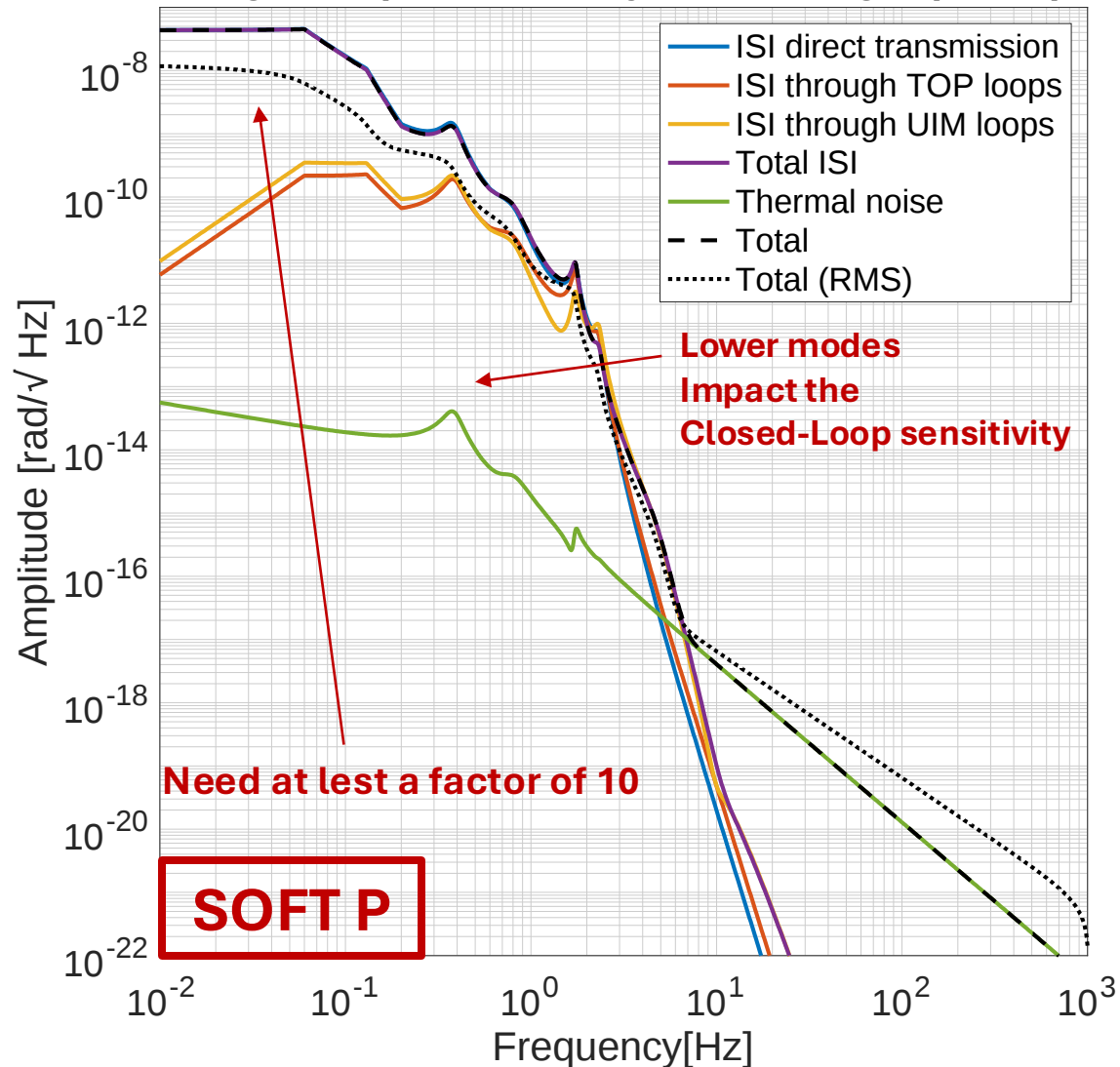
Soft DOF

- We assume a WFS noise of $1\text{e-}15 \text{ rad/Hz}^{1/2}$. Order of magnitude based on [G2100751](#)

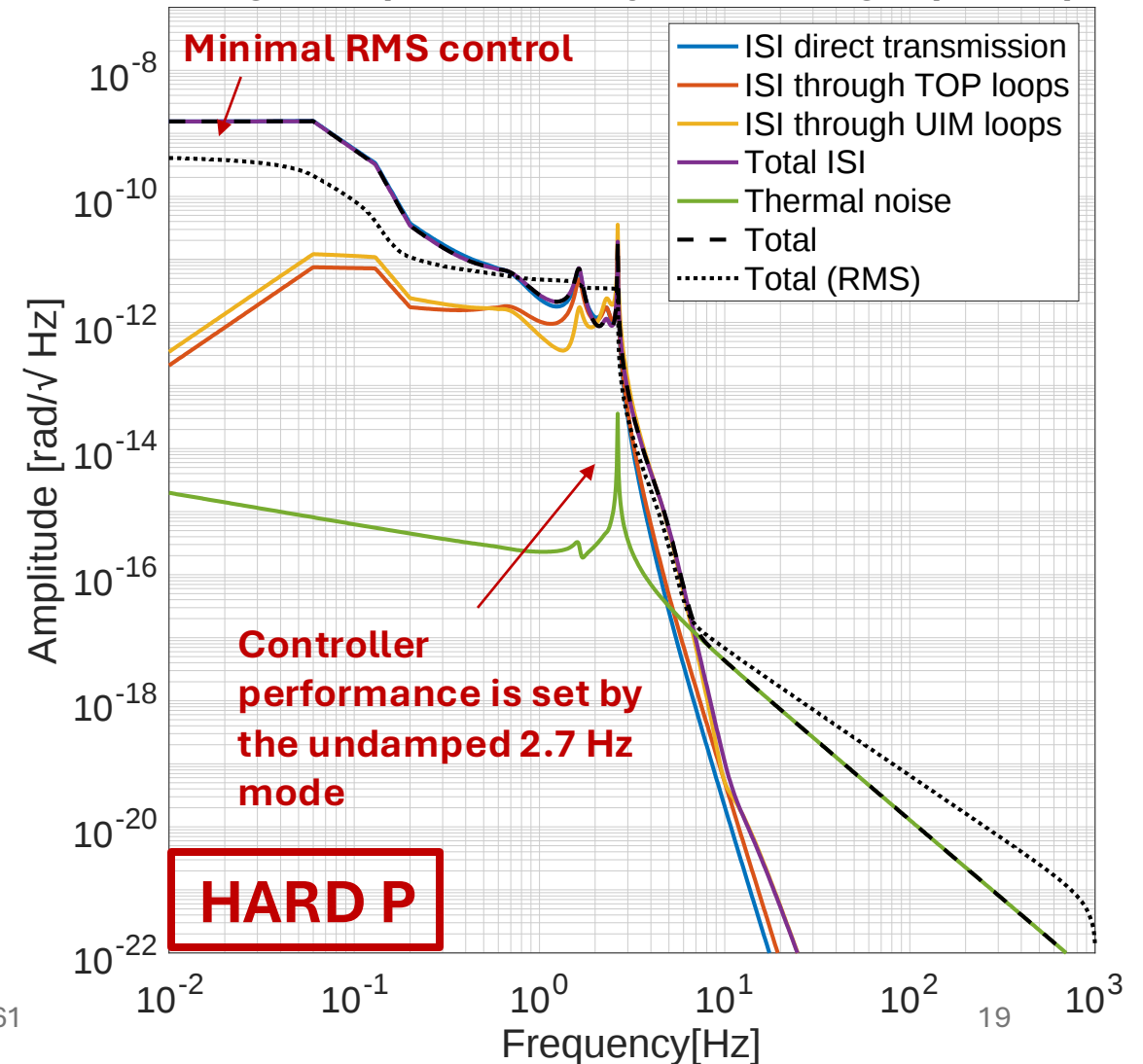
Pitch ASC (1.5 MW):

Open-Loop Motion

Single suspended cavity noise Budget (soft P)

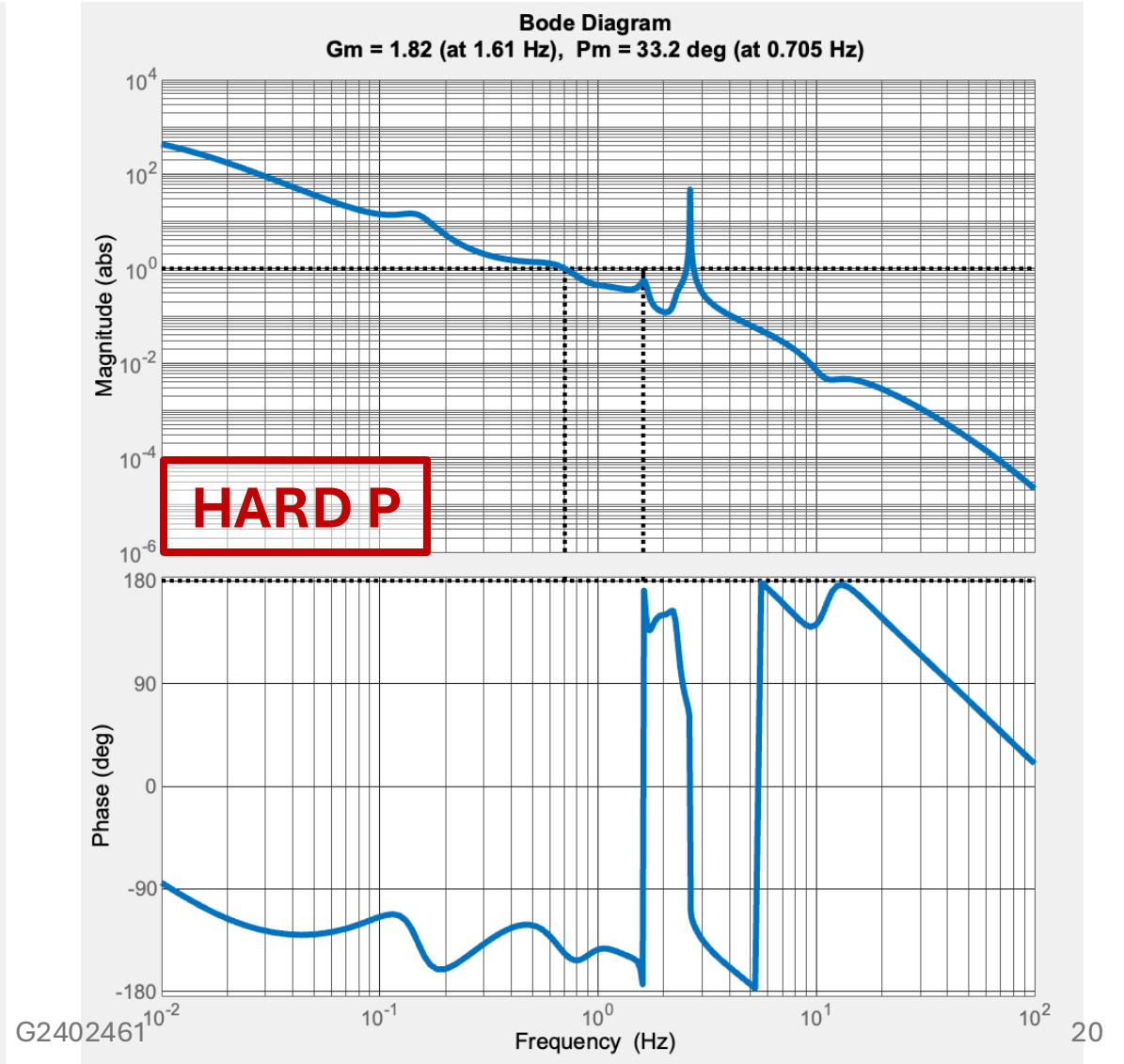
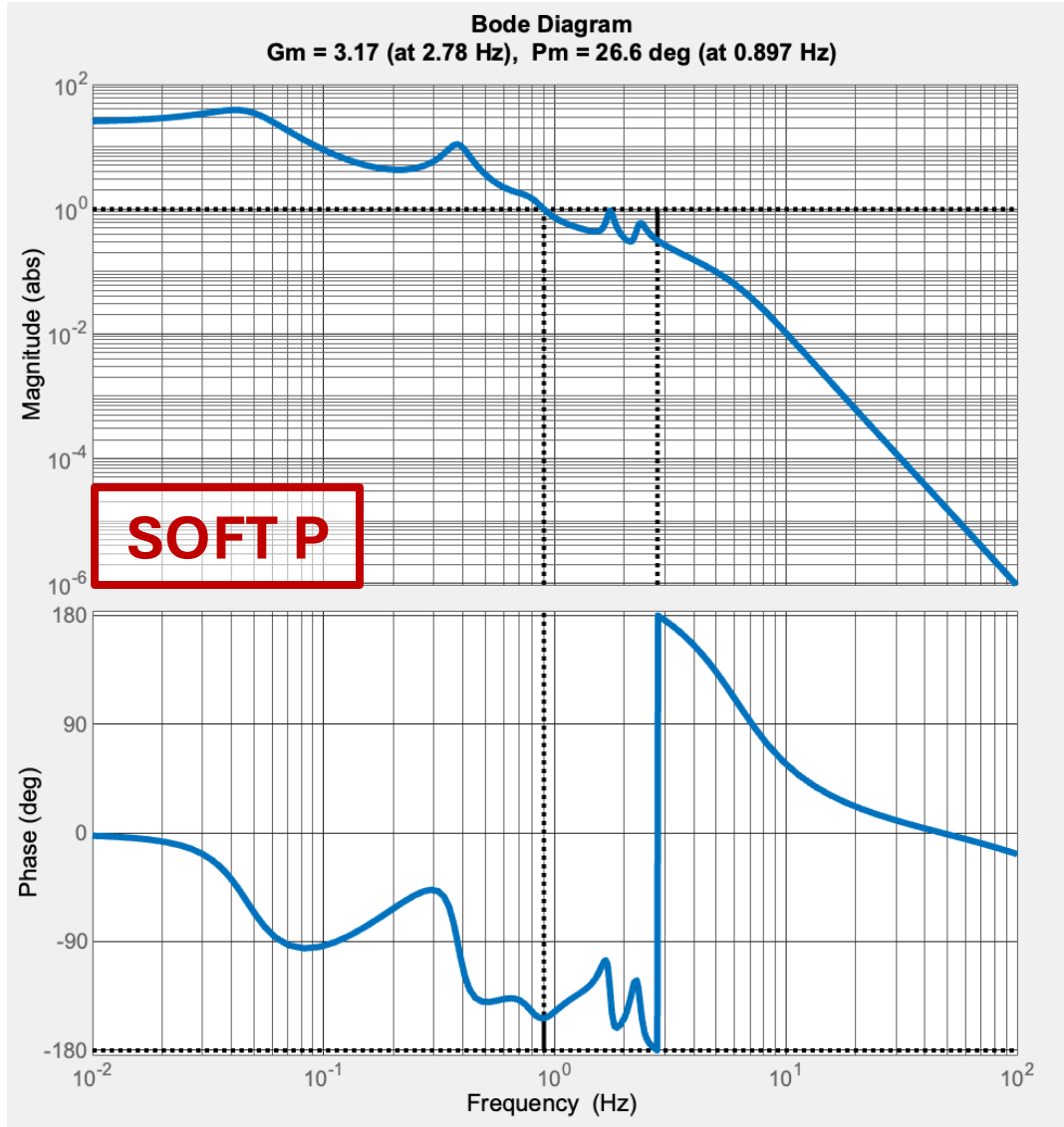


Single suspended cavity noise Budget (hard P)

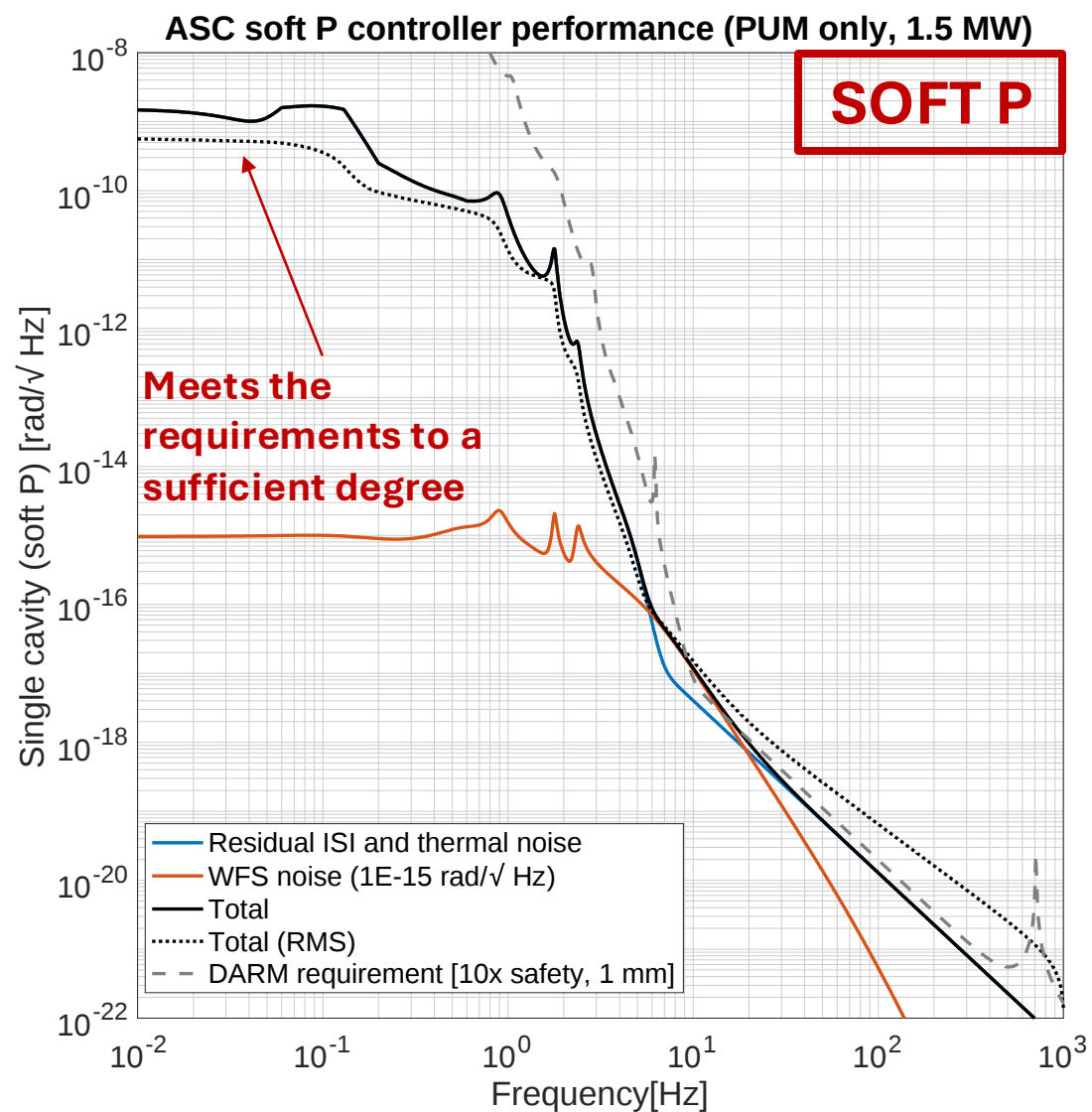


Pitch ASC (1.5 MW):

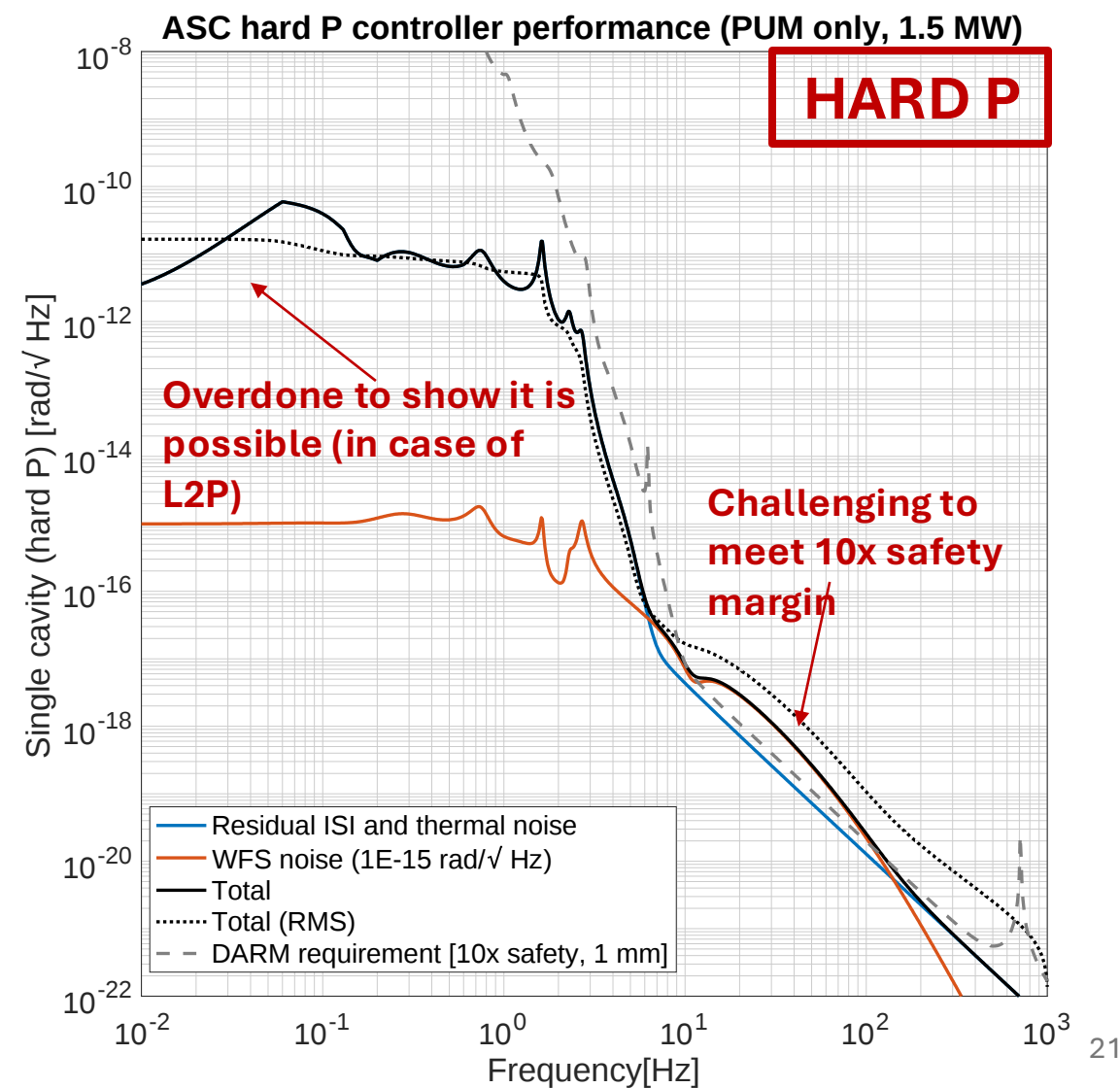
Open-Loop Gains



Pitch ASC (1.5 MW):

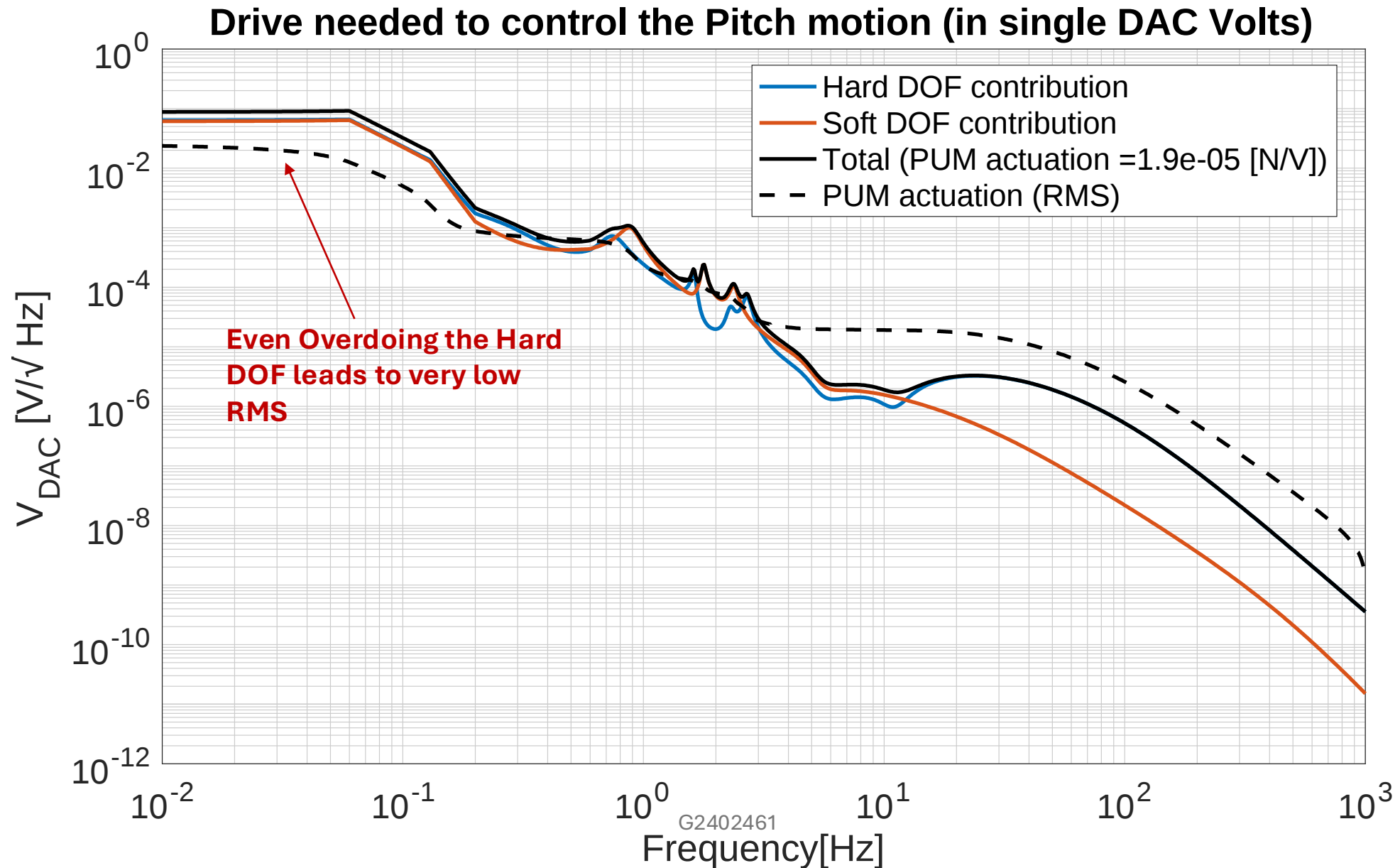


Closed-Loop Motion



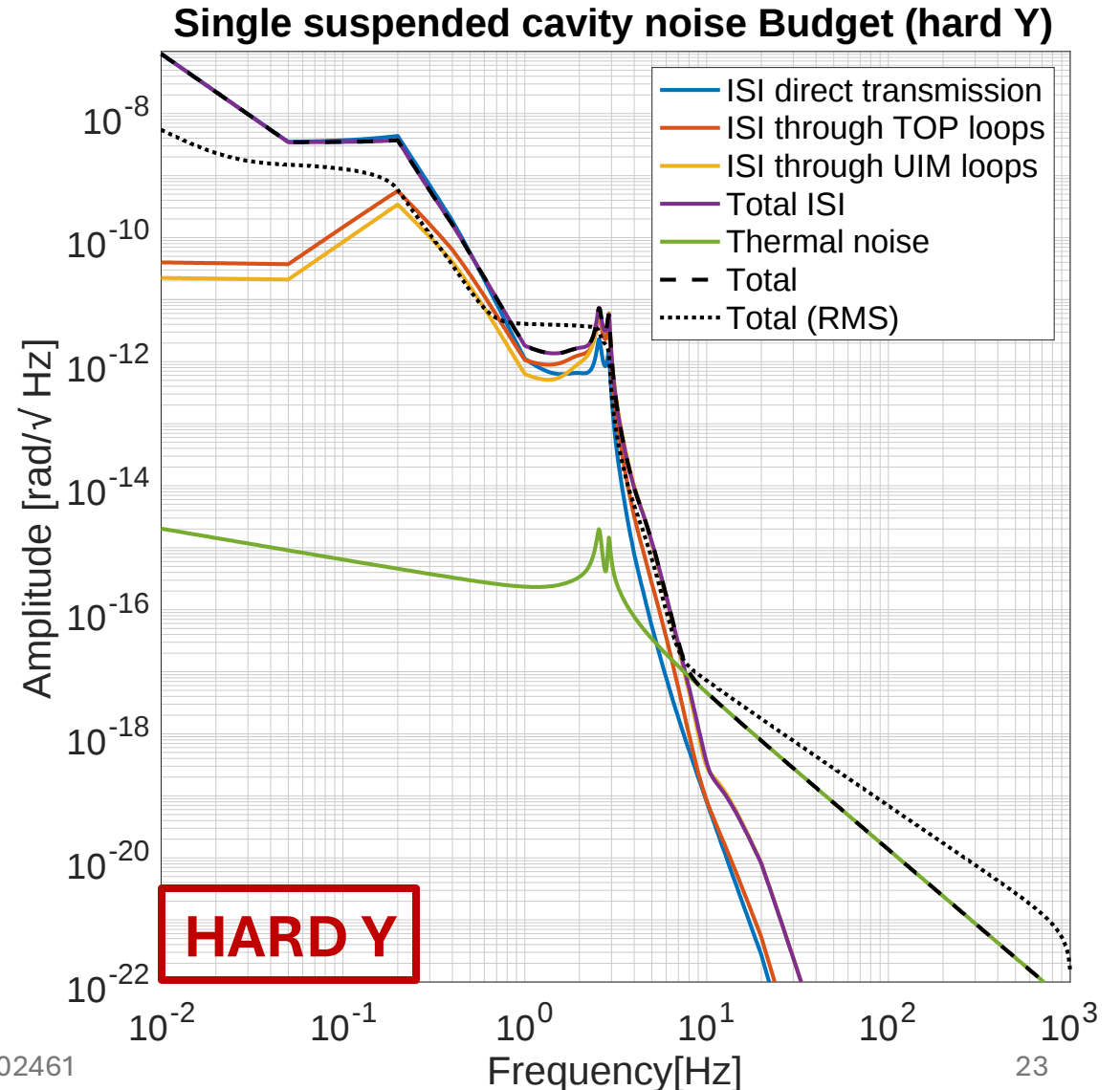
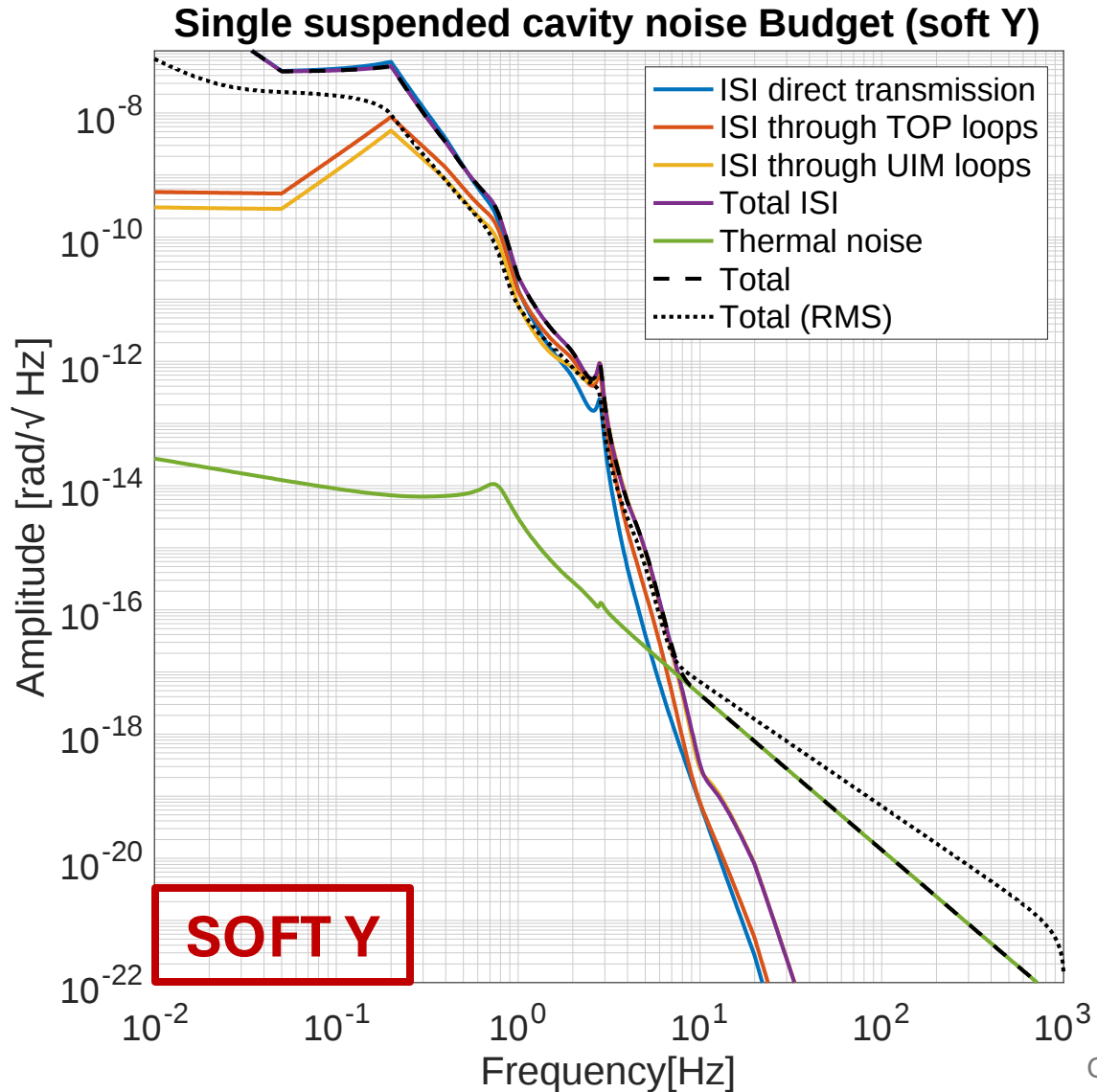
Pitch ASC (1.5 MW):

Upper-Limit DAC volts



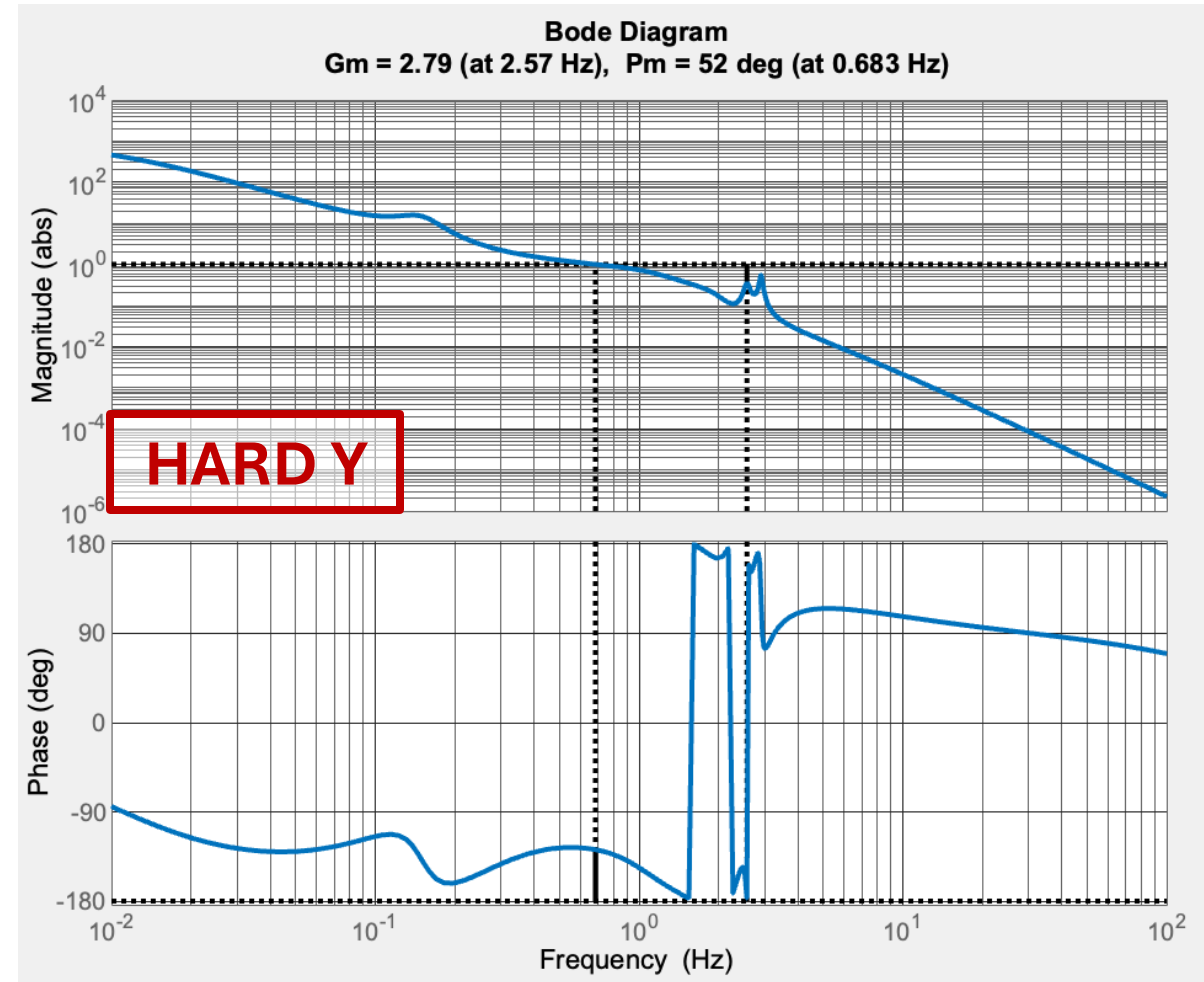
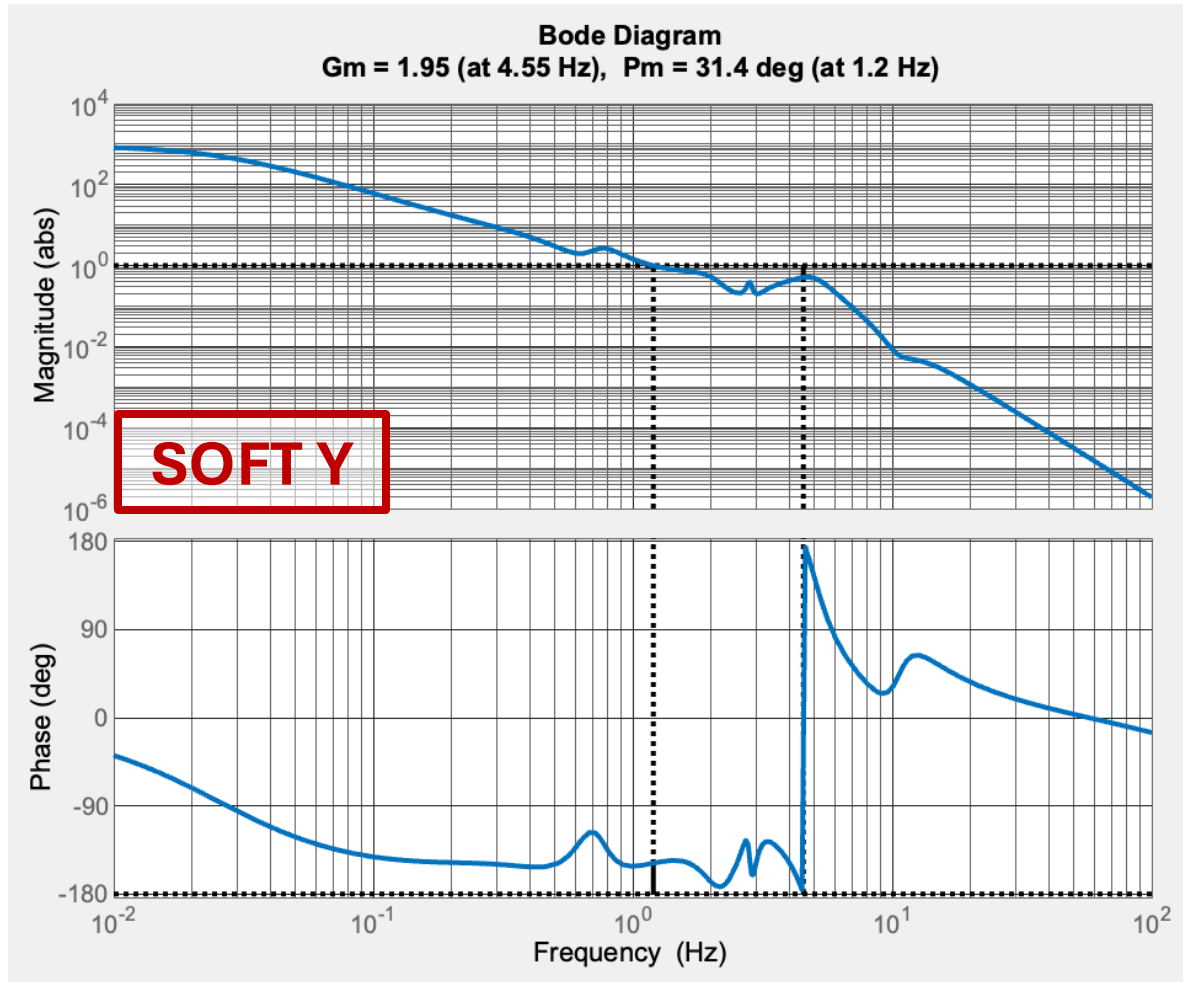
Yaw ASC (1.5 MW):

Open-Loop Motion

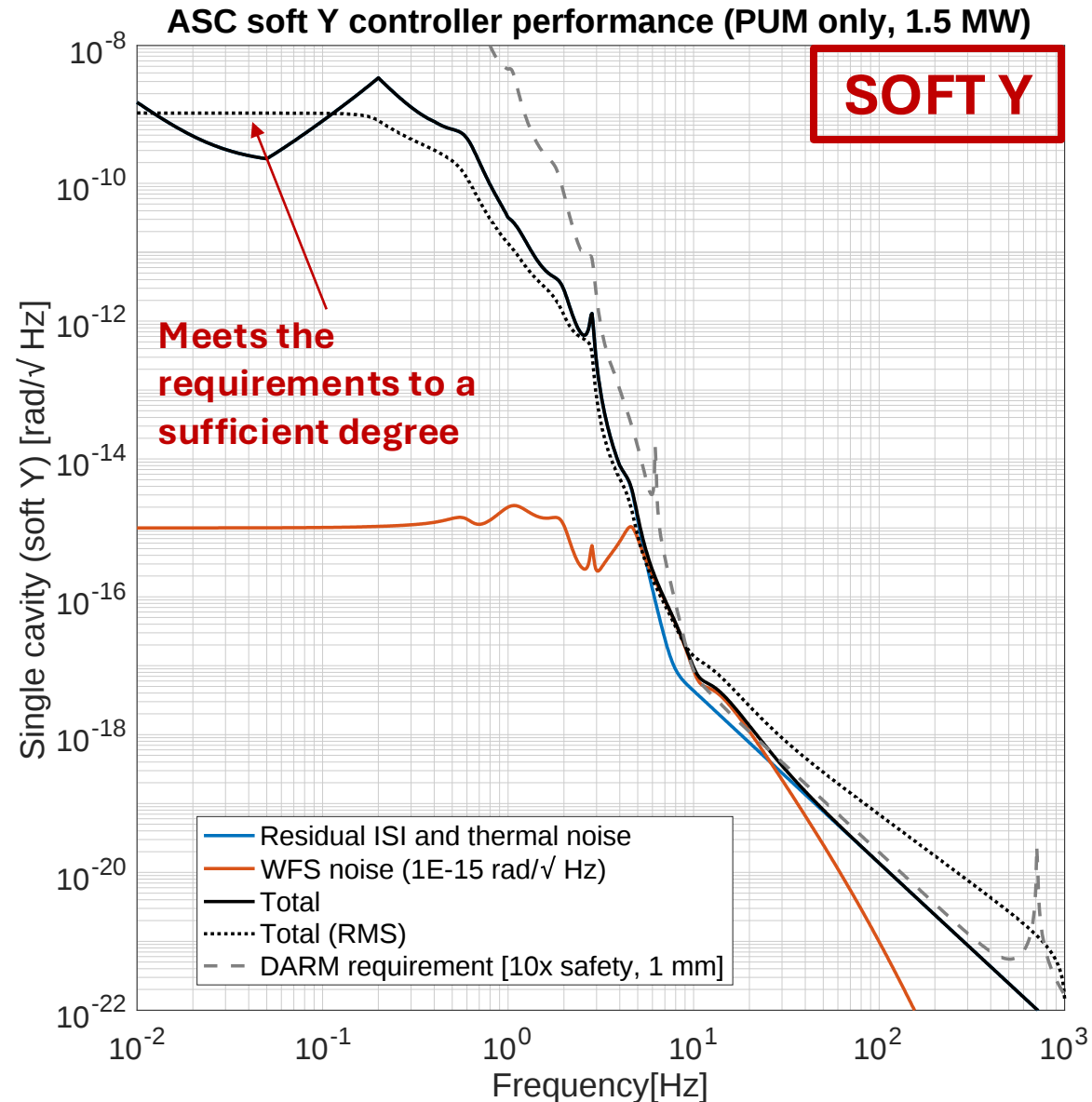


Yaw ASC (1.5 MW):

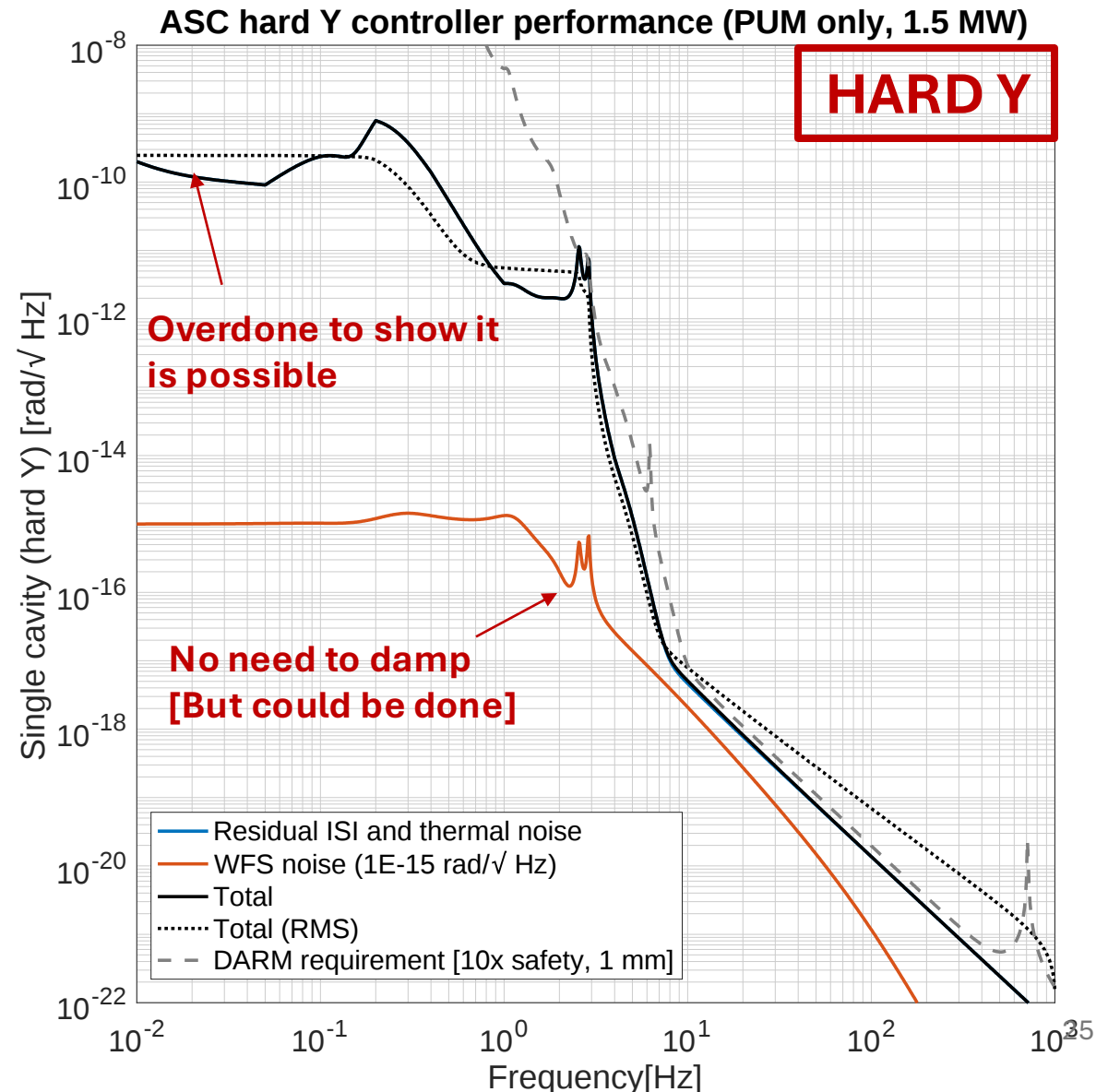
Open-Loop Gains



Yaw ASC (1.5 MW):

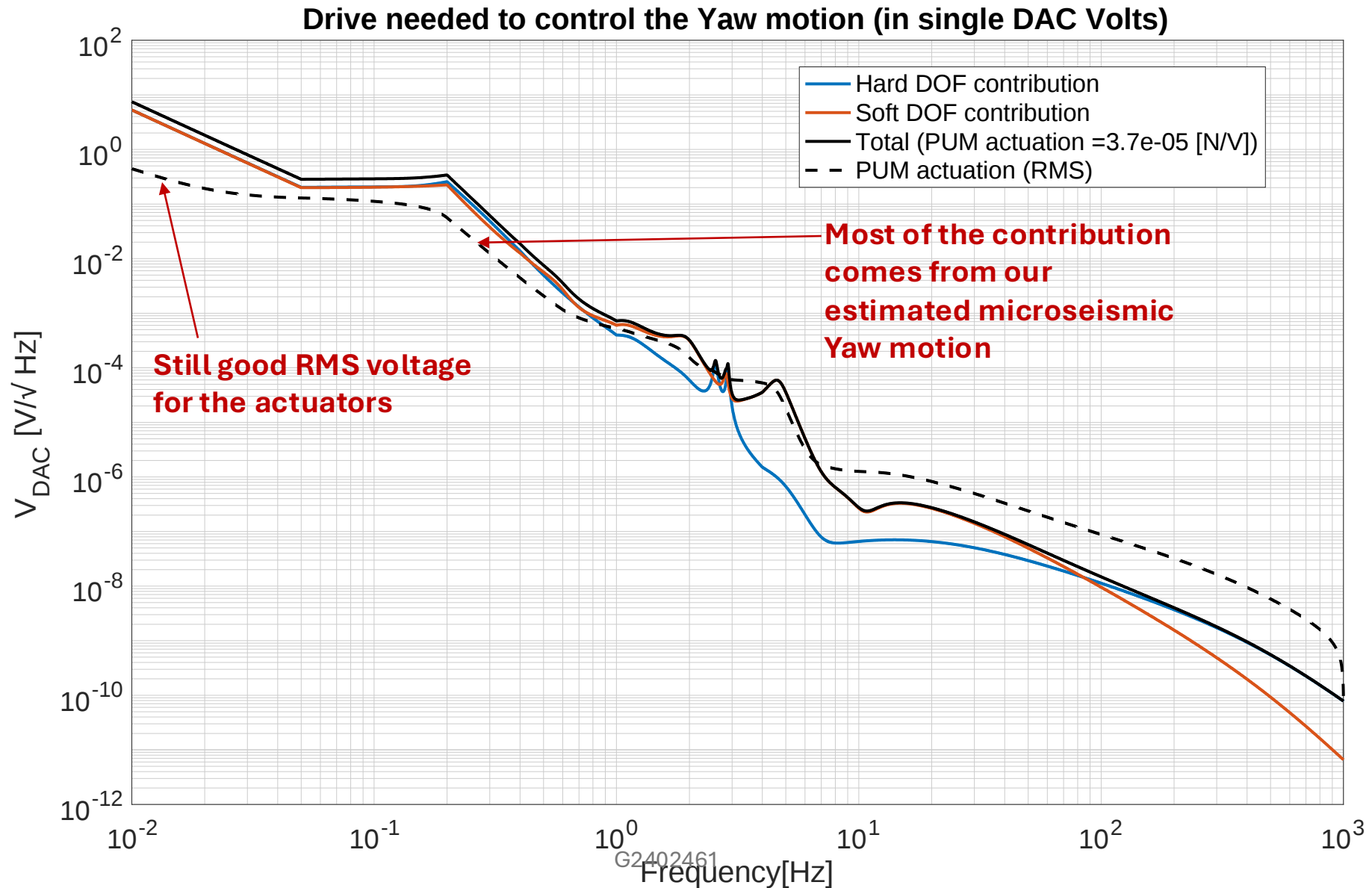


Closed-Loop Motion



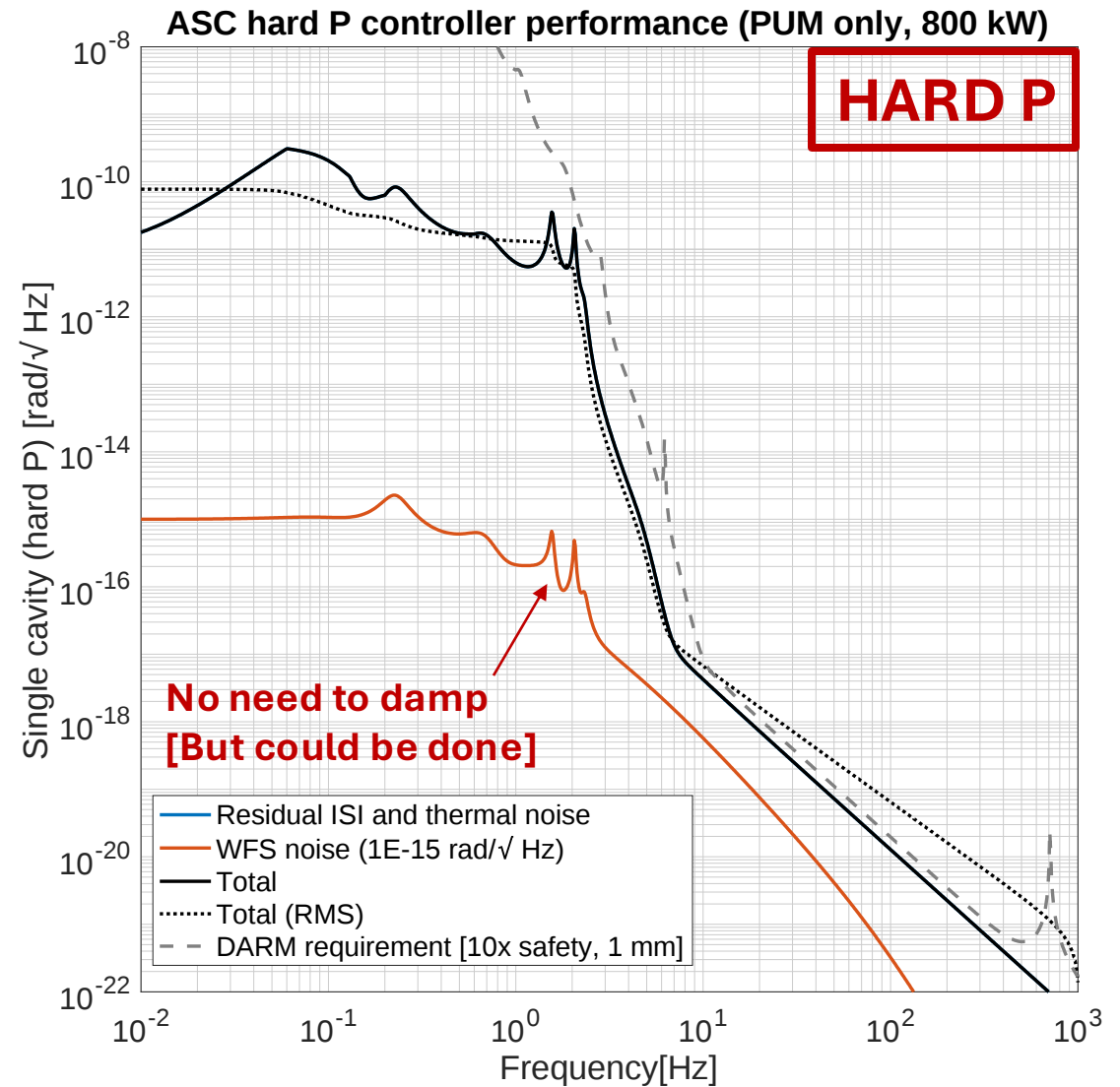
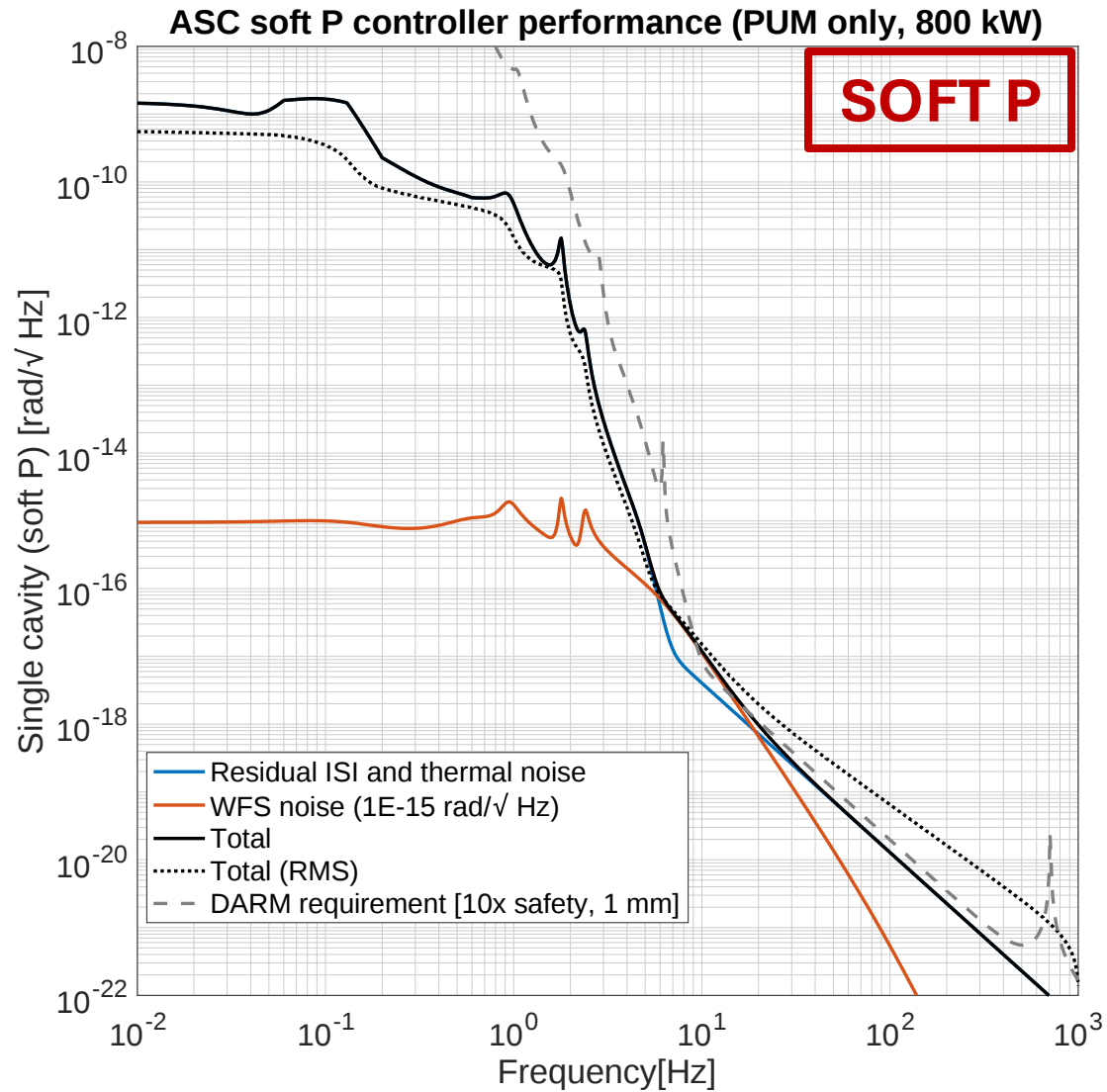
Yaw ASC (1.5 MW):

Upper-Limit DAC volts

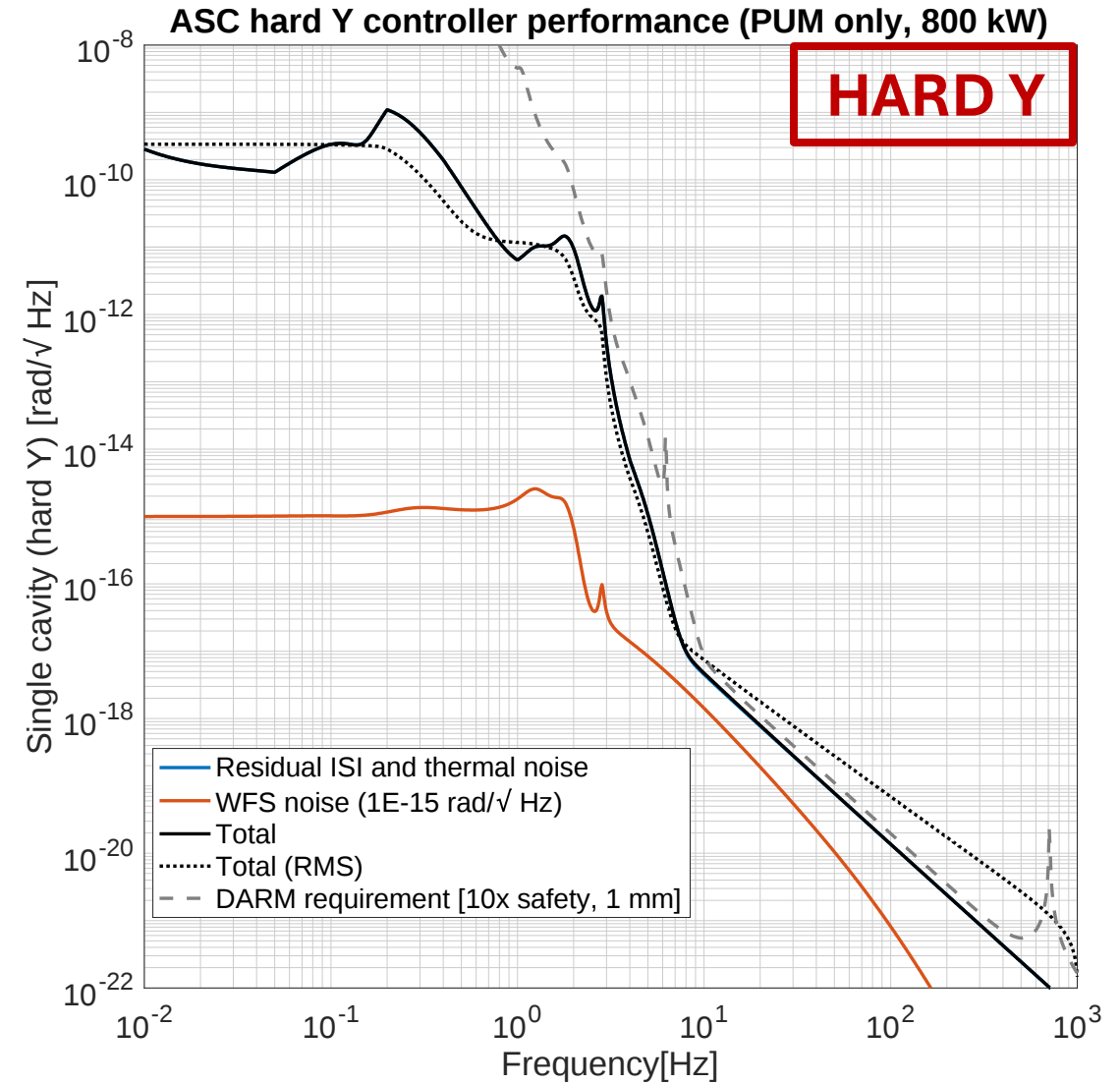
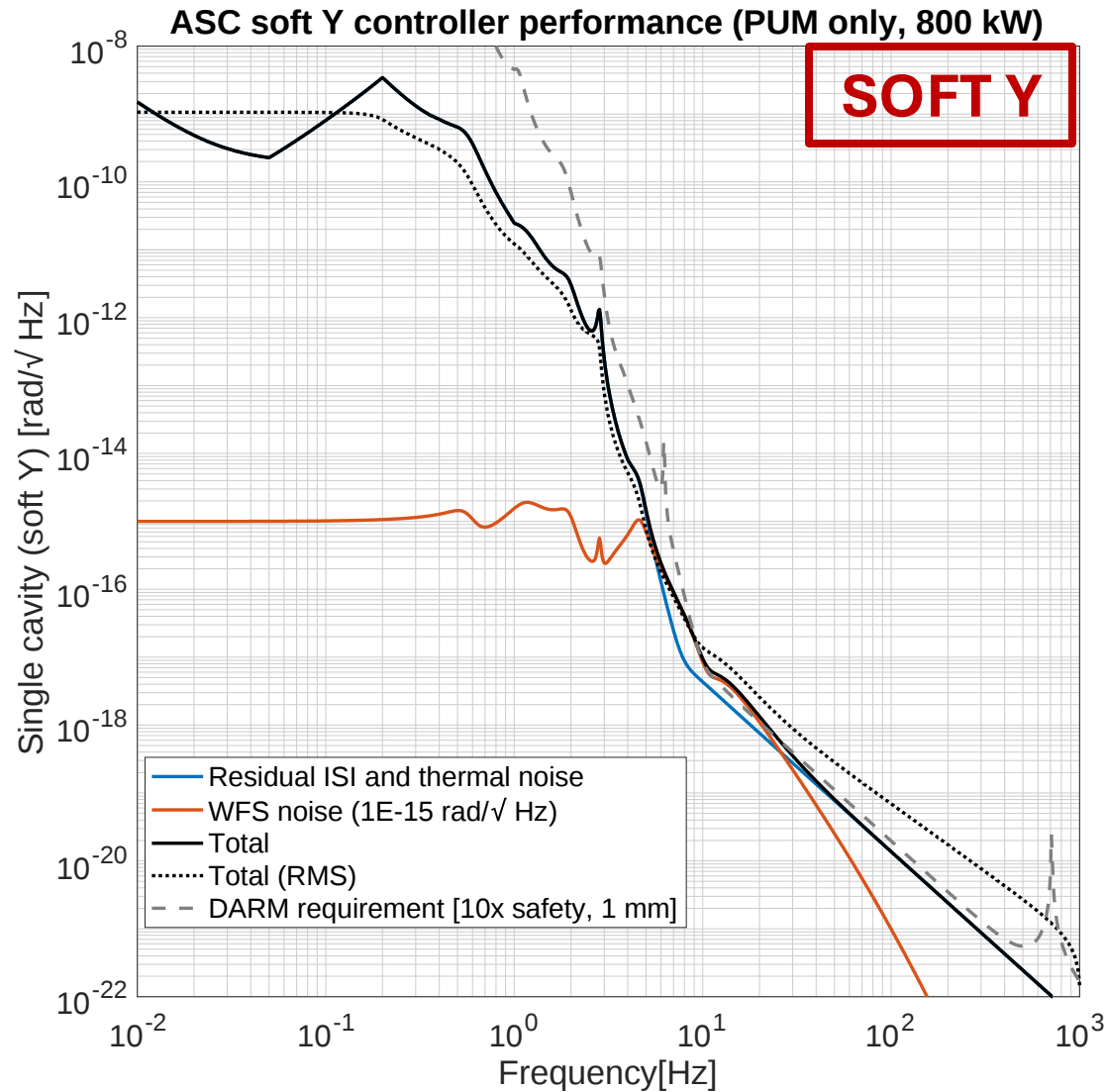


What about ASC at lower powers?

800 kW ASC performance



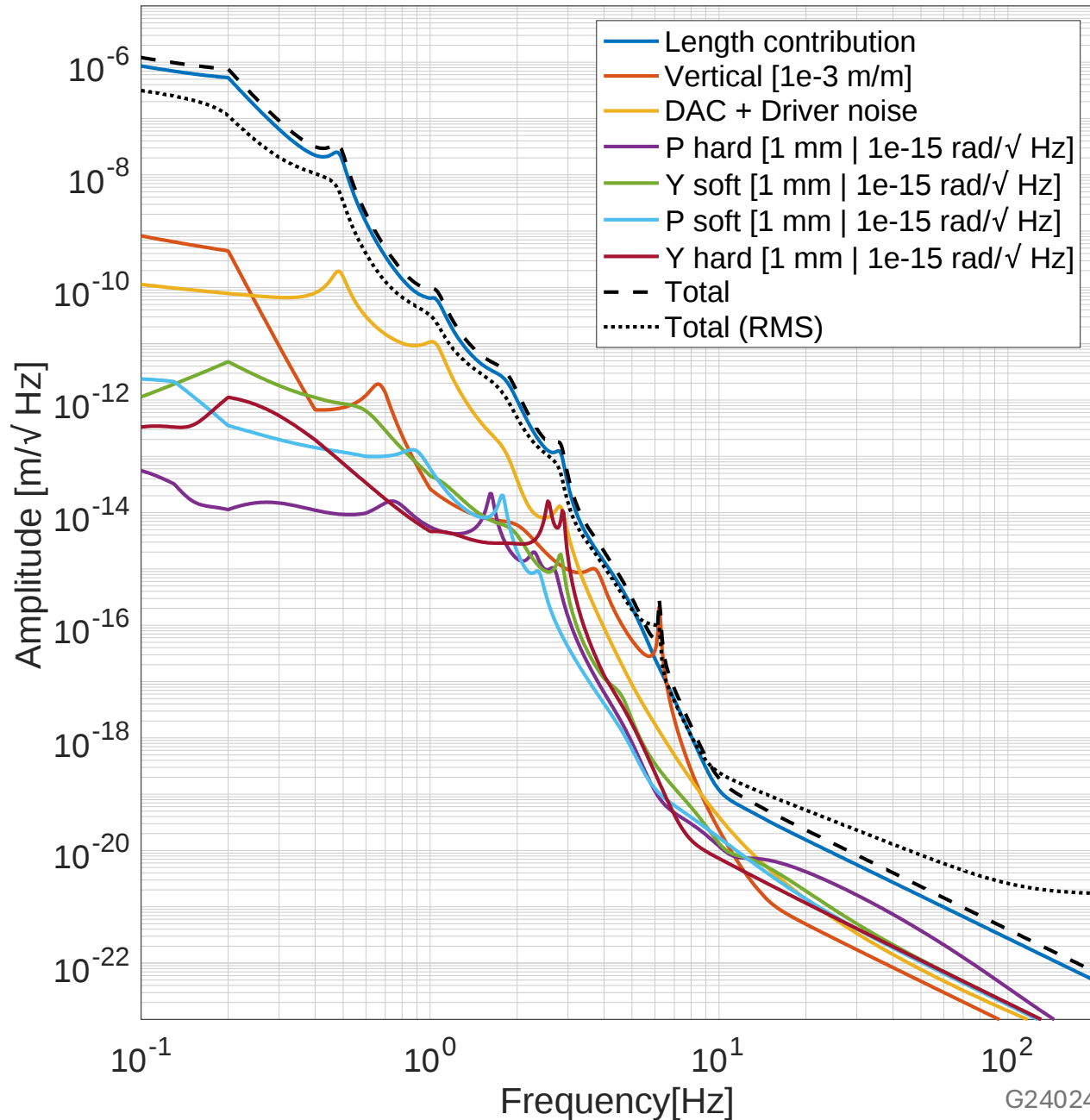
800 kW ASC performance



ASC takeaways (for now)

- At lower powers (less than 1 MW) it should be possible to damp the hard mode locally, simplifying the ASC loops.
- Building a reasonable controller for the well-damped angular plants (< 1 MW) is doable.
- At lower powers, the limiting factor is likely to be our ability to control the soft mode RMS.
- At 1.5 MW we must resort to more complicated controllers to deal with the hard Pitch degree of freedom.

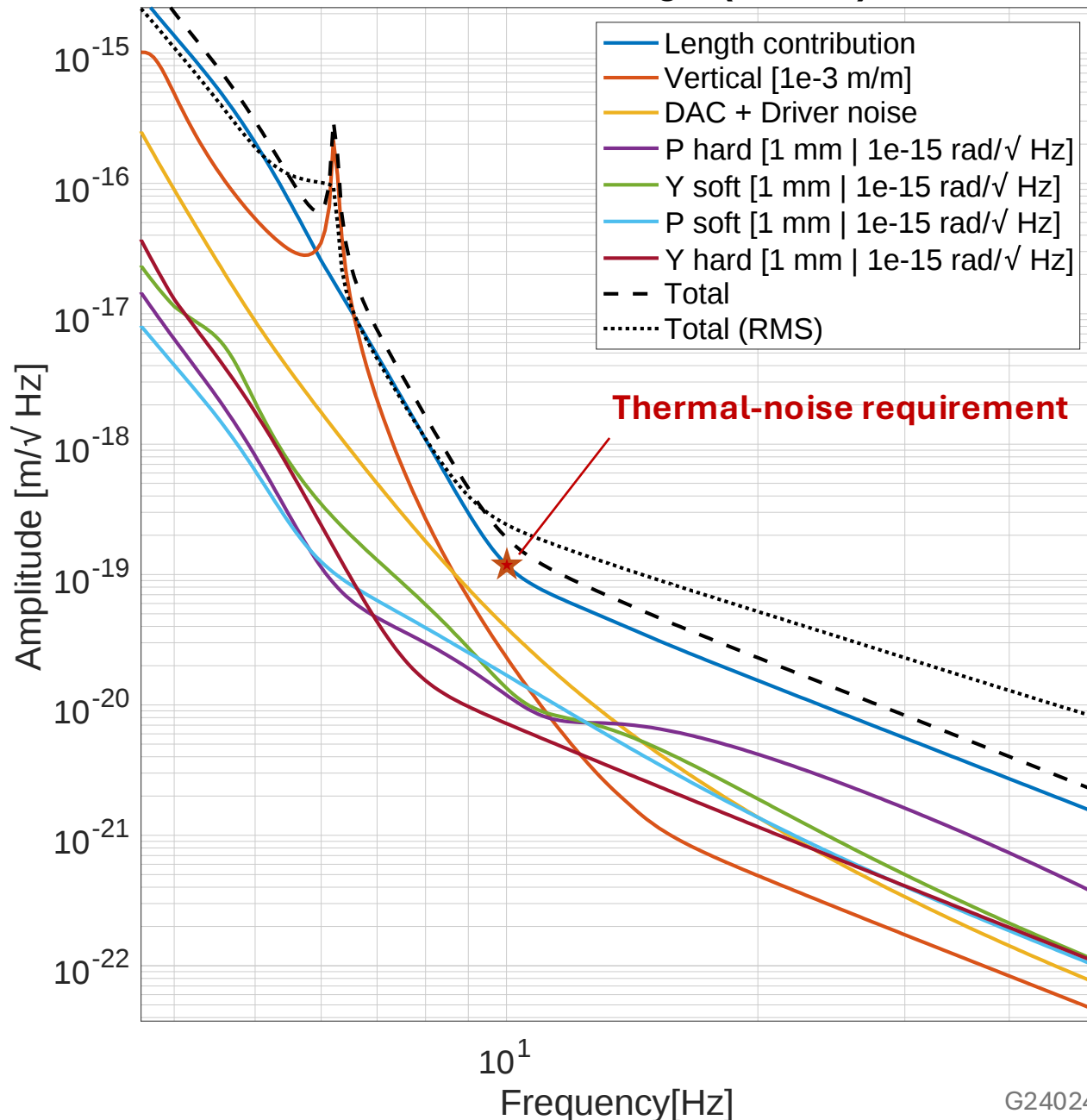
DARM noise Budget (1.5 MW)



Let's put it all together into a noise budget

- The main contributors to the noise that can be mitigated are:
 - The TST stage DAC noise
 - The P hard dof due to the undamped mode
 - The Y hard dof due to the poorly damped mode

DARM noise Budget (1.5 MW)



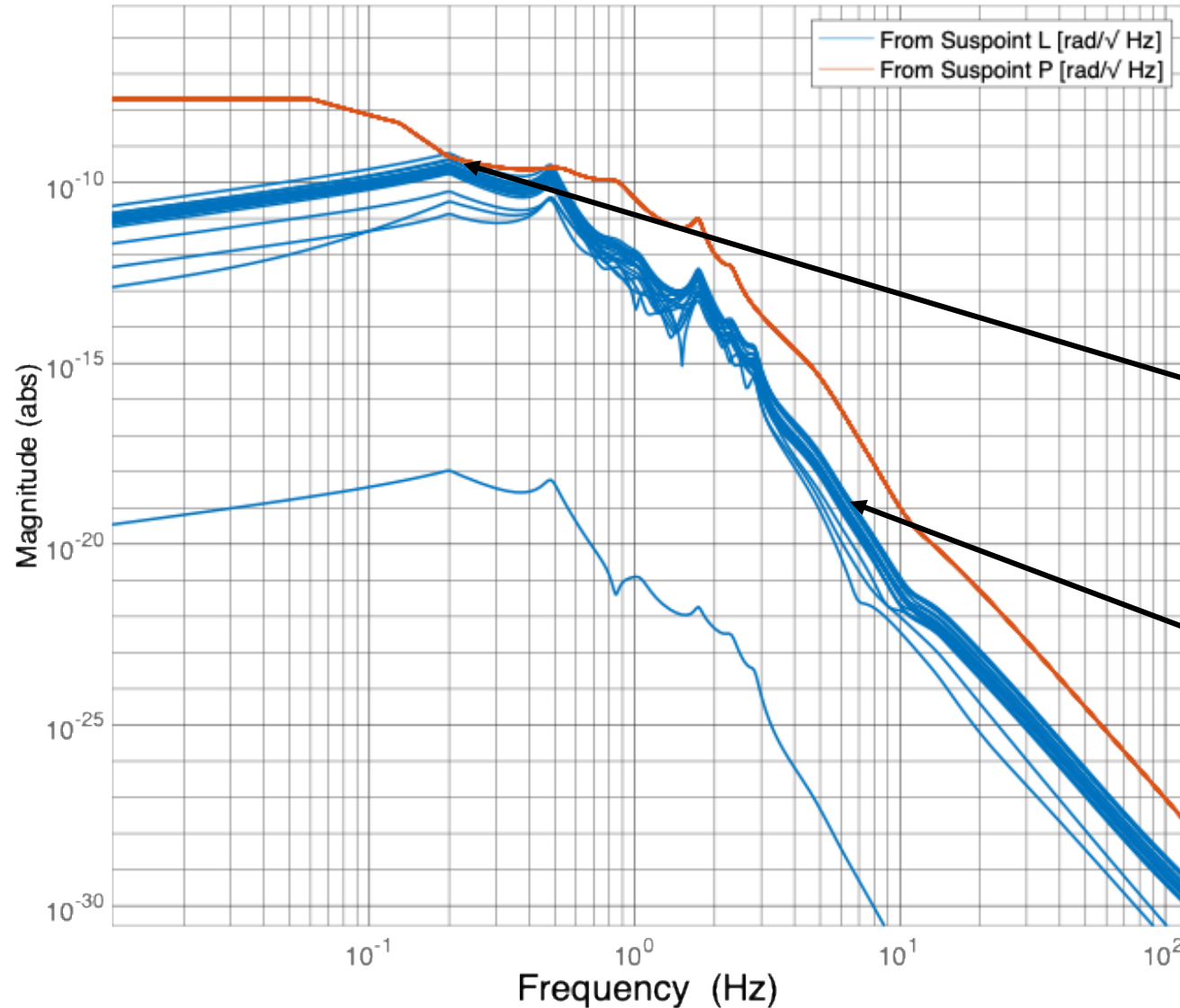
Let's put it all together into a noise budget

- The main contributors to the noise that can be mitigated are:
 - The TST stage DAC noise
 - The P hard dof due to the undamped mode
 - The Y hard dof due to the poorly damped mode
- Note:** This assumes the scenario where the WFS noise is at the $1 \text{ e-15 rad/Hz}^{1/2}$.
- Note:** This assumes the dofs are well damped and decoupled

Caveats

- How much uncertainty can we tolerate on this design?
- Can we reduce the actuator noise?
- How good do the sensors need to be?

Pitch of the TST stage for uncertain d-values unc=250 microns



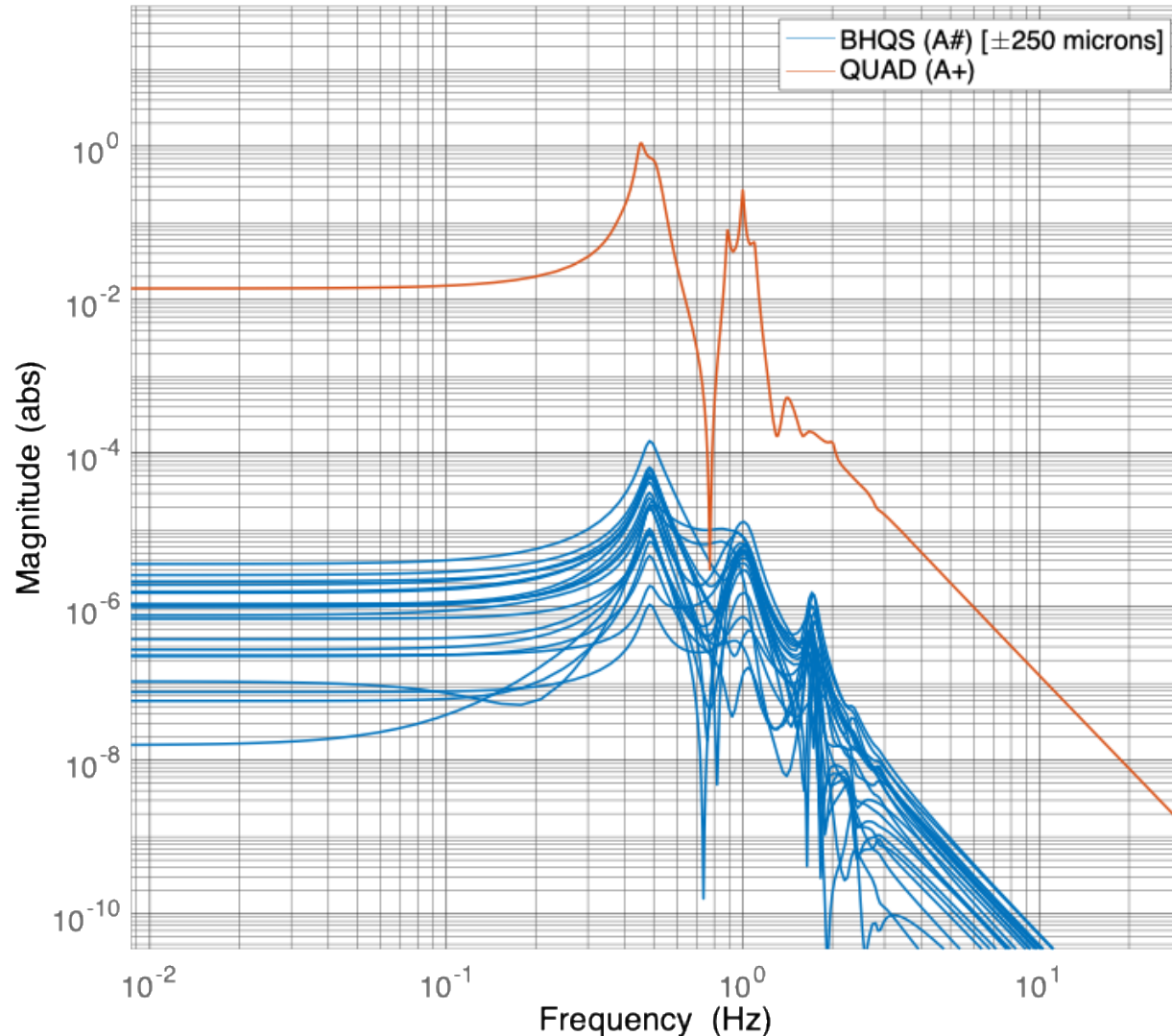
How much uncertainty?

Length-to-pitch cross-coupling From ISI

- 250 μm tolerance is enough to ensure the Length-to-Pitch coupling is lower everywhere except for the microseism.
- The Length-to-Pitch coupling in this case is 100 times lower above the resonances, even when including the Length controls

Percent change on the TST-TST L and P Open Loop Gains for uncertain d-values
unc=250 microns

From: dampedout.tst.disp.L To: dampedout.tst.disp.P



How much uncertainty?

- 250 microns keeps the loop interaction on the 0.01% level.
- 1% is the limit of what we would consider “decoupled” (about 3cm for the BHQS)

In a 2x2 Multi-input / Multi-output system

L2L	P2L
L2P	P2P

the fraction

$$\frac{(L2P)(P2L)}{(L2L)(P2P)}$$

represents the fractional interaction between two **high-gain** Single-input / Single-output loops like the ones used for interferometric controls.

Caveats

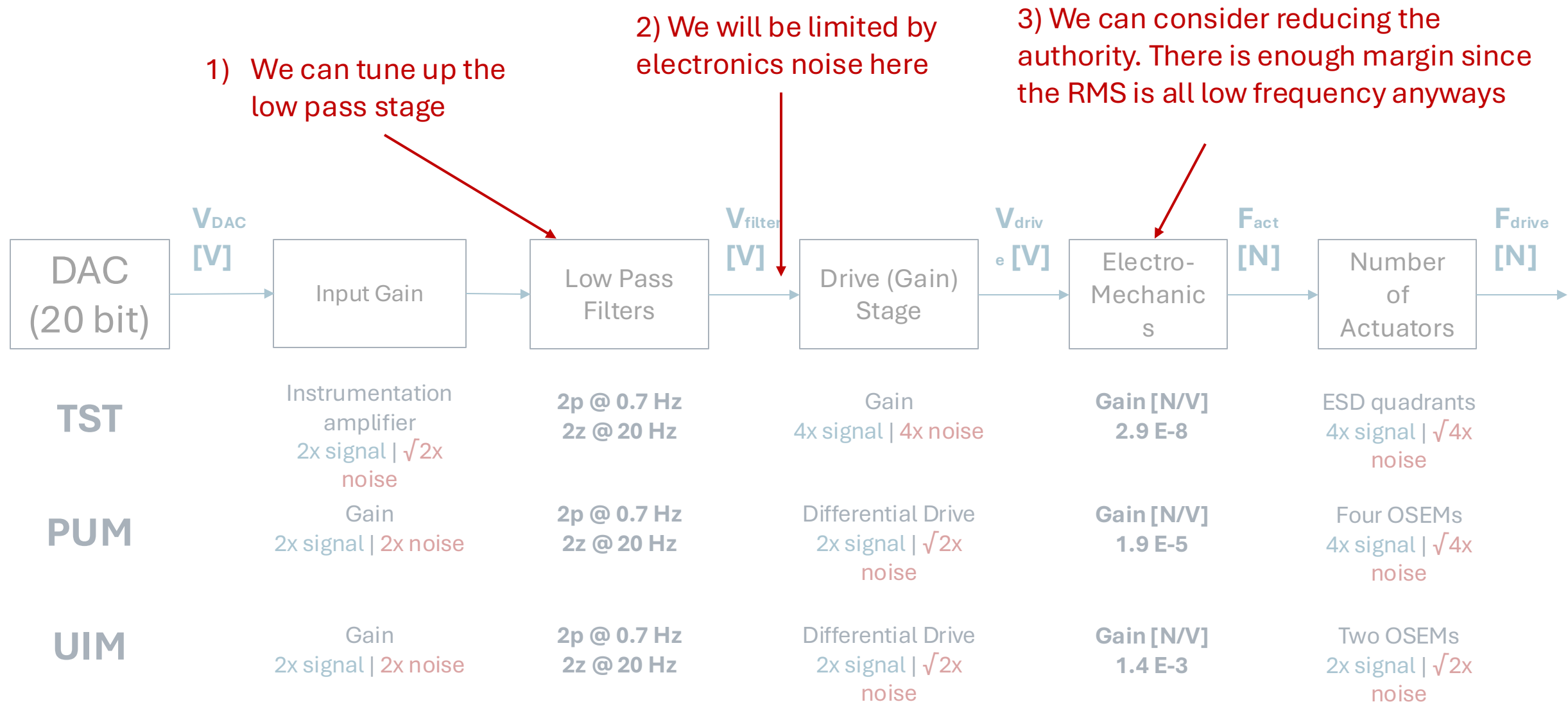
- How much uncertainty can we tolerate on this design?

About 250 microns on the d-values → Limited by microseism

Loop decoupling resists d-value uncertainties of at least 1cm

- Can we reduce the actuator noise?
- How good do the sensors need to be?

About the actuator noise



Caveats

- How much uncertainty can we tolerate on this design?

About 250 microns on the d-values → Limited by microseism

Loop decoupling resists d-value uncertainties of at least 1cm

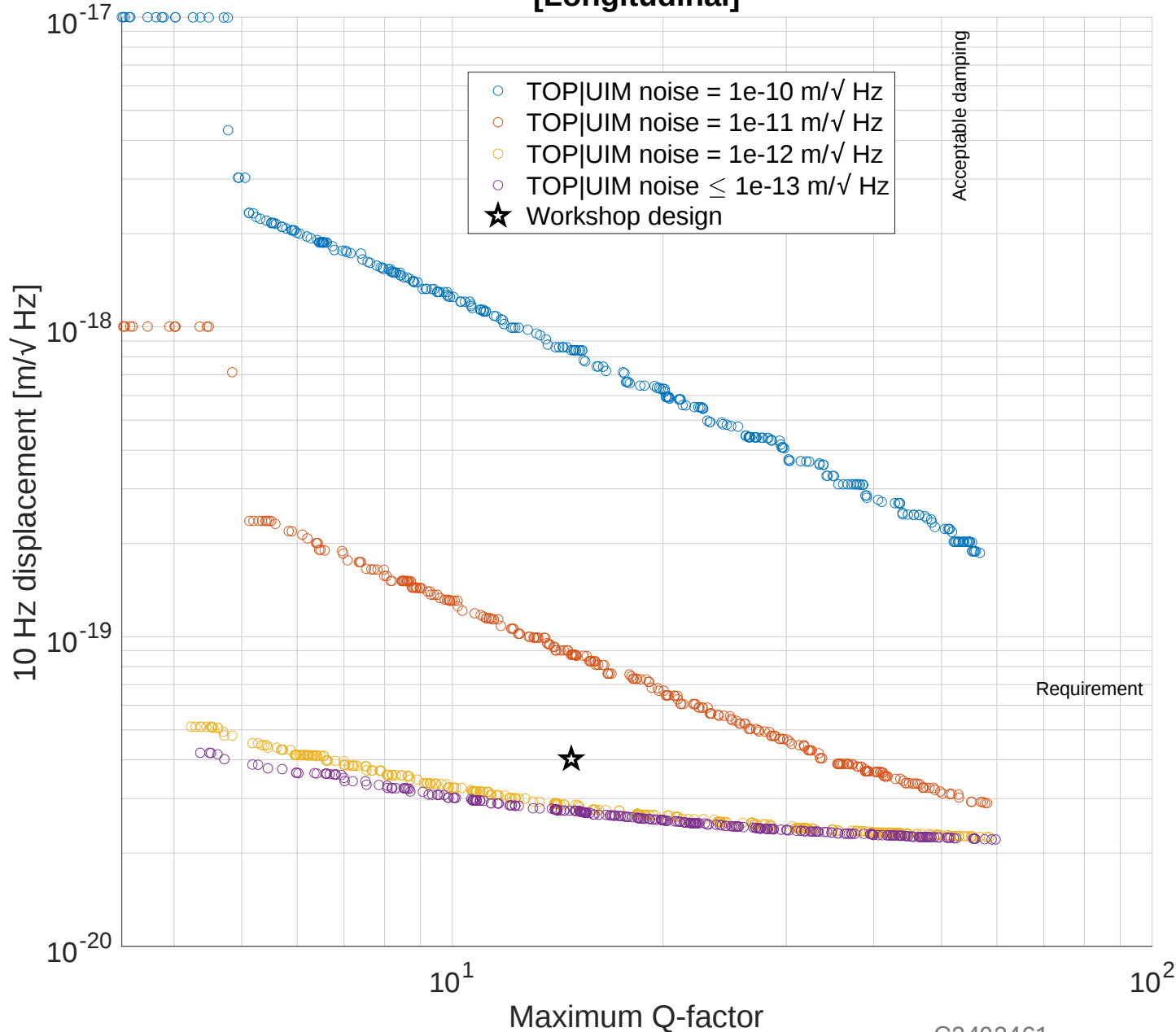
- Can we reduce the actuator noise?

There should be enough margin to reduce the ESD's authority without saturating the DACs

The noise comes from the TST stage, but most of the actuation RMS happens at the UIM.

- How good do the sensors need to be?

Pareto front for local damping [Longitudinal]



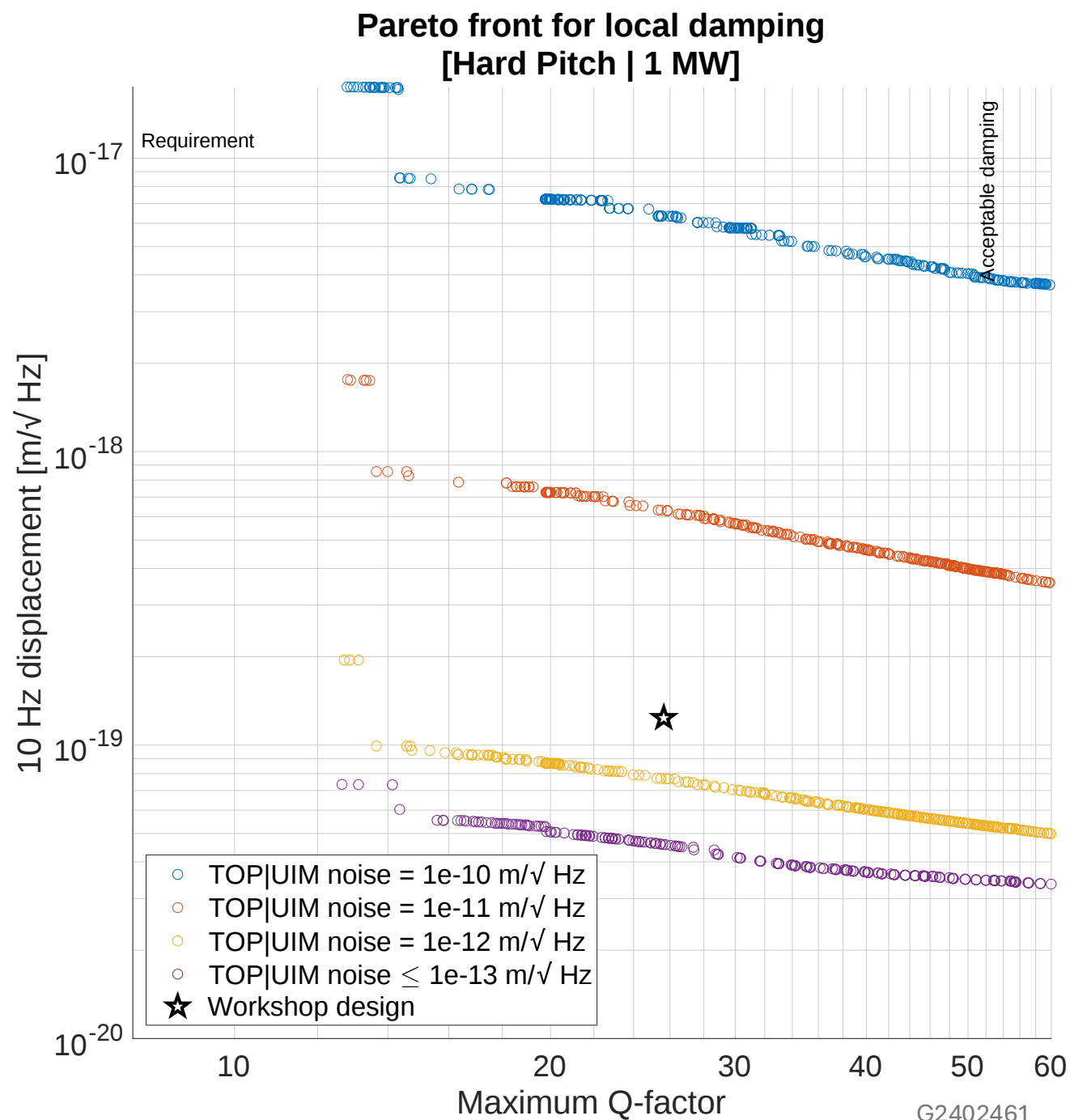
What noise for sensors?

Assumed controller:

2 real zeros at 0 Hz, 2 real poles , elliptic filter for rolloff.

For Longitudinal:

- Any sensor performing better than $1\text{ e-}13$ m/Hz^{1/2} will be limited by ISI noise.
- Sensors with noise above $3\text{ e-}11$ m/Hz^{1/2} are unlikely to meet our requirements
- A performance better than $5\text{ e-}12$ m/Hz^{1/2} is enough to rival the idealized calculations.



What noise for sensors?

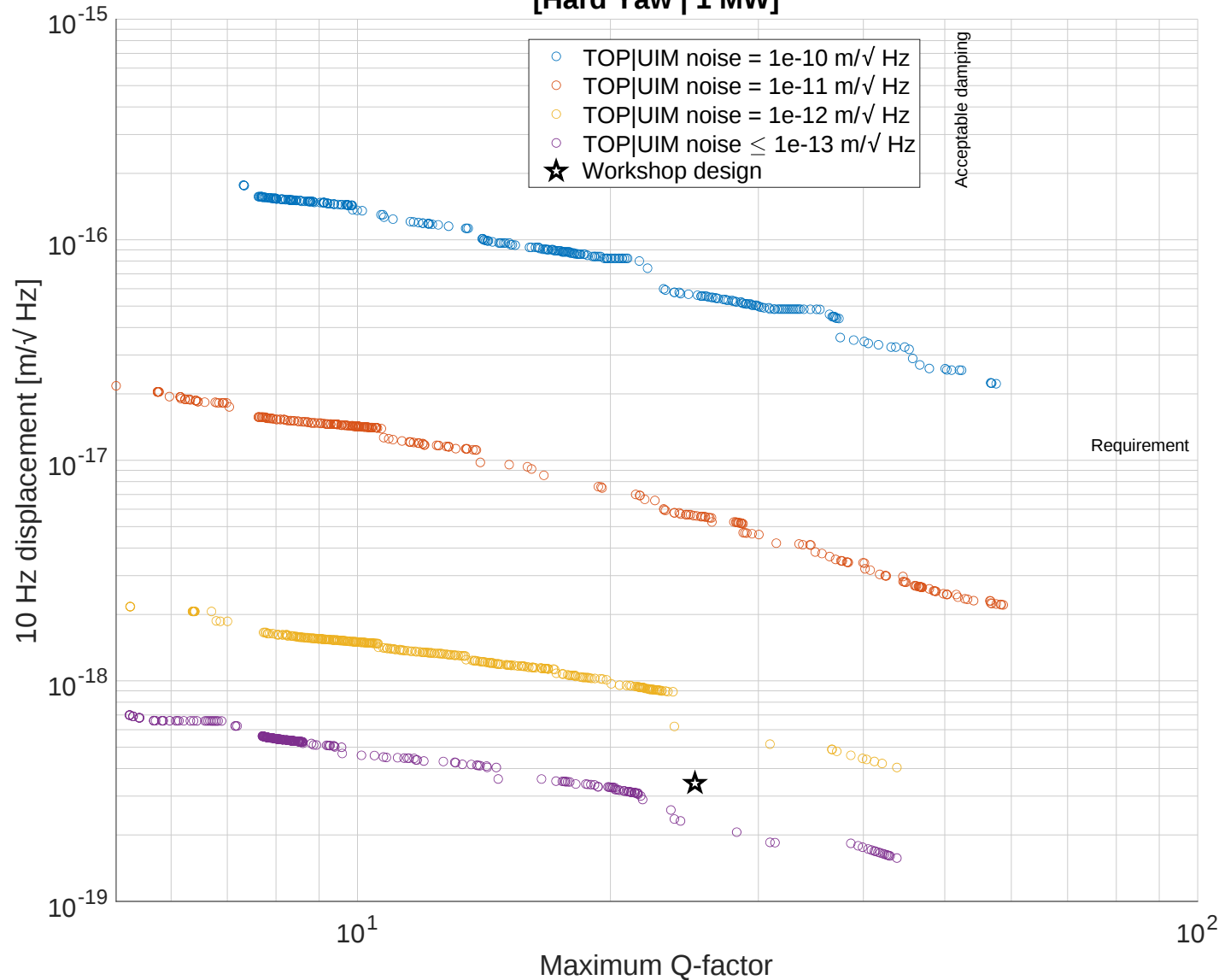
Assumed controller:

2 real zeros at 0 Hz, 2 real poles , elliptic filter for rolloff.

For Pitch:

- Up to 1 MW, we should be able to pick sensors up to $1e-10$ m/Hz^{1/2}.
- To get some margin, we would still prefer something below $1e-11$ m/Hz^{1/2}.

Pareto front for local damping
[Hard Yaw | 1 MW]



What noise for sensors?

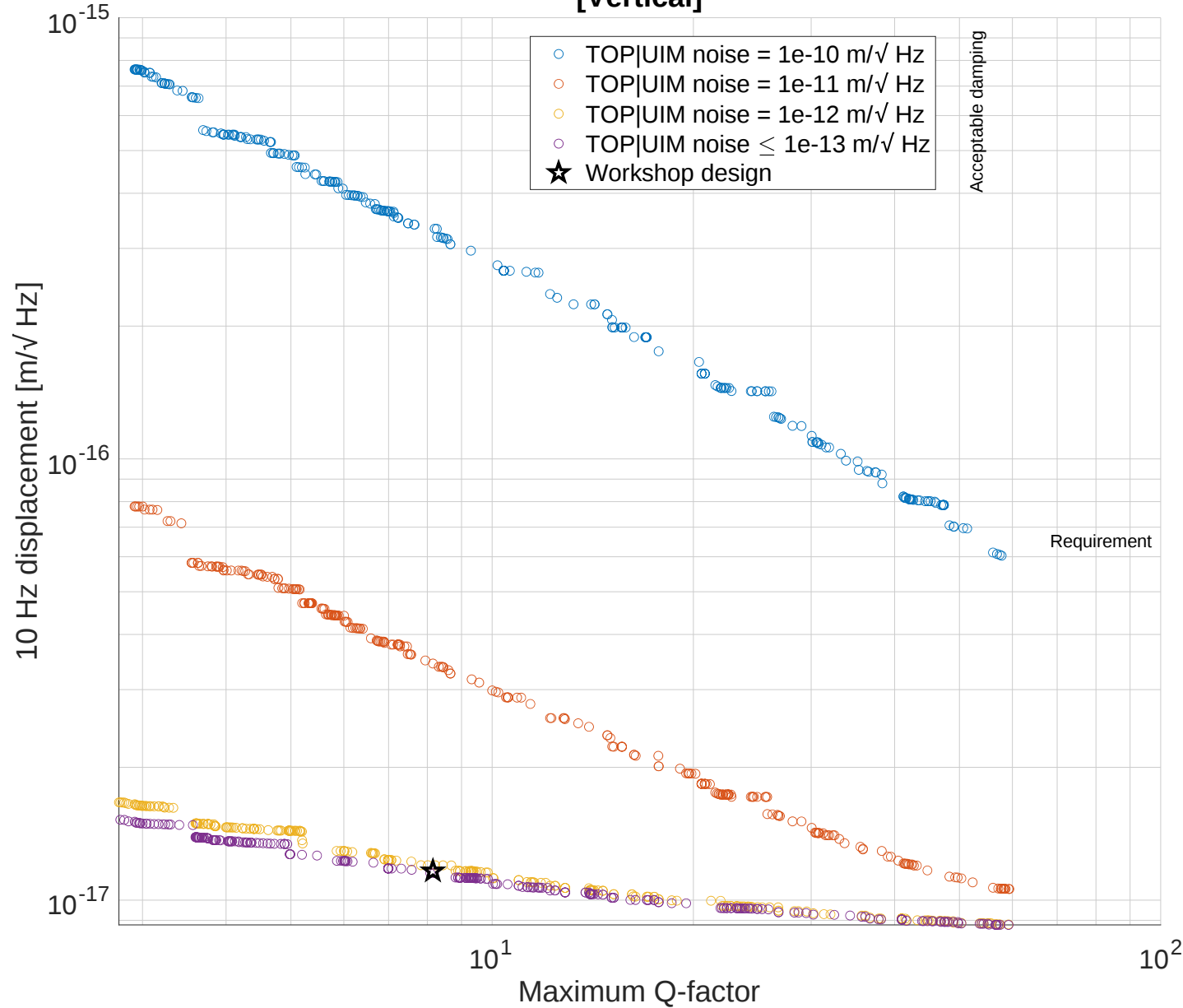
Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Yaw:

- We must use the UIM to aid with damping
- At 1 MW, we to damp the Yaw mode a sufficient amount, we want a sensor with noise below $1e-11$ m/Hz^{1/2}.

Pareto front for local damping [Vertical]



What noise for sensors?

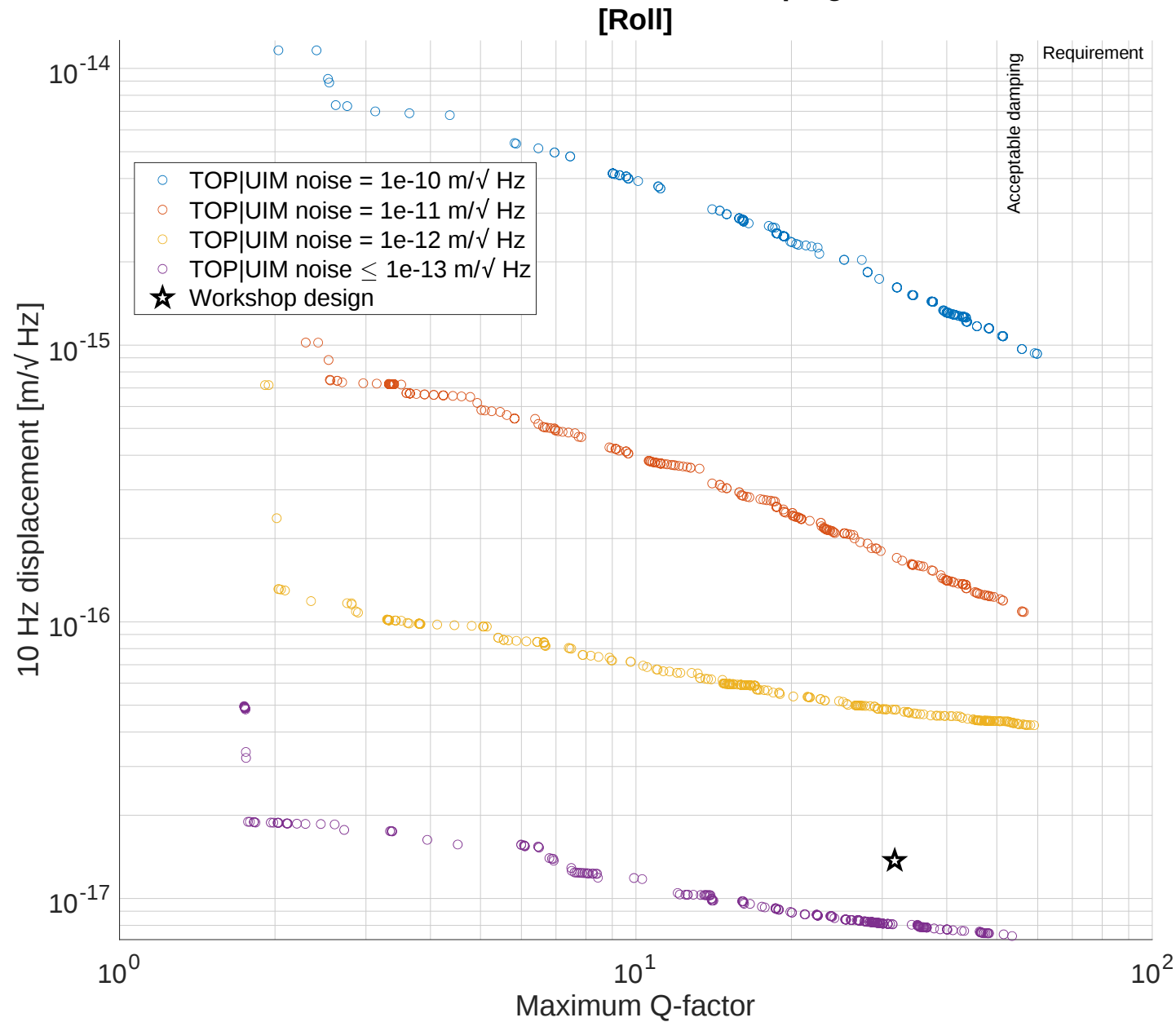
Assumed controller:

2 real zeros at 0 Hz, 2 real poles , elliptic filter for rolloff.

For Vertical (excluding the bounce mode):

- Only the TOP mass is needed for good performance.
- A sensing noise lower than the $3\text{e-}11$ m/Hz^{1/2} would allow for a Q of around 20.

Pareto front for local damping



What noise for sensors?

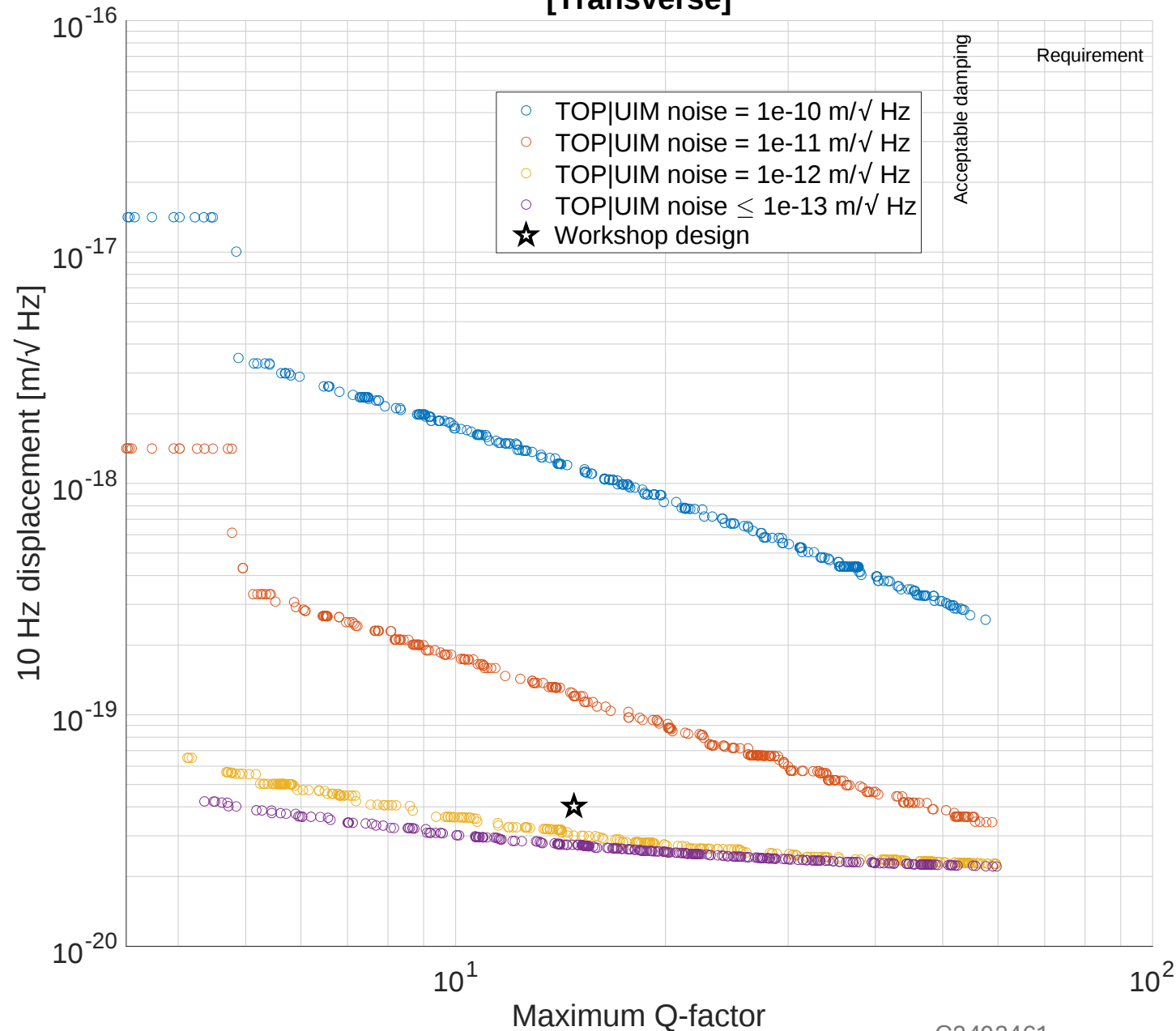
Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Roll (excluding the roll mode):

- We can piggyback from the other DOFs.
- The UIM is not required to achieve these loop performances.

Pareto front for local damping [Transverse]



What noise for sensors?

Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Transverse (excluding the roll mode):

- We can piggyback from the other DOFs.

Caveats

- How much uncertainty can we tolerate on this design?

About 250 microns on the d-values → Limited by microseism

Loop decoupling resists d-value uncertainties of at least 1cm

- Can we reduce the actuator noise?

There should be enough margin to reduce the ESD's authority without saturating the DACs

The noise comes from the TST stage, but most of the actuation RMS happens at the UIM.

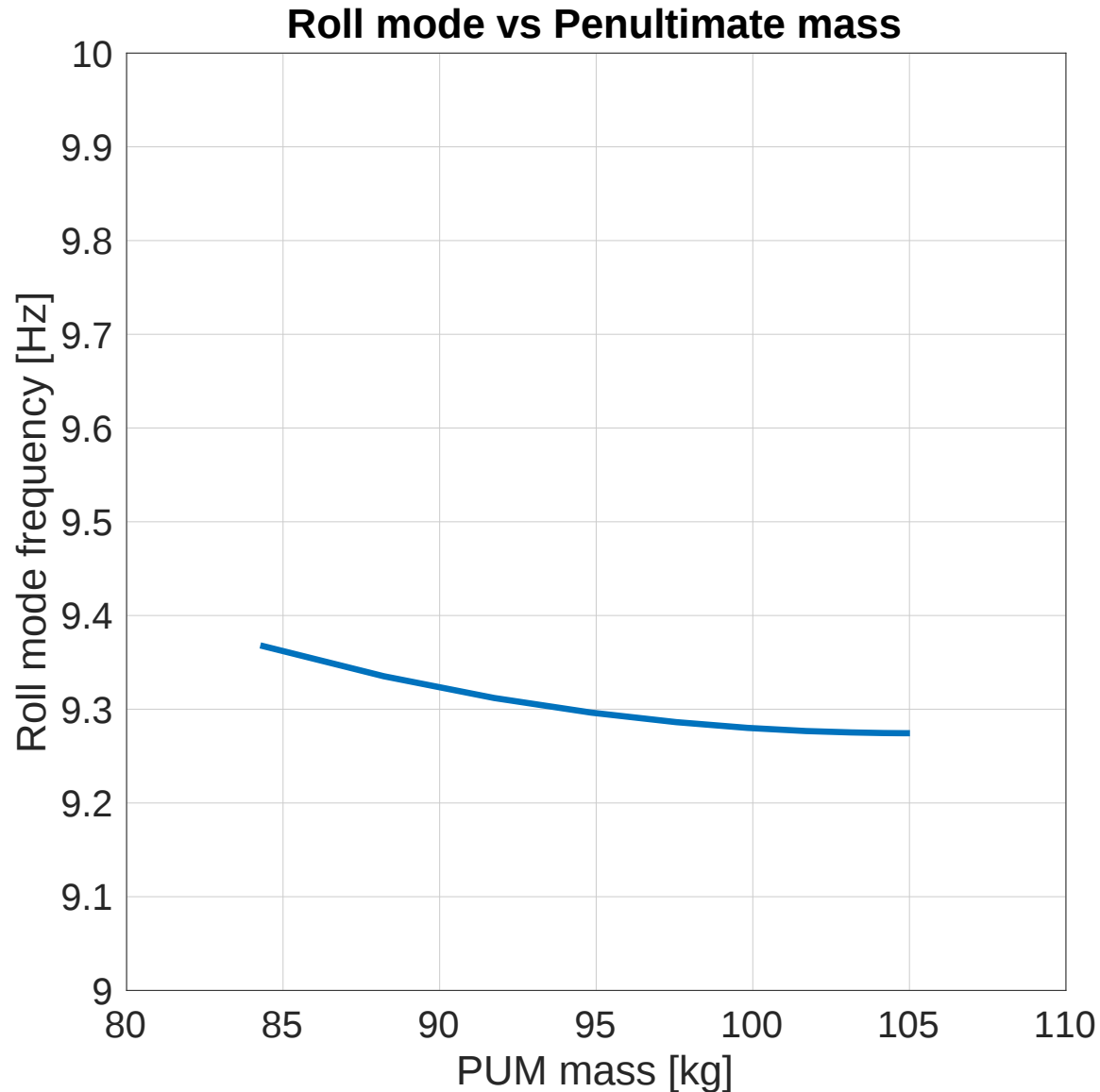
- How good do the sensors need to be?

Noise > $3\text{e-}11 \text{ m/Hz}^{1/2}$
 $3\text{e-}11 \text{ m/Hz}^{1/2} > \text{Noise} > 1\text{e-}11 \text{ m/Hz}^{1/2}$
 $1\text{e-}12 \text{ m/Hz}^{1/2} > \text{Noise} > 5\text{e-}13 \text{ m/Hz}^{1/2}$
 $1\text{e-}12 \text{ m/Hz}^{1/2} > \text{Noise} > 5\text{e-}13 \text{ m/Hz}^{1/2}$
 $5\text{e-}13 \text{ m/Hz}^{1/2} > \text{Noise} > 5\text{e-}13 \text{ m/Hz}^{1/2}$

Only for R, T
OK for all dofs (especially R,T,V)
Good enough for all dofs
Great
Excellent (we should improve the ISIs now)

Last minute things that we might want to consider

- Accurate assessment of the Roll mode frequency.
- Should we trade off Roll mode for Longitudinal isolation?
- What if we increased the mass of the test mass to 105 kg?
- What about trading Pitch at low frequencies for damping the Pitch hard mode?
- Should we change the orientation of the blade springs?



Should we trade off with the roll mode?

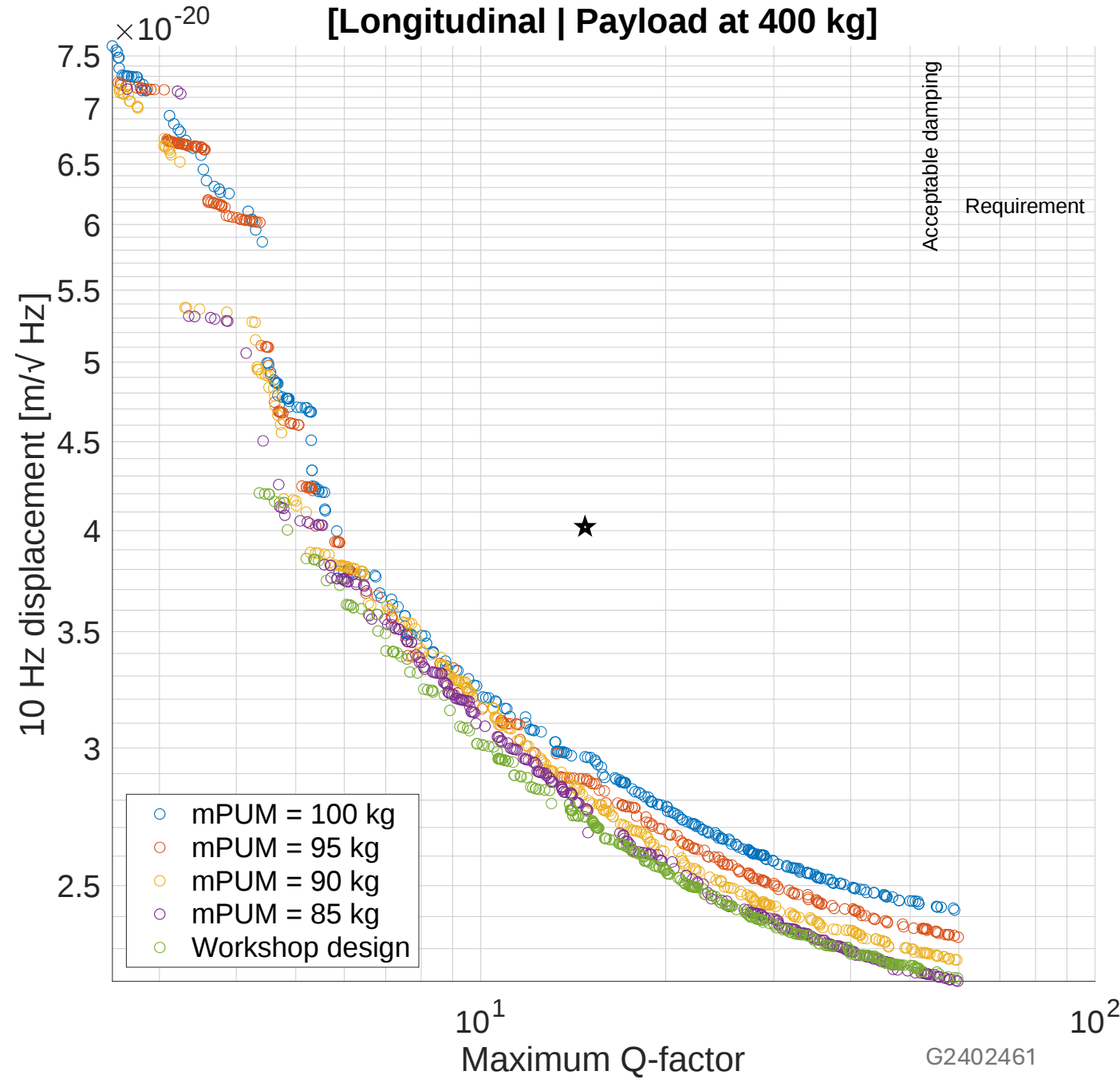
- Taking into account the effect of the nulling region for the fibers sets the roll mode at around 9.3 Hz.
- Changing the mass of the PUM in a 'donut' pattern has little effect on this.

Recommendation:

Only trade off if something would greatly benefit (Length | Pitch | Yaw)

Not very worth the risk since the $f_{\text{Roll}} > 9 \text{ Hz}$

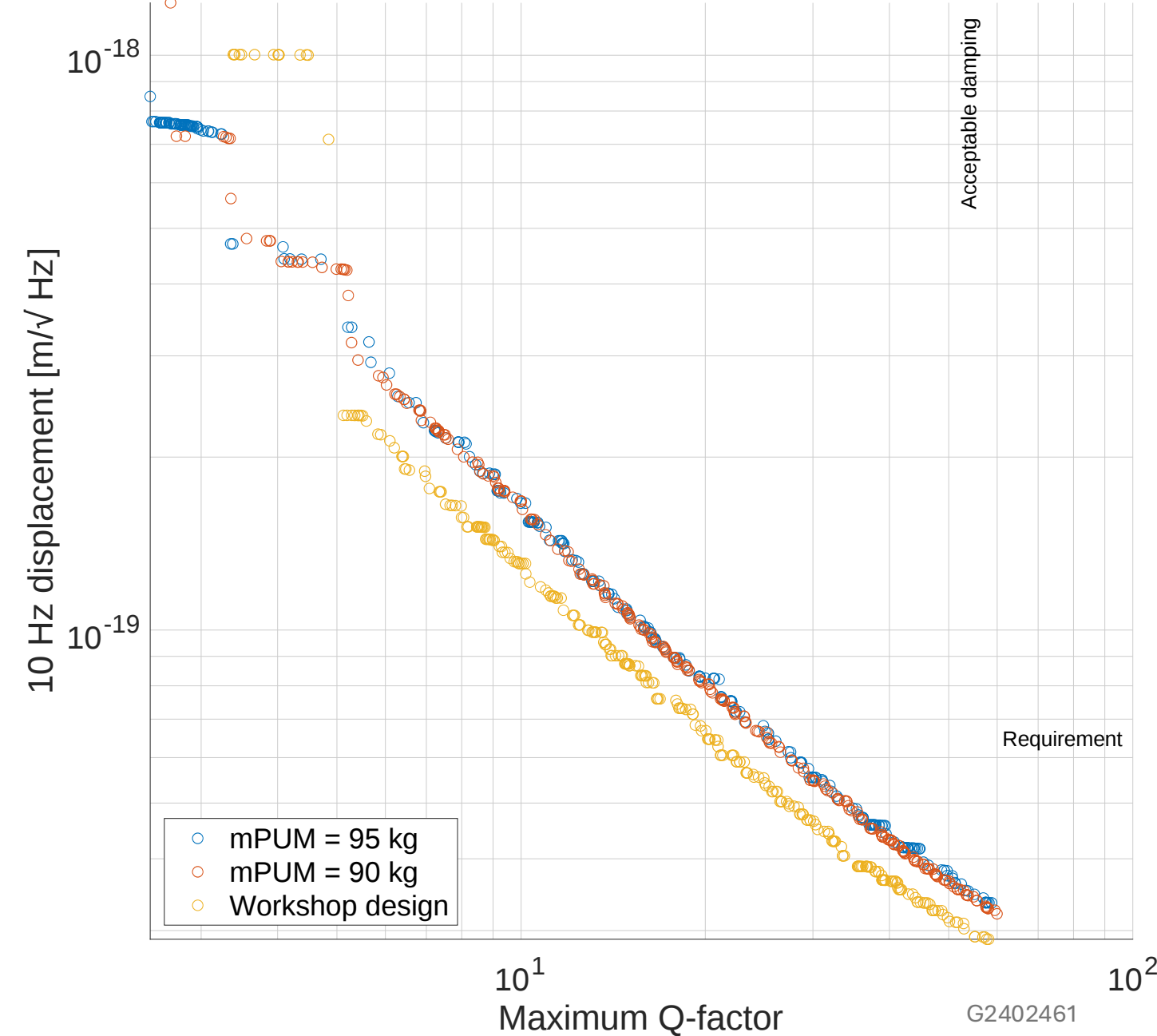
Pareto front for local damping [Longitudinal | Payload at 400 kg]



Should we increase the mass of the TST stage?

- We get marginally worse longitudinal performance unless we increase the payload proportionally.
- Payload should be 420 kg if we want to retain Longitudinal isolation.

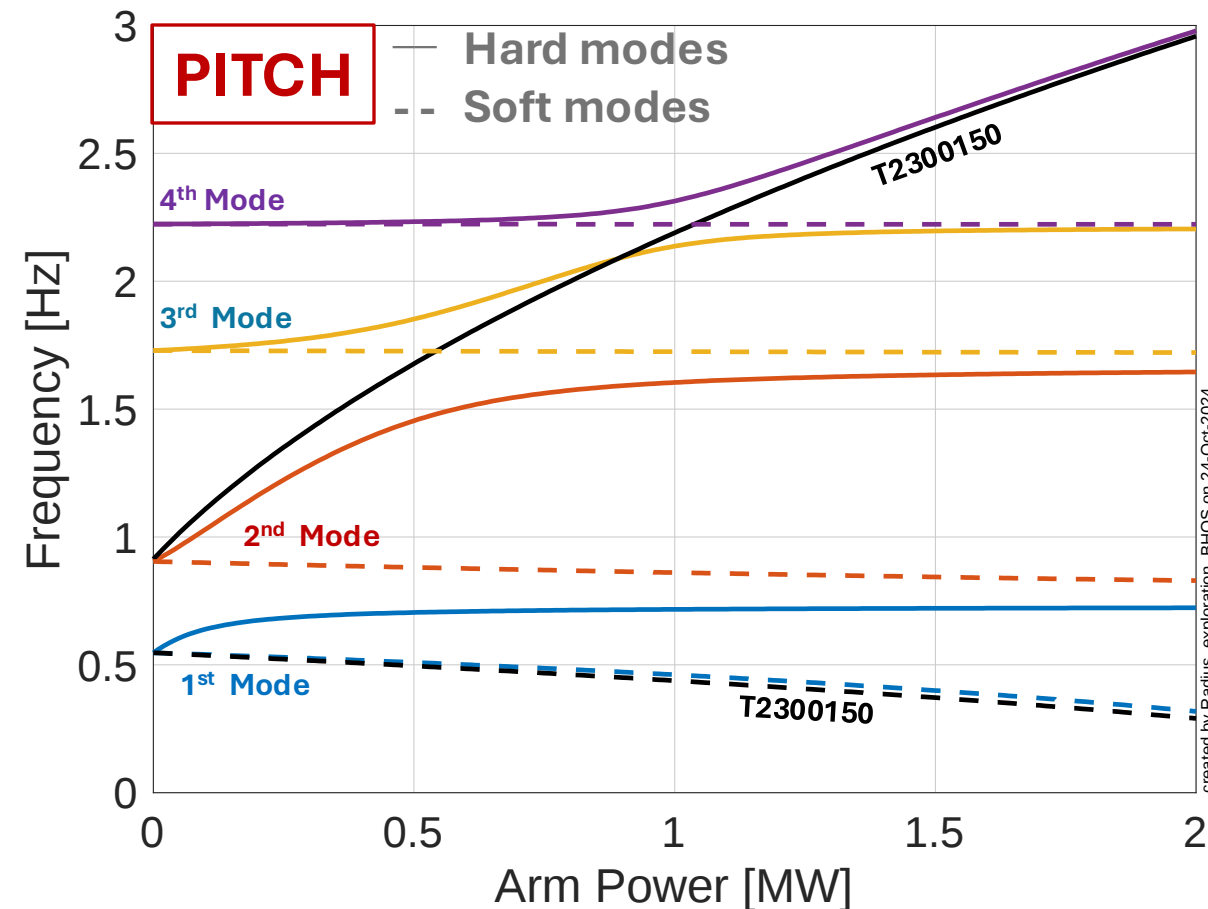
Pareto front for local damping [Longitudinal | Payload at 400 kg]



Should we increase the mass of the TST stage?

- We get marginally worse longitudinal performance unless we increase the payload proportionally.
- If we added $1\text{e-}11 \text{ m/Hz}^{1/2}$ sensor noise the situation looks equally compromised.
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Should we increase the mass of the TST stage?

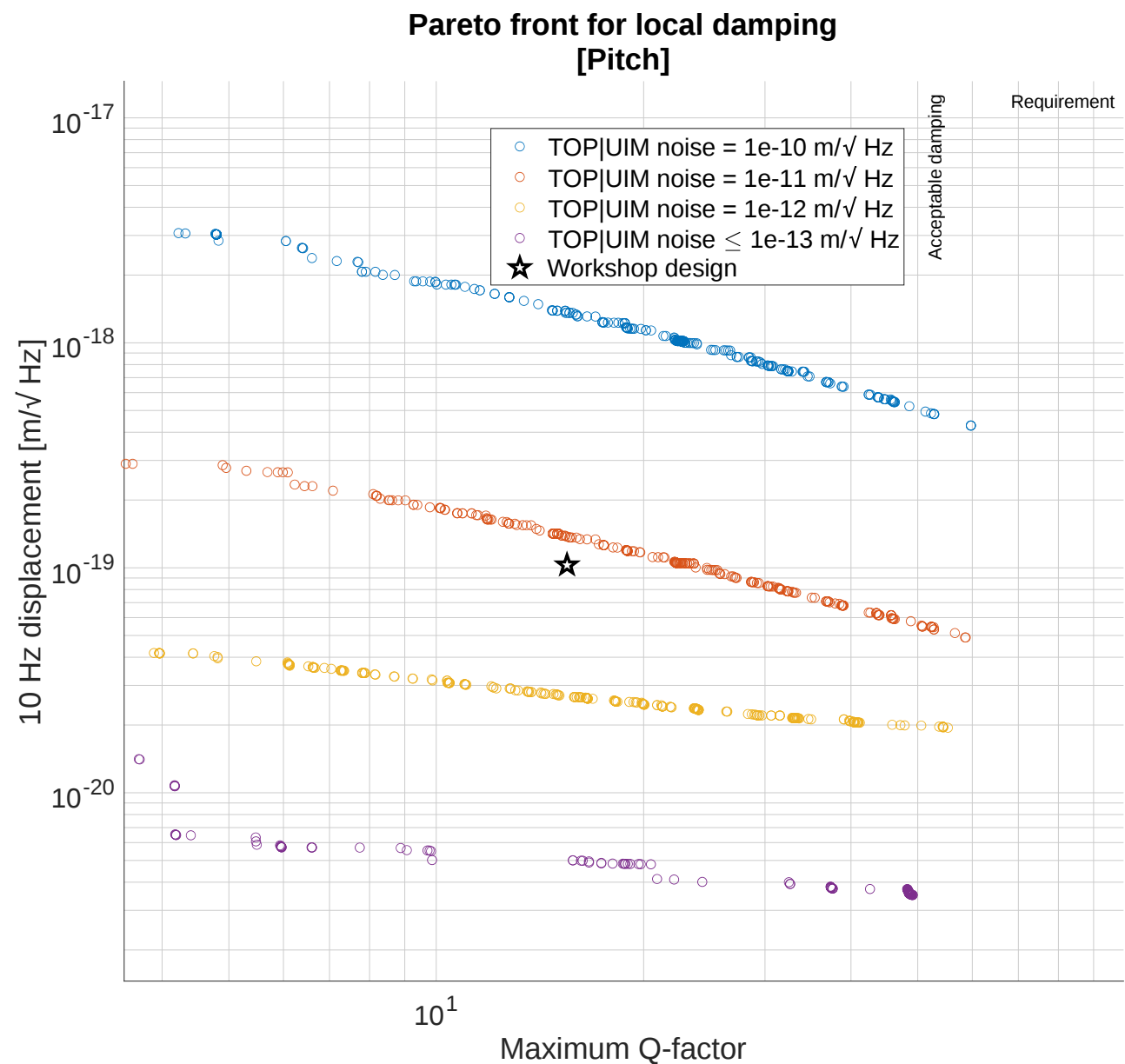


$$f_{4,\text{hard}} \approx \frac{1}{2\pi} \sqrt{\frac{k_{\text{hard}} + k_4}{I_4}}$$

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- If we added $1\text{e-}11 \text{ m/Hz}^{1/2}$ sensor noise the situation looks equally compromised.
- Payload should be 420 kg if we want to retain Longitudinal isolation.
- Moving to 105 kg results in a 2.5 % reduction in the Pitch hard mode frequency at 1.5 MW

Recommendation:

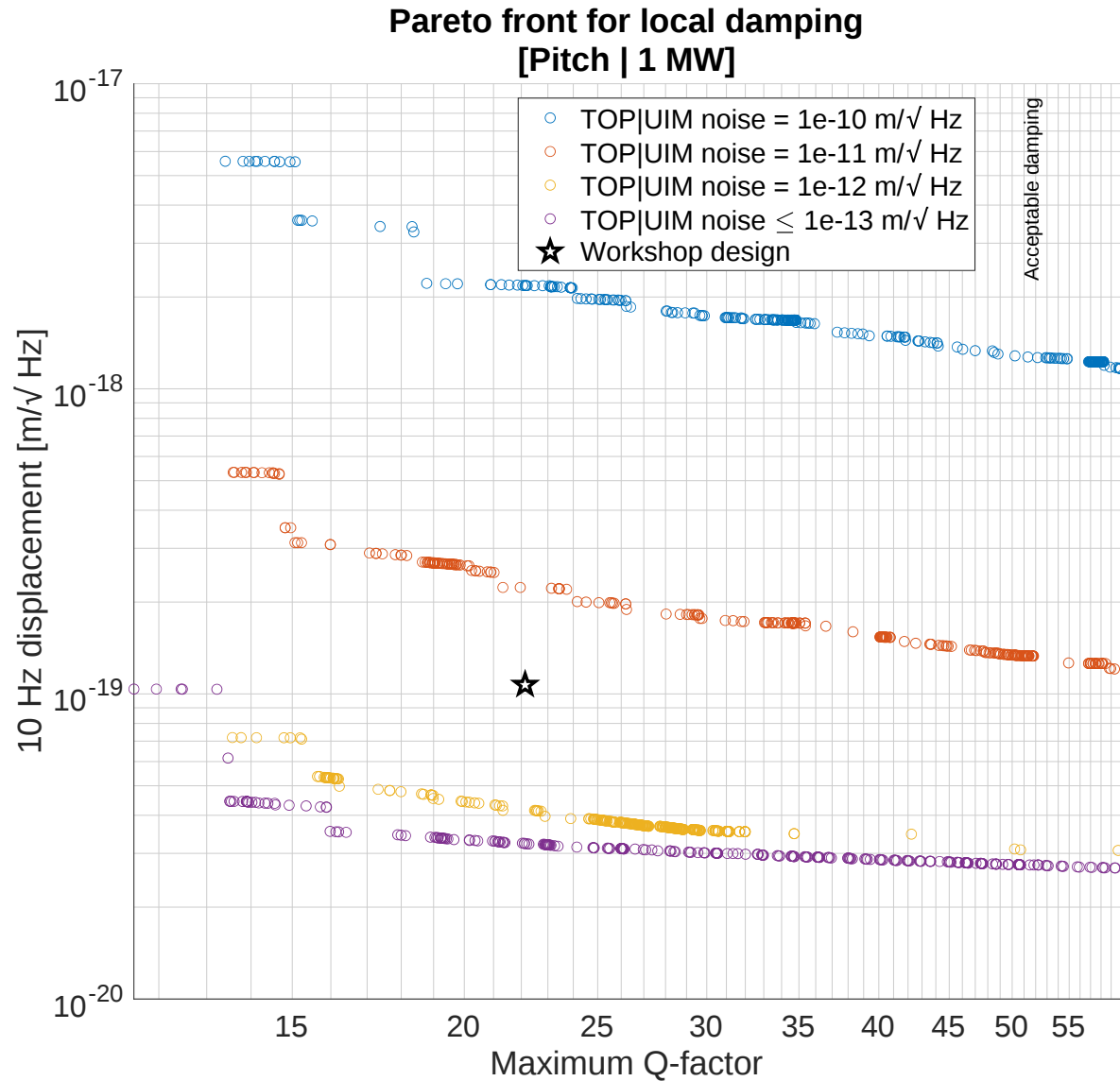
Increase proportional to the payload if possible.
Unless 2.5% change in the hard mode is worth it



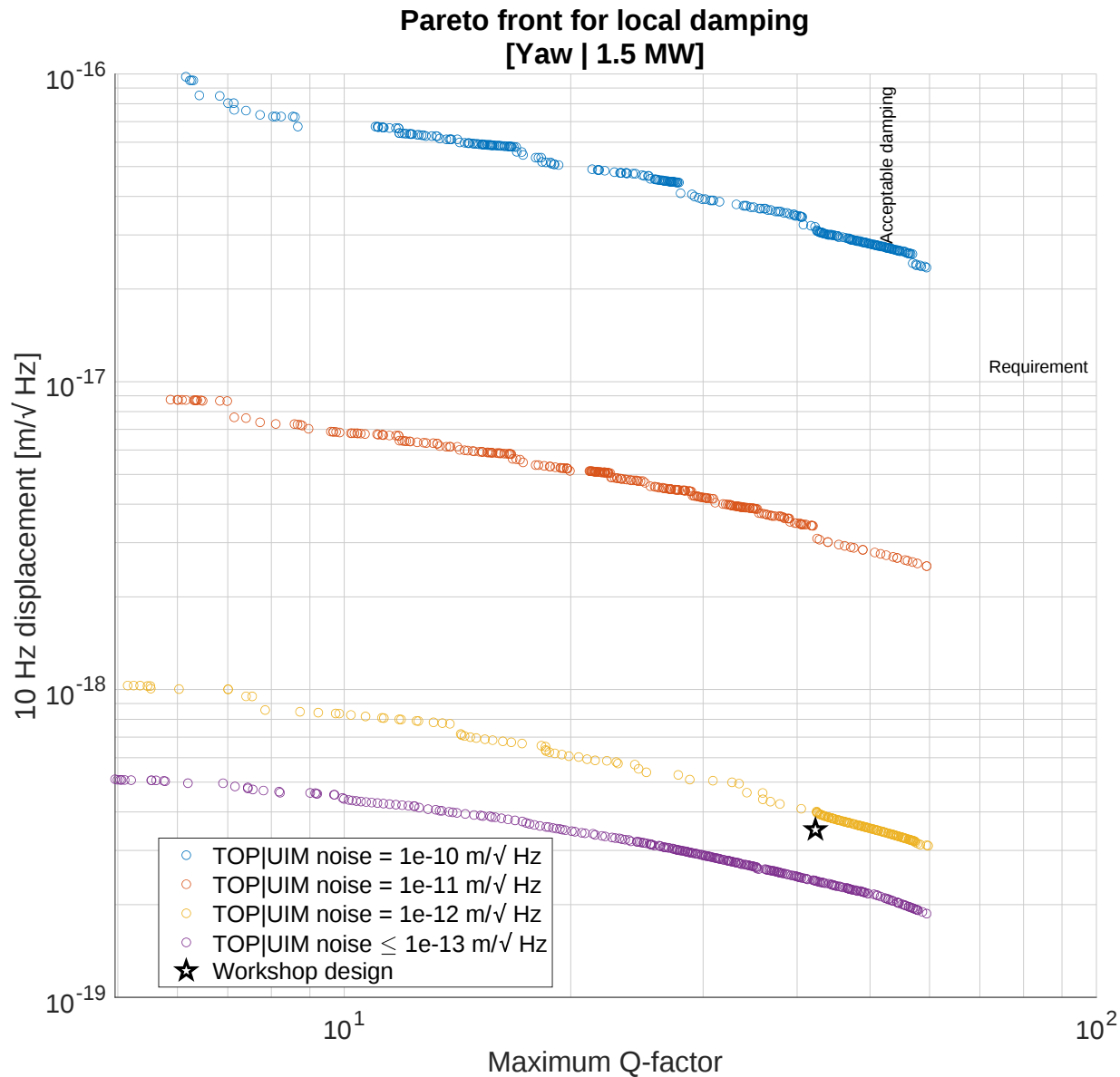
Trade off to better damp the hard Pitch mode?

- The Pitch plant is optimized to be easy to damp in any sensor noise condition at 0 W.

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- We are in good shape (Q of 14 or so) with $1e-11$ m/Hz^{1/2} sensors up to 1 MW with some tuning of the local damping.
 - By 1.2 MW it is unfeasible to keep the Q below 20 with local damping



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 - By 1.2 MW it is unfeasible to keep the Q below 20 with local damping
- In contrast, Yaw can be damped to a Q of 8 while meeting the requirements with $1\text{e-}11$ m/Hz^{1/2}

Recommendation:

Target an 'easy to operate' power over which we want low Qs.

Design with less margin to locally damp for longer

General conclusions

- The conceptual design of the BHQS is finalized.
 - Hopefully, all modes below 10 Hz.
 - It should perform without issues until 800 kW – should be easy to work at 1 MW power.
 - The ASC is challenging past that up to 1.5 MW
- We have a tool to compare (and codesign) damping with suspension designs.
[15 second runtime per design]
- We established tolerances for the d values (0.25 mm)
- We established a target for the suspension sensors:
 - $3\text{e-}11 \text{ m/Hz}^{1/2} > \text{Noise} > 1\text{e-}11 \text{ m/Hz}^{1/2}$ OK for all dofs (especially R,T,V)
 - $1\text{e-}12 \text{ m/Hz}^{1/2} > \text{Noise} > 5\text{e-}13 \text{ m/Hz}^{1/2}$ Good enough for all dofs
 - $1\text{e-}12 \text{ m/Hz}^{1/2} > \text{Noise} > 5\text{e-}13 \text{ m/Hz}^{1/2}$ Great
 - $5\text{e-}13 \text{ m/Hz}^{1/2} > \text{Noise} > 5\text{e-}13 \text{ m/Hz}^{1/2}$ Excellent (we should improve the ISIs now)