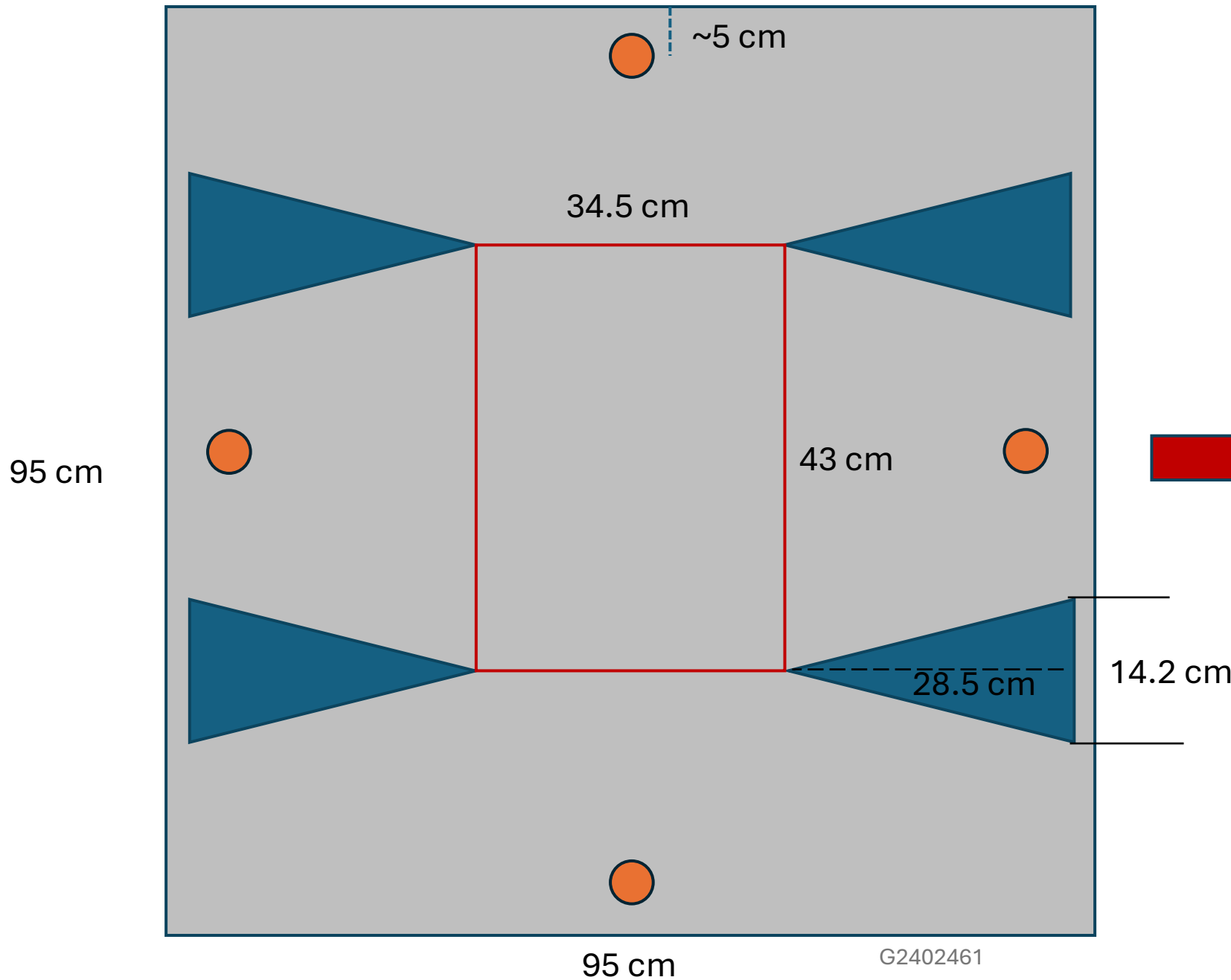


3rd BHQS Workshop Slides

Edgard Bonilla

Outline

- Design refresher
- Numbers for the design
- Show the LSC | ASC loops
 - It works easily at 800 kW
 - Challenging at 1.5 MW
- Uncertainty analysis
 - 0.25 mm seems like the d-value uncertainty
 - At 1 mm we would just get more low-f RMS
- How good do the sensors need to be?
 - 1 e-11 is good enough for all dofs.
 - 1 e-12 for UIM sensors would get most of the design where we want it.
- Anything we missed?
 - Roll mode estimate – 9.5 Hz? – Let's not cut the PUM
 - Smaller PUM – Depends on Roll
 - Higher resonance in Pitch – I think it is worth it, but only helps above 1 MW power

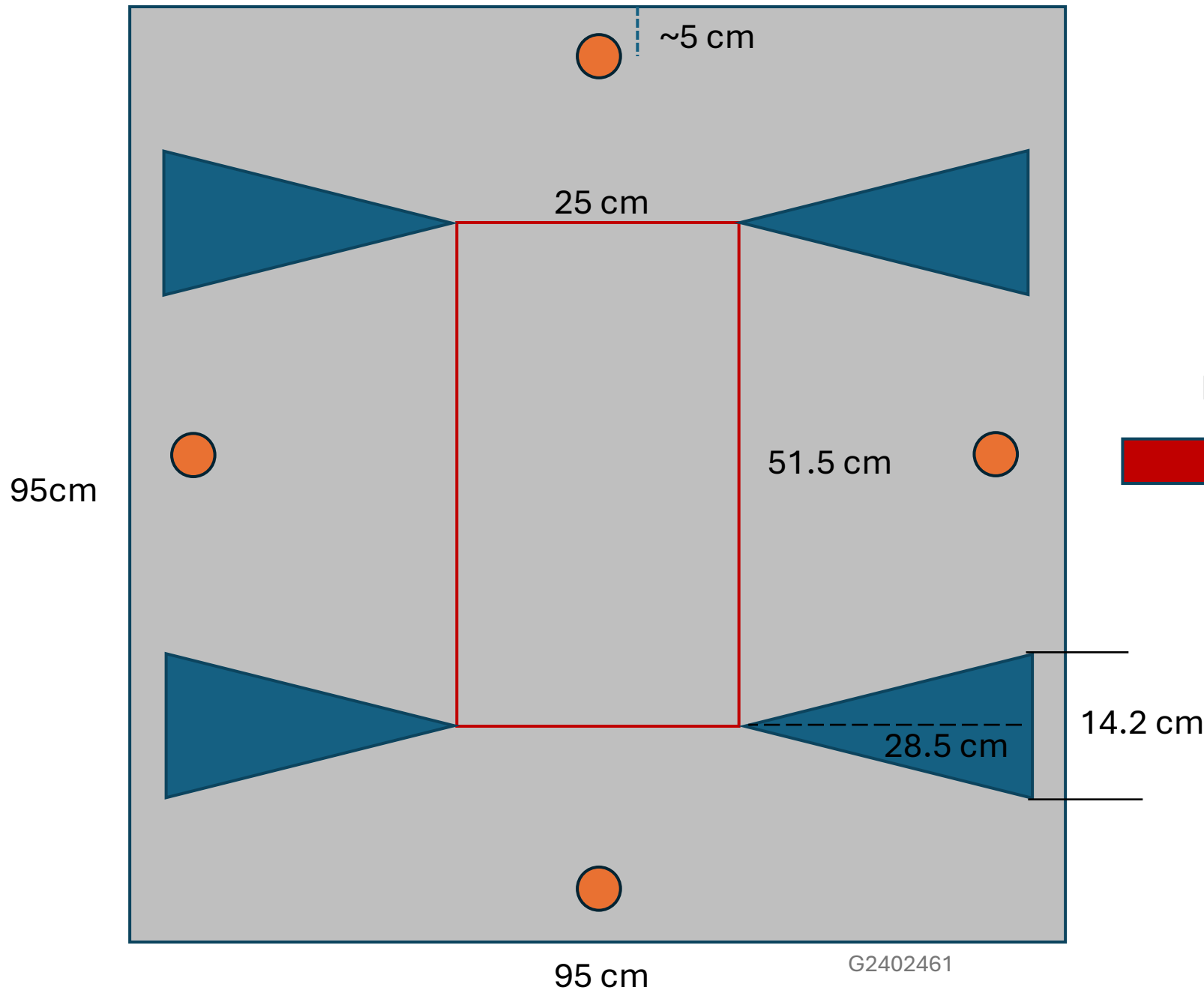


Top Mass (top view)

Beam tube direction



- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)

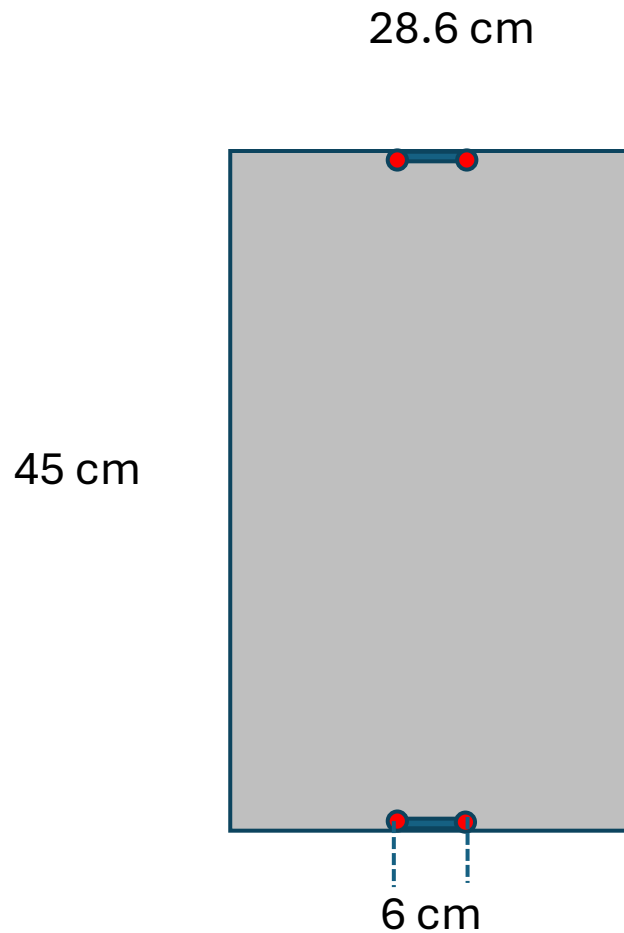


UIM (top view)

Beam tube direction



- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)

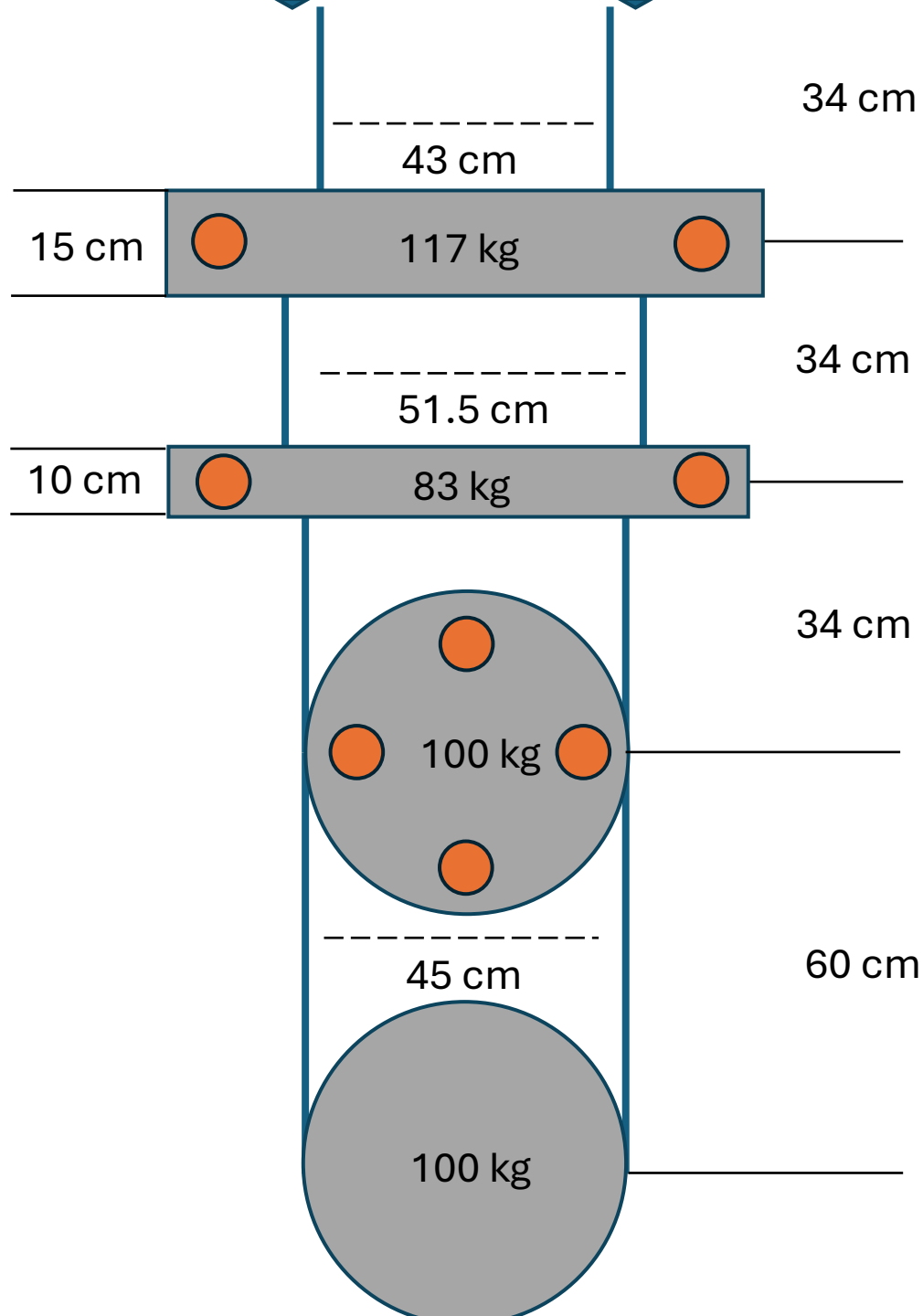


PUM (top view)

Beam tube direction

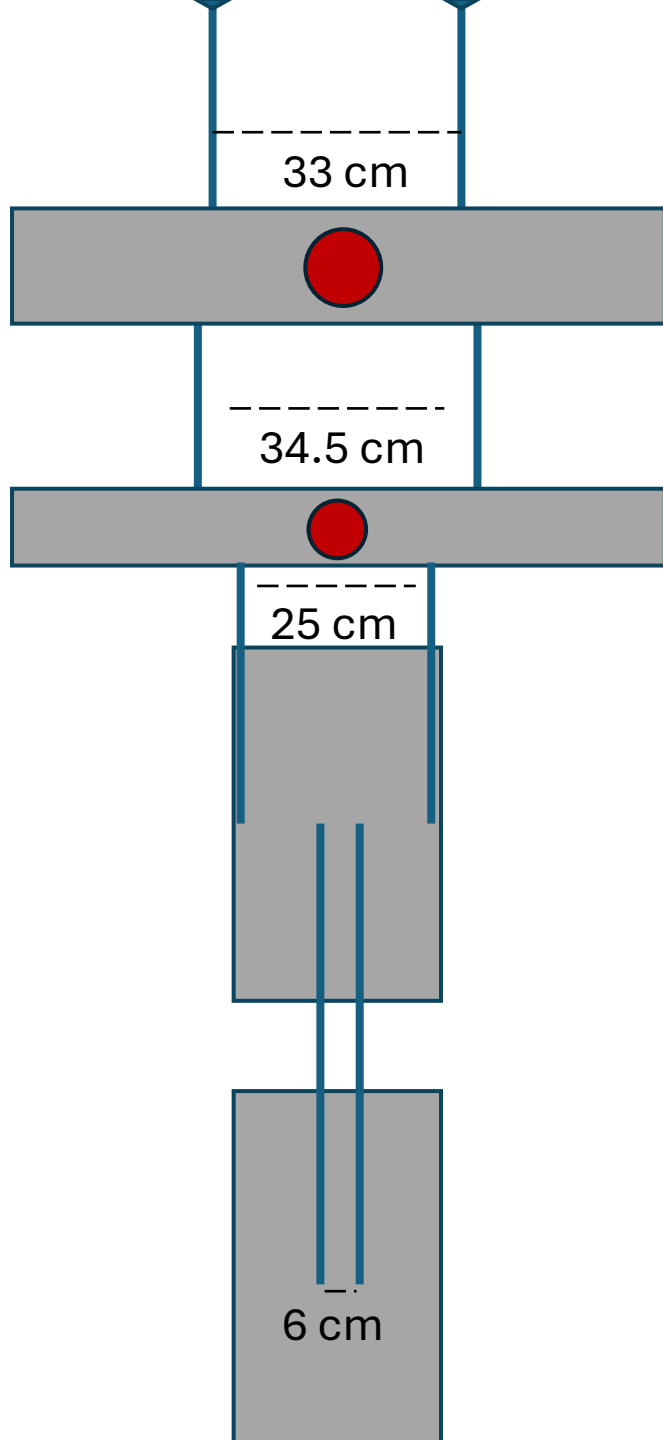


- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)



BHQS (front view)

- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)



BHQS

(side view)

- **TOP:** 7 Sensors/Actuators.
- **UIM:** 7 Sensors/Actuators.
- **PUM:** 4 Sensors/Actuators. (L/P/Y)
- **TST:** 4 Sensors/Actuators. (L/P/Y)

Design parameters (full)

Symbols	Description	Units	TOP	UIM	PUM	TST
$m_n/m_1/m_2/m_3$	Mass	[kg]	117	83	100	100
$I_{n,x}/I_{1,x}/I_{2,x}/I_{3,x}$	Roll moment of inertia	[kg·m ²]	9.7	5.9	2.6	2.6
$I_{n,y}/I_{1,y}/I_{2,y}/I_{3,y}$	Pitch moment of inertia	[kg·m ²]	10.3	6.3	1.9	1.9
$I_{n,z}/I_{1,z}/I_{2,z}/I_{3,z}$	Yaw moment of inertia	[kg·m ²]	17.6	10	1.9	1.9
$I_{n,xy}/I_{1,xy}/I_{2,xy}/I_{3,xy}$	R-P cross moment of inertia	[kg·m ²]	0	0	0	0
$I_{n,yz}/I_{1,yz}/I_{2,yz}/I_{3,yz}$	P-Y cross moment of inertia	[kg·m ²]	0	0	0	0
$I_{n,zx}/I_{1,zx}/I_{2,zx}/I_{3,zx}$	Y-R cross moment of inertia	[kg·m ²]	0	0	0	0
$k_{cn}/k_{c1}/k_{c2}$	Vertical spring stiffness (per side)	[kN/m]	6.5	9.3	5.2	N/A
$k_{xn}/k_{x1}/k_{x2}$	Lateral spring stiffness (per side)	[kN/m]	2500	2600	2200	N/A
$Y_n/Y_1/Y_2/Y_3$	Young's moduli of wires	[GPa]	212	212	212	72
$l_n/l_1/l_2/l_3$	Stretched wire length	[m]	0.34	0.34	0.34	0.60
$r_n/r_1/r_2/r_3$	radii of wires	[μm]	1400	1200	1000	220
$d_{top}/d_n/d_1/d_3$	(upper) wire vertical attachment distance	[mm]	0	0	0	0
$d_m/d_0/d_2/d_4$	(lower) wire vertical attachment distance	[mm]	0	0	0	0
$s_n/s_u/s_i/s_l$	front-back wire attachment distance	[cm]	16.5	17	12.5	2.95
$n_{n0}/n_0/n_2/n_4$	(upper) wire transverse attachment distance	[cm]	21.6	25.7	22.5	22.5
$n_{n1}/n_1/n_3/n_5$	(lower) wire transverse attachment distance	[cm]	21.6	25.7	22.5	22.5

Design parameters (full)

Description	Units	ST2	TOP	UIM
Length	[cm]	44.0	28.5	28.5
Width	[cm]	22.0	14.2	14.2
Thickness	[mm]	3.4	2.9	2.4
Stress	[MPa]	1000	1000	1000
Deflection	[cm]	23.8	22.0	24.0
Radius of curvature	[cm]	31.6	26	22.8
Internal mode	[Hz]	74	80.1	73.5

Blade Springs:

These were changed in Dec 2023 so the TOP|UIM fit within 1 square meter.

It makes the vertical plant stiffer.
[G2302370](#)

Fiber stress: 1.6 Gpa - [Double that of Advanced LIGO]

Thin radius: 220 μm

Thick radius: 650 μm - [For nulling thermoelastic]

Nulling length: 4 cm - [On each end]

Design parameters (Simplified)

Symbols	Description	Units	TOP	UIM	PUM	TST
L	Distance to the previous stage	[cm]	34	34	34	60
m	Mass of the stage	[kg]	117	83	100	100
I_{RR}	Stage moment of inertia (Roll)	[kg·m ²]	9.7	5.9	2.6	2.6
I_{PP}	Stage moment of inertia (Pitch)	[kg·m ²]	10.3	6.3	1.9	1.9
I_{YY}	Stage moment of inertia (Yaw)	[kg·m ²]	17.6	10	1.9	1.9
k_L	Longitudinal stiffness above stage	[kN/m]	11.5	8.1	5.7	1.6
k_T	Transverse stiffness above stage	[kN/m]	11.5	8.1	5.7	1.6
k_V	Vertical stiffness above stage	[kN/m]	13	18.6	11	84.9
k_R	Roll rotational stiffness above stage	[N·m]	610	1200	560	4300
k_P	Pitch rotational stiffness above stage	[N·m]	355	550	170	74
k_Y	Yaw rotational stiffness above stage	[N·m]	852	785	380	84

Design parameters (Simplified)

Degree of freedom	Units	f_1	f_2	f_3	f_4
Longitudinal	[Hz]	0.45	0.96	1.7	2.6
Transverse	[Hz]	0.45	0.96	1.7	2.6
Vertical	[Hz]	0.67	1.91	3.6	6.7
Roll	[Hz]	0.77	1.86	3.3	9.4
Pitch	[Hz]	0.55	0.93	1.77	2.23
Yaw	[Hz]	0.68	1.05	1.86	2.72

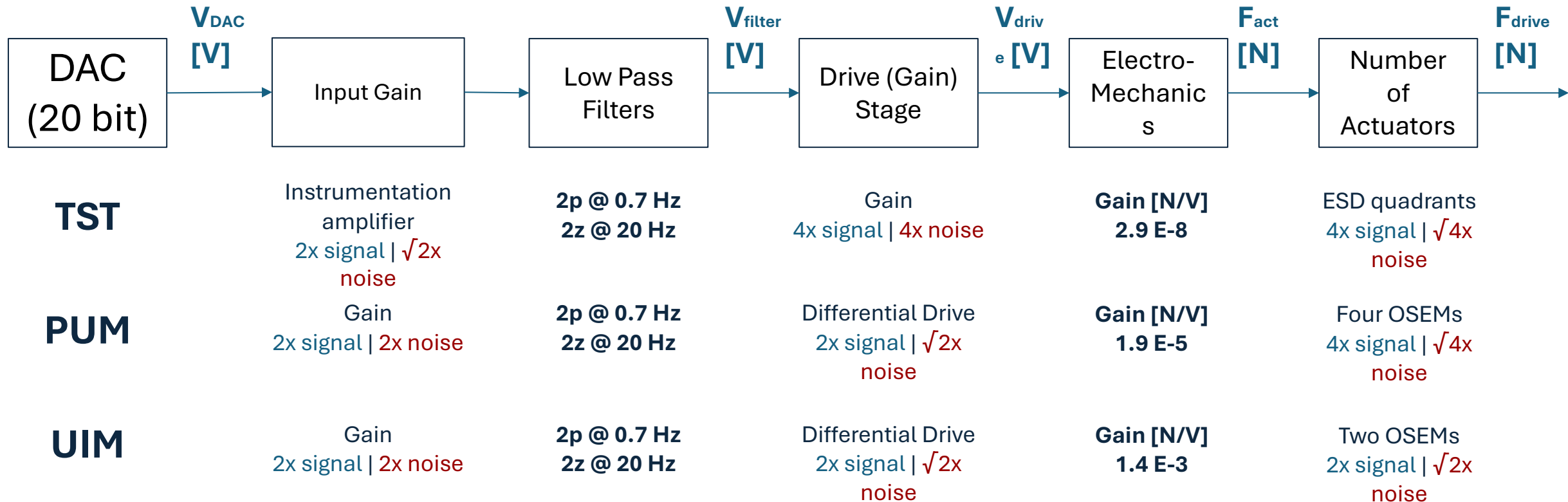
Bounce and roll
recalculated to account
for fiber nulling region
[4 cm on each side]

LSC | ASC loops

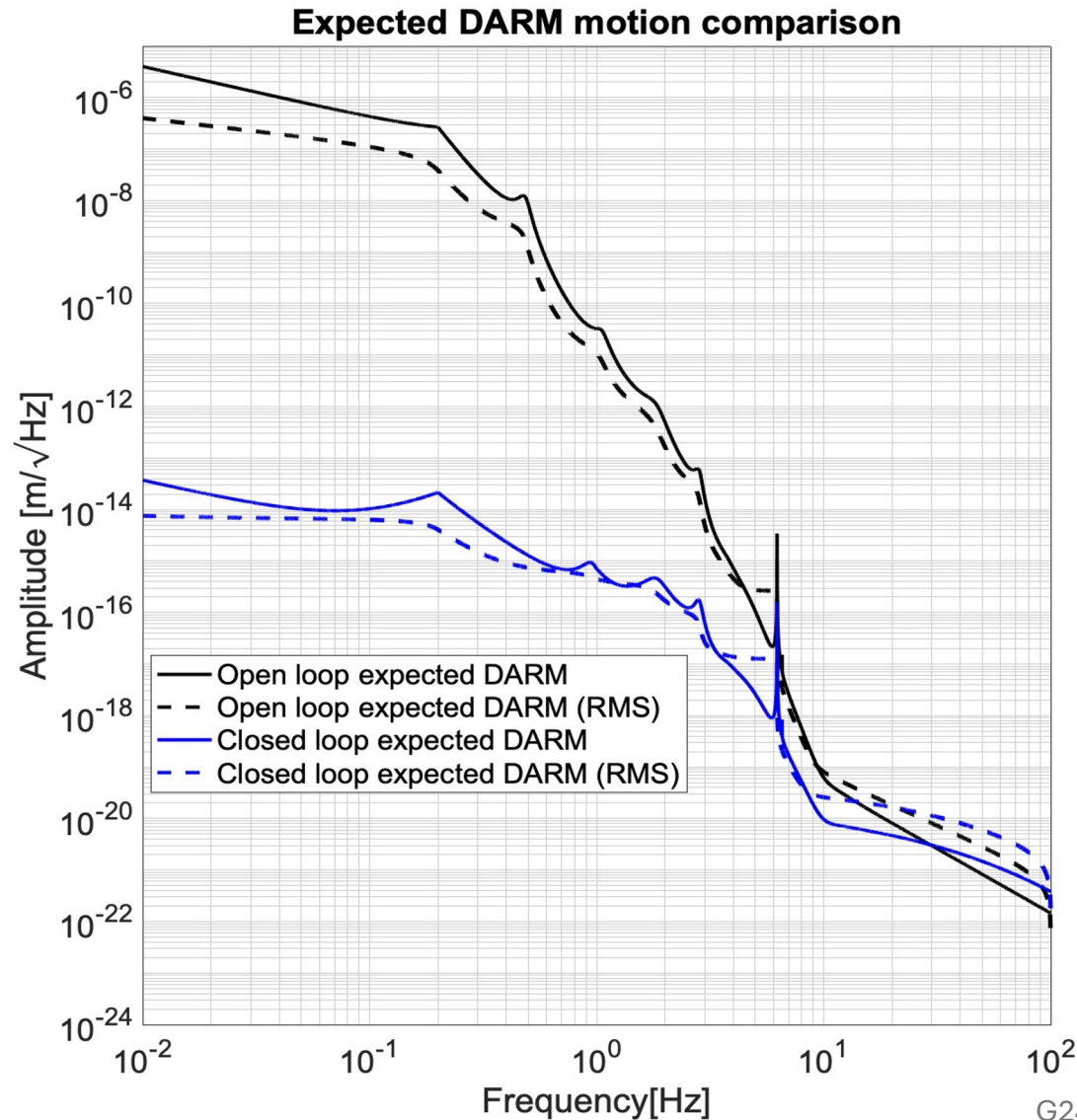
LSC Loops



Full strawman design: [G2401425](#)



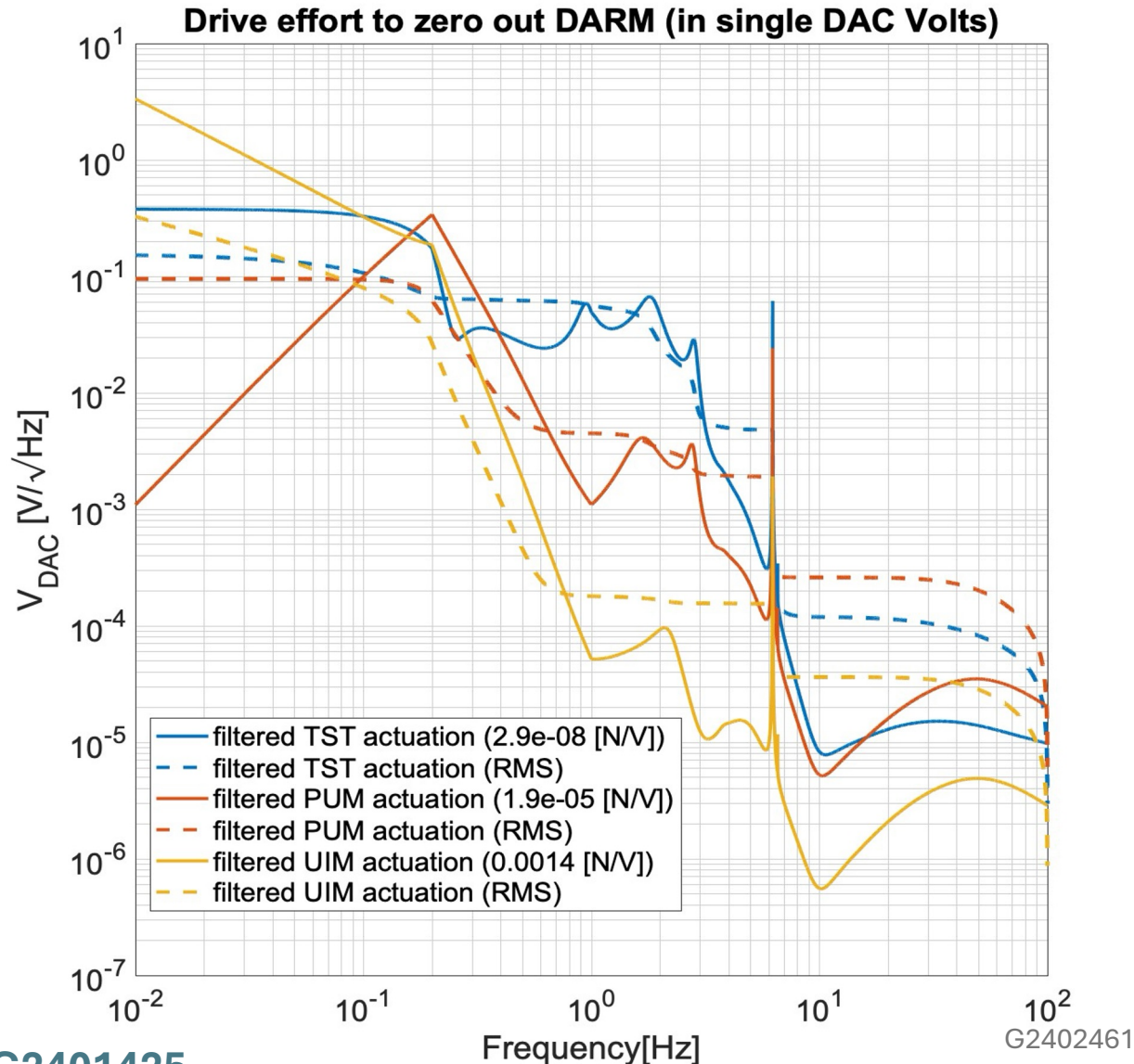
LSC Loops



Strawman controller performance

- 70 Hz unity gain frequency.
- Conditionally stable (but that's ok)
- 10^{-14} m RMS in closed loop (as required)

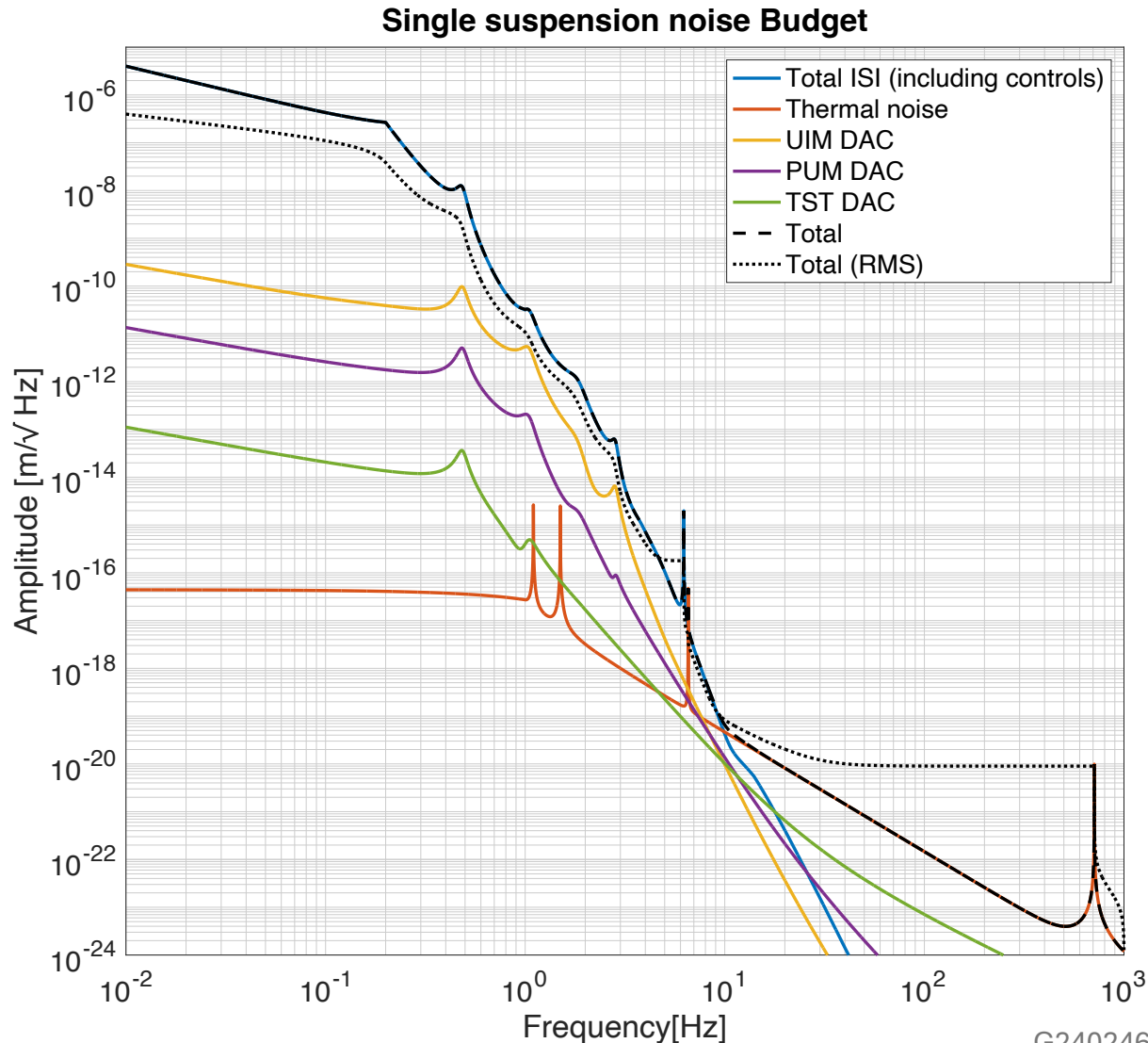
LSC Loops



Strawman controller performance

- 70 Hz unity gain frequency.
- Conditionally stable (but that's ok)
- 10^{-14} m RMS in closed loop (as required)
- The drive effort is distributed among the UIM, PUM and TST stages.
- The RMS voltage for all three does not exceed 1 V.

LSC Loops



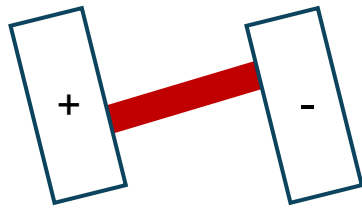
Strawman controller performance

- 70 Hz unity gain frequency.
- Conditionally stable (but that's ok)
- 10^{-14} m RMS in closed loop (as required)
- The drive effort is distributed among the UIM, PUM and TST stages.
 - The RMS voltage for all three does not exceed 1 V.
- The DAC noise is consistently 5x below the ISI+Thermal noise contribution above 4 Hz.

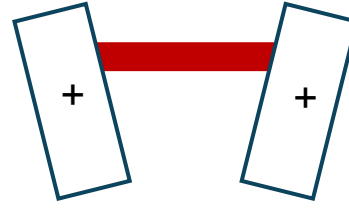
ASC loops

ASC Loops

- They are actuated from the PUM in the hard/soft basis



Hard DOF



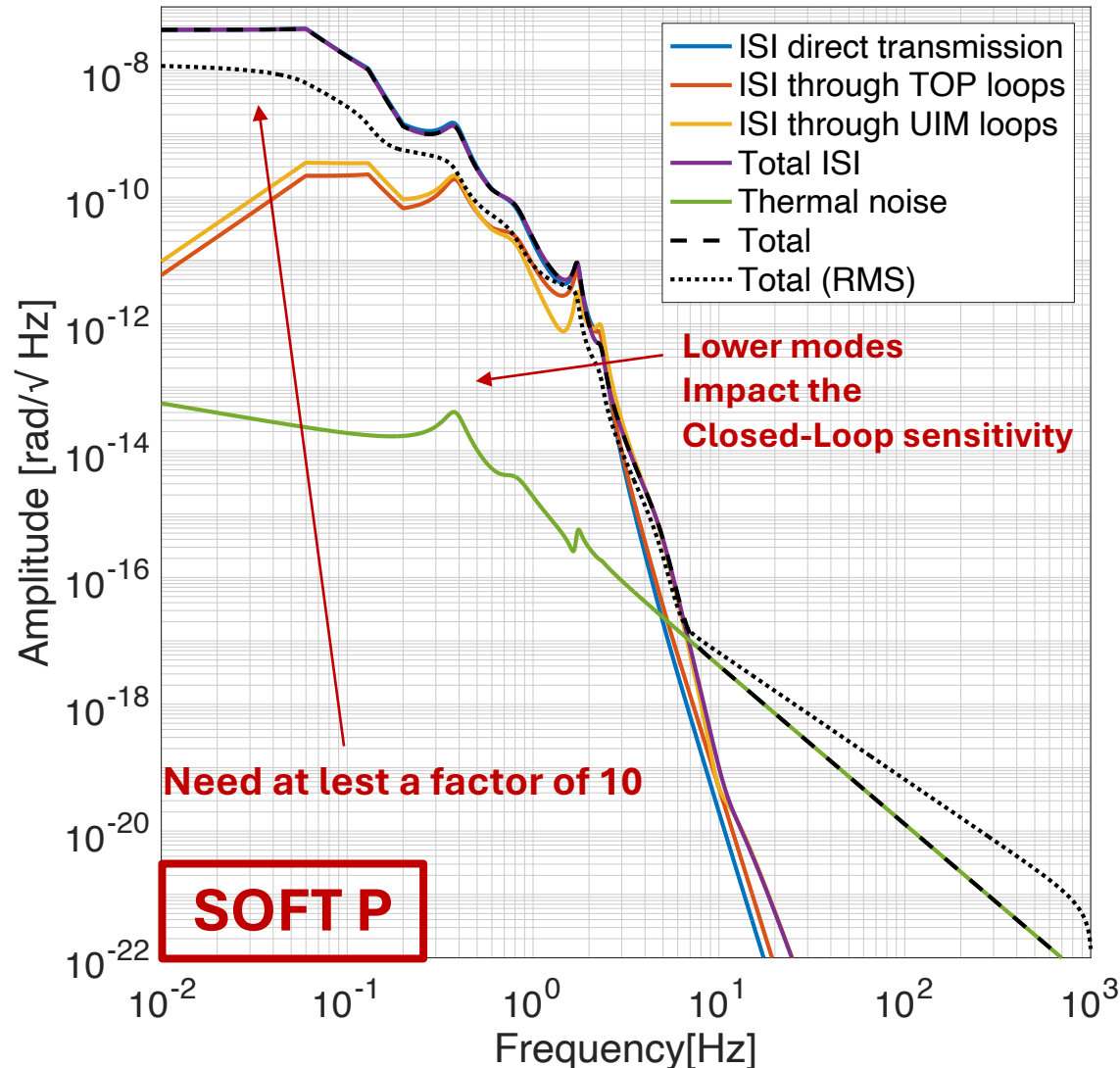
Soft DOF

- We assume a WFS noise of $1\text{e-}15 \text{ rad/Hz}^{1/2}$. Order of magnitude based on [G2100751](#)

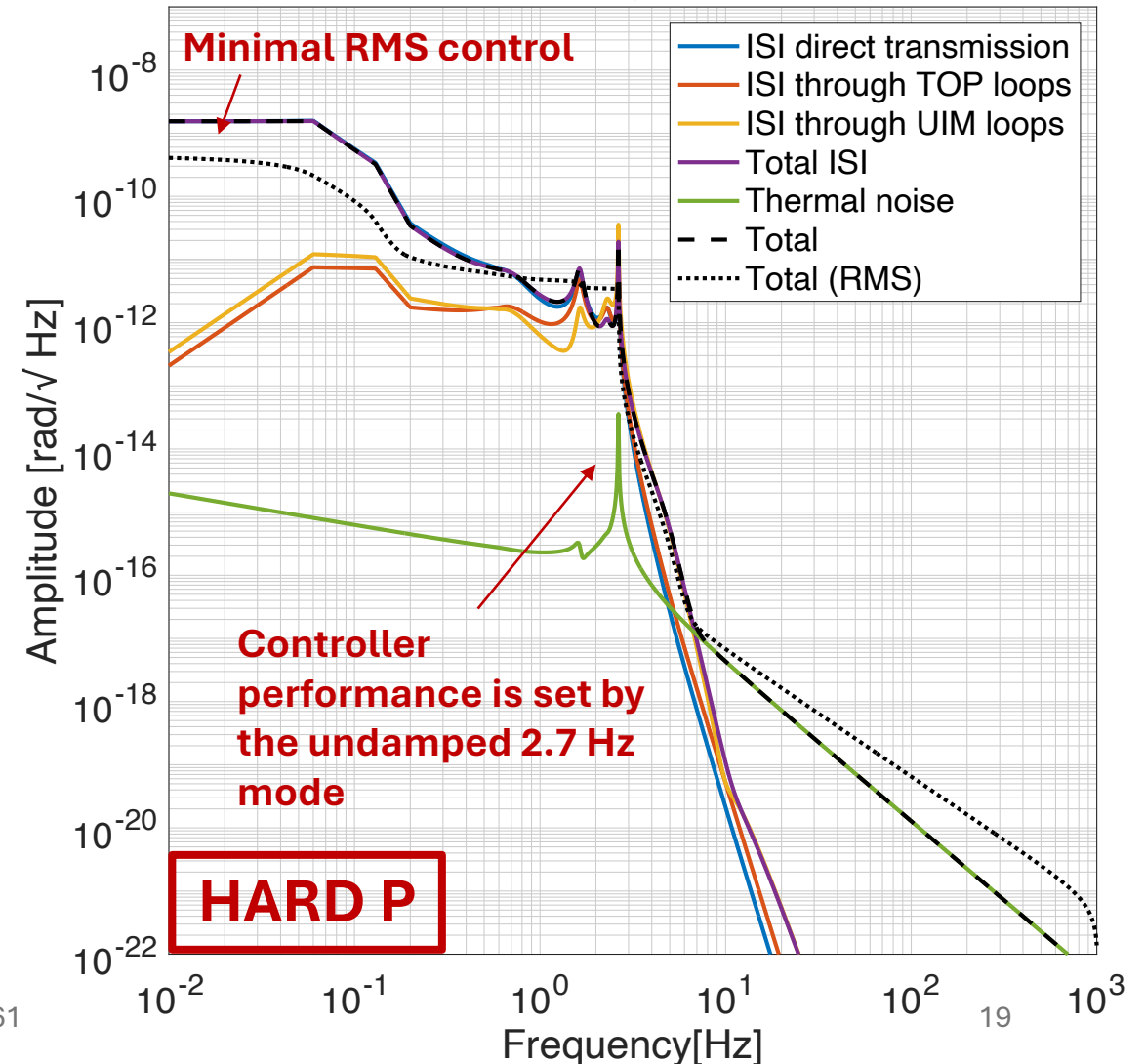
Pitch ASC (1.5 MW):

Open-Loop Motion

Single suspended cavity noise Budget (soft P)

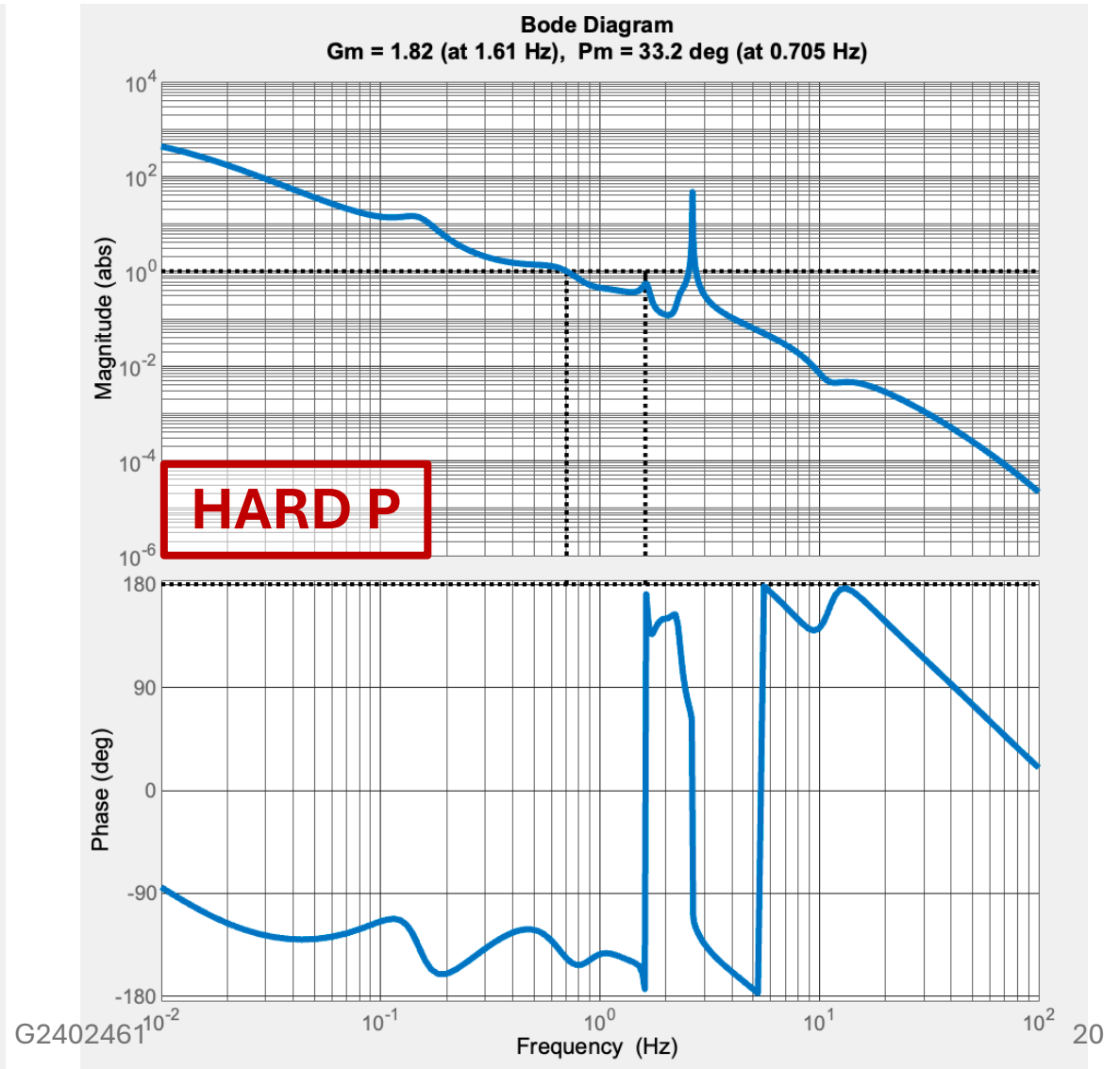
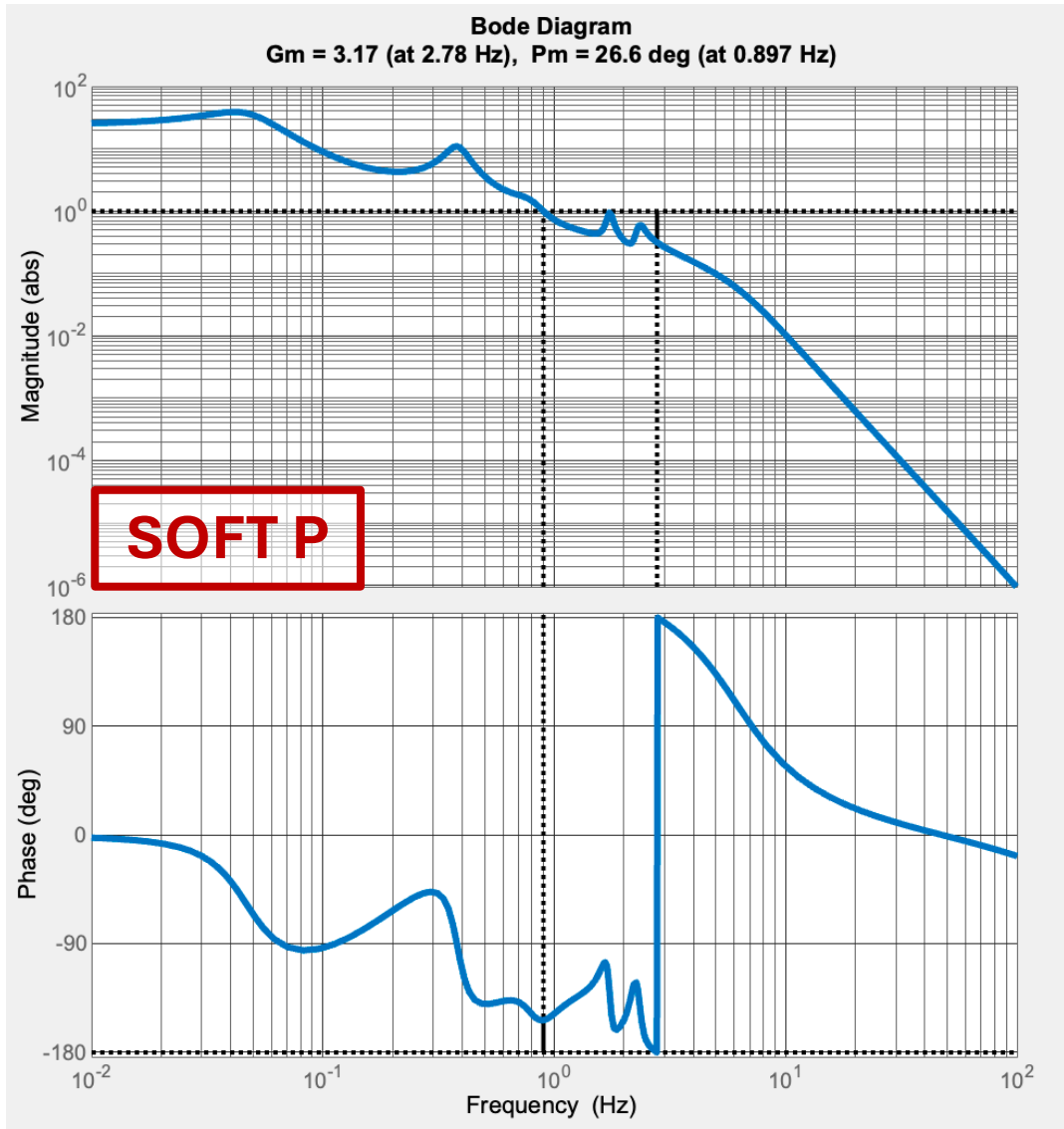


Single suspended cavity noise Budget (hard P)

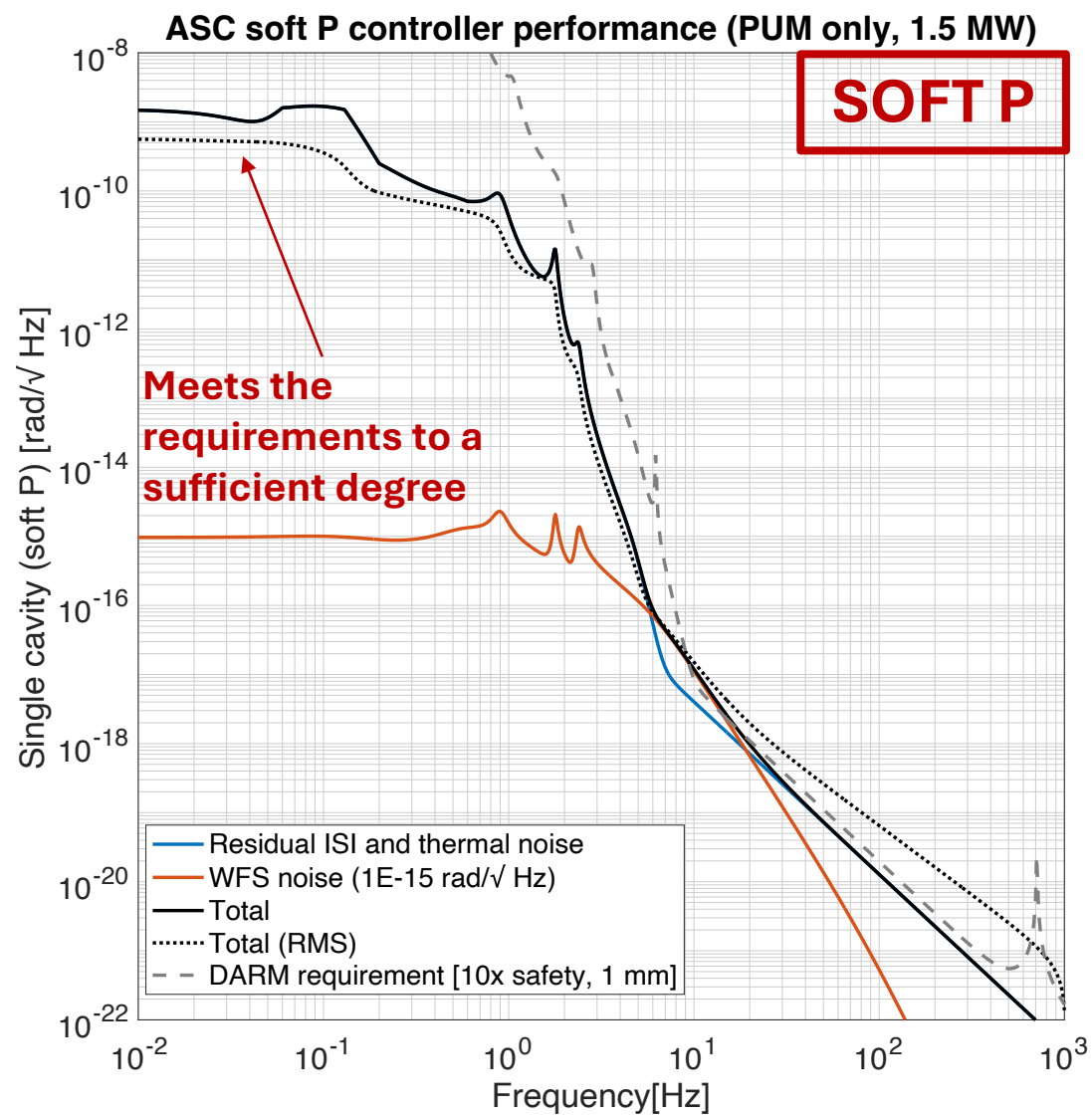


Pitch ASC (1.5 MW):

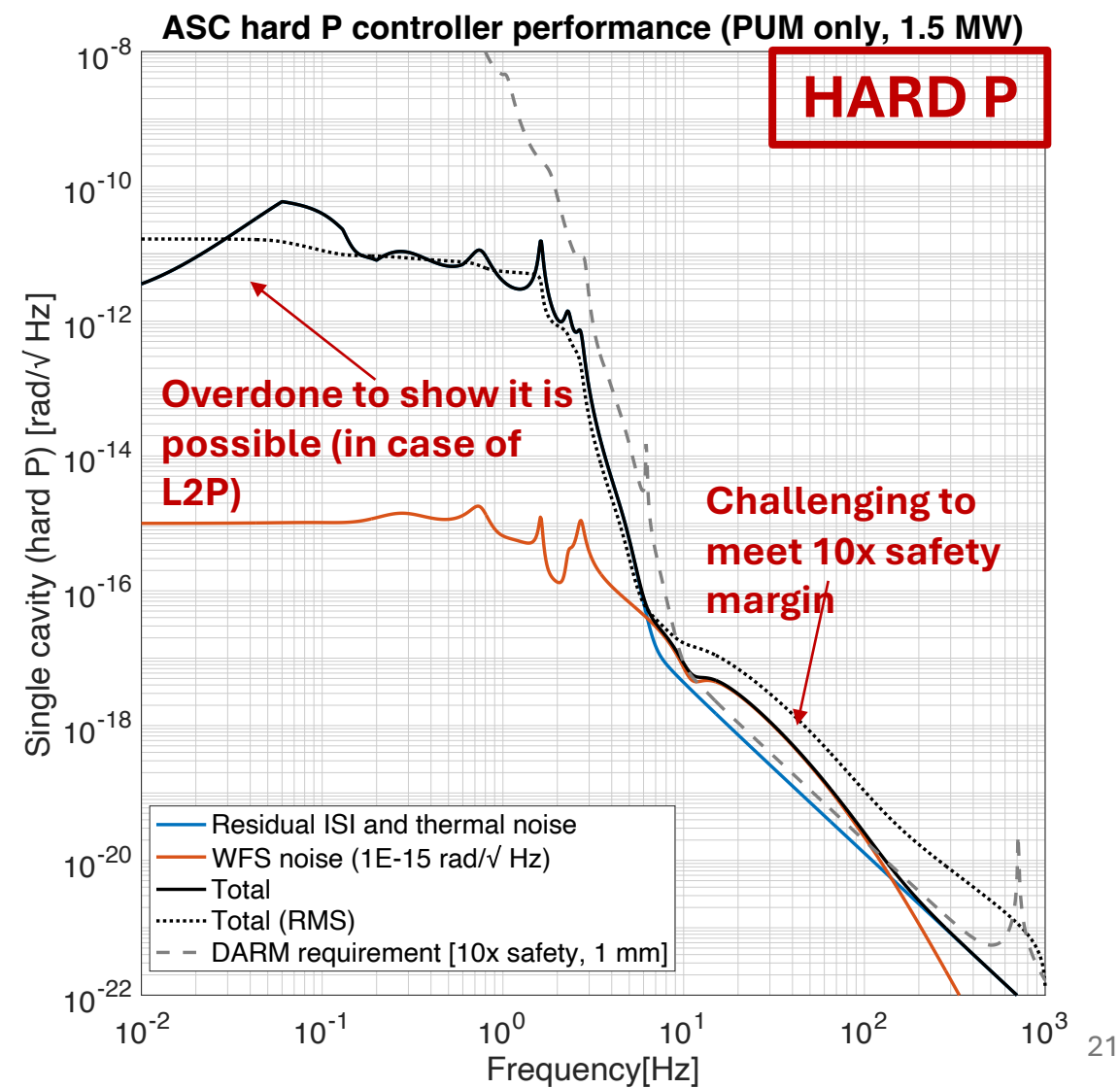
Open-Loop Gains



Pitch ASC (1.5 MW):

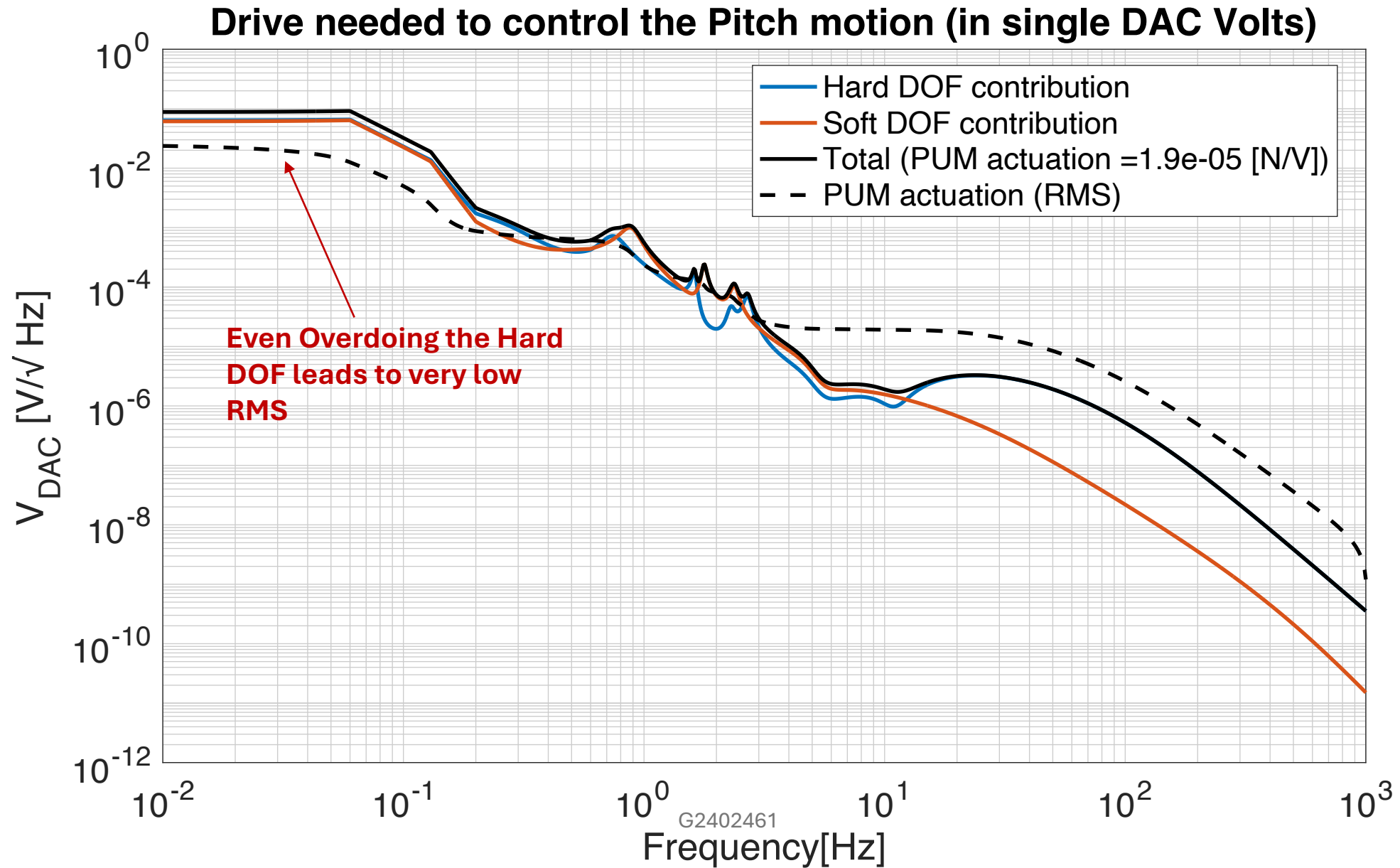


Closed-Loop Motion



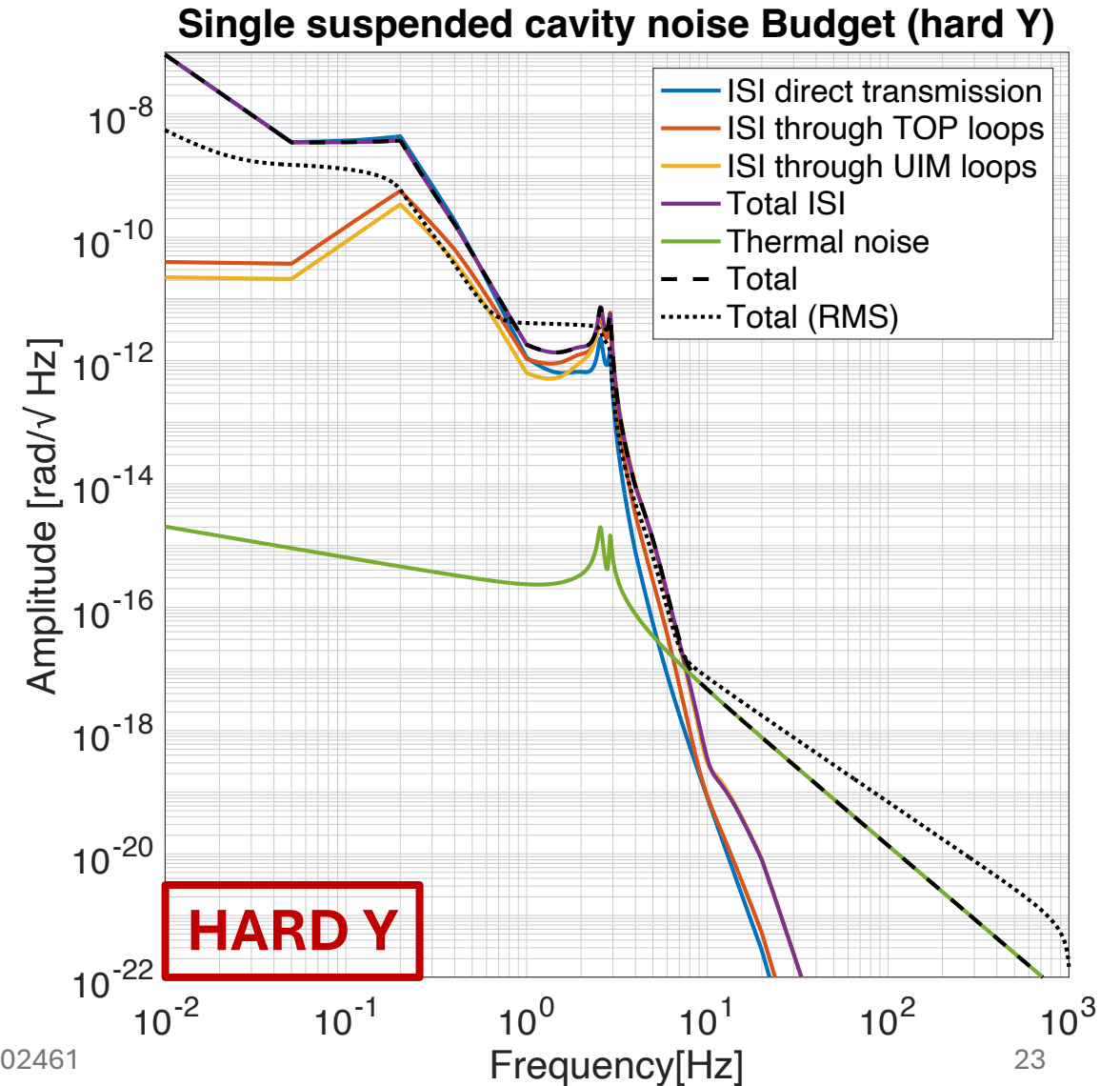
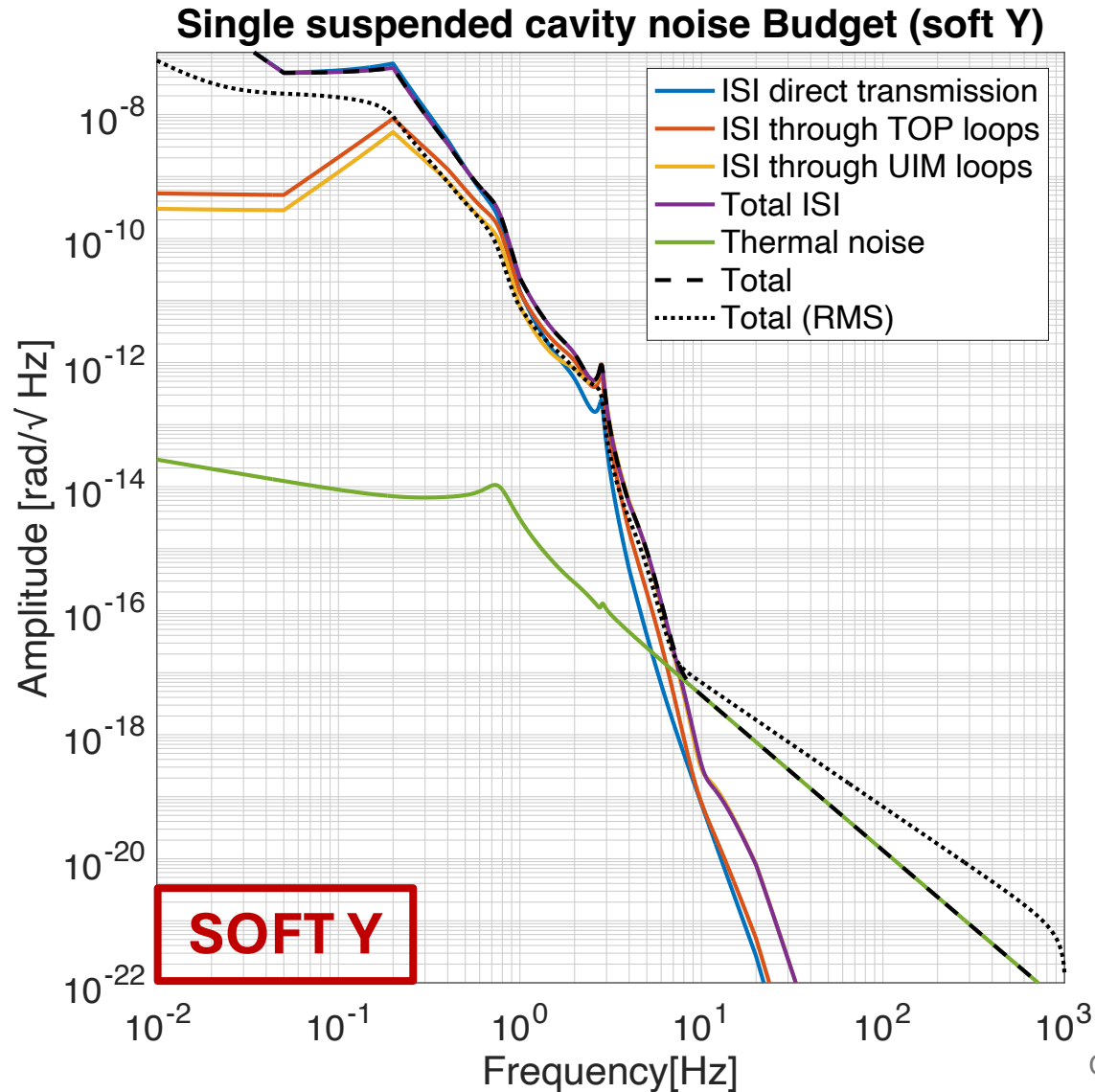
Pitch ASC (1.5 MW):

Upper-Limit DAC volts



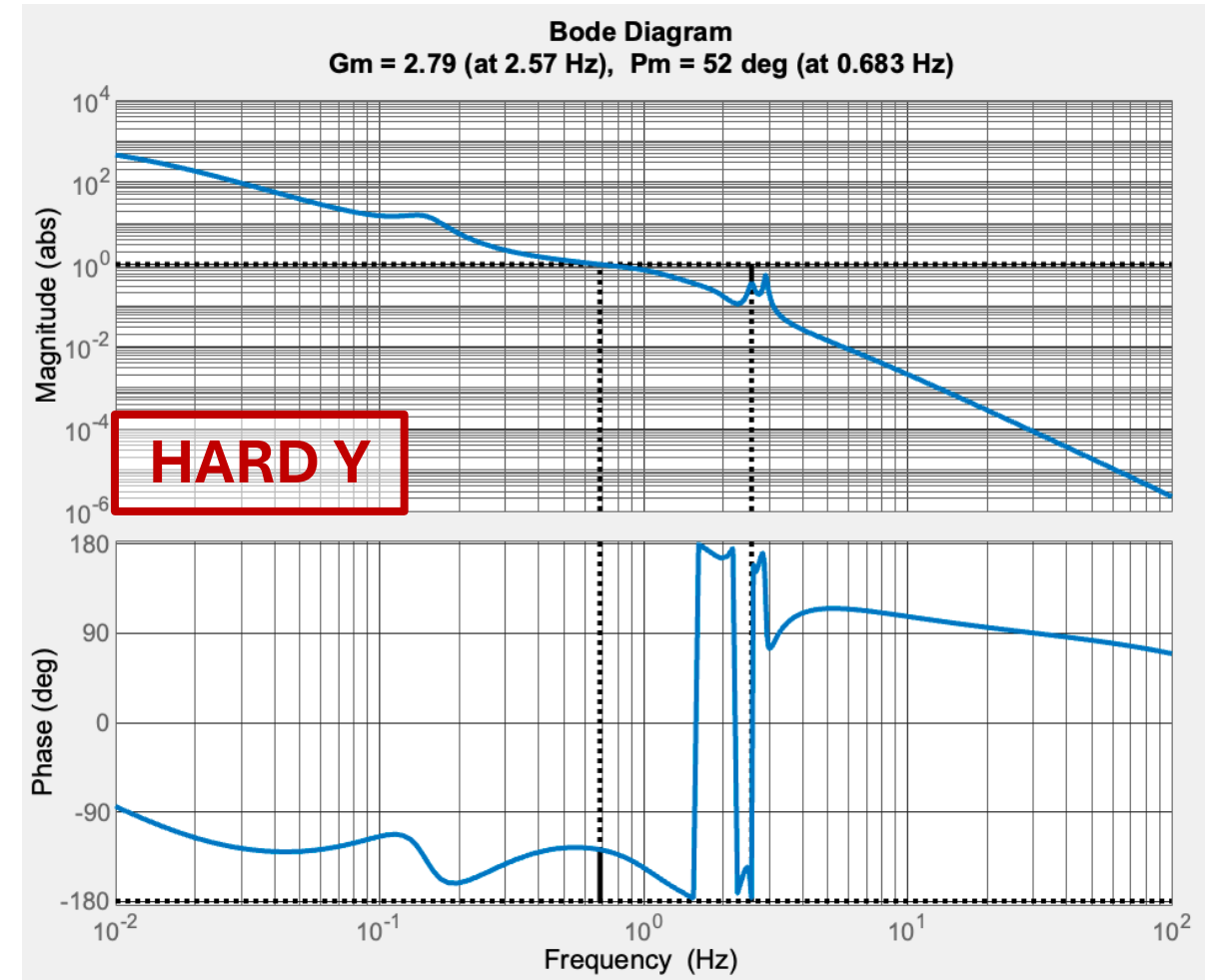
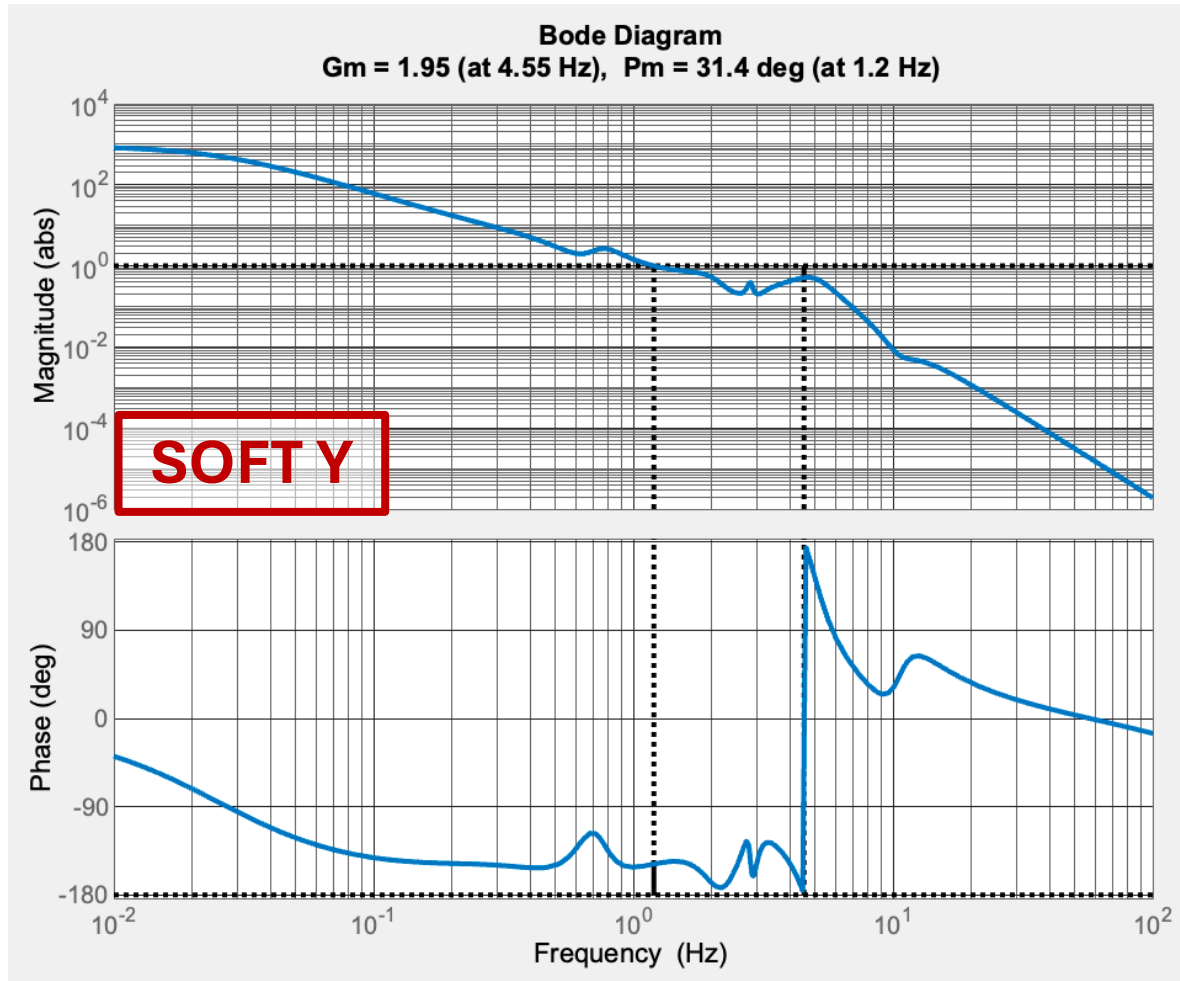
Yaw ASC (1.5 MW):

Open-Loop Motion

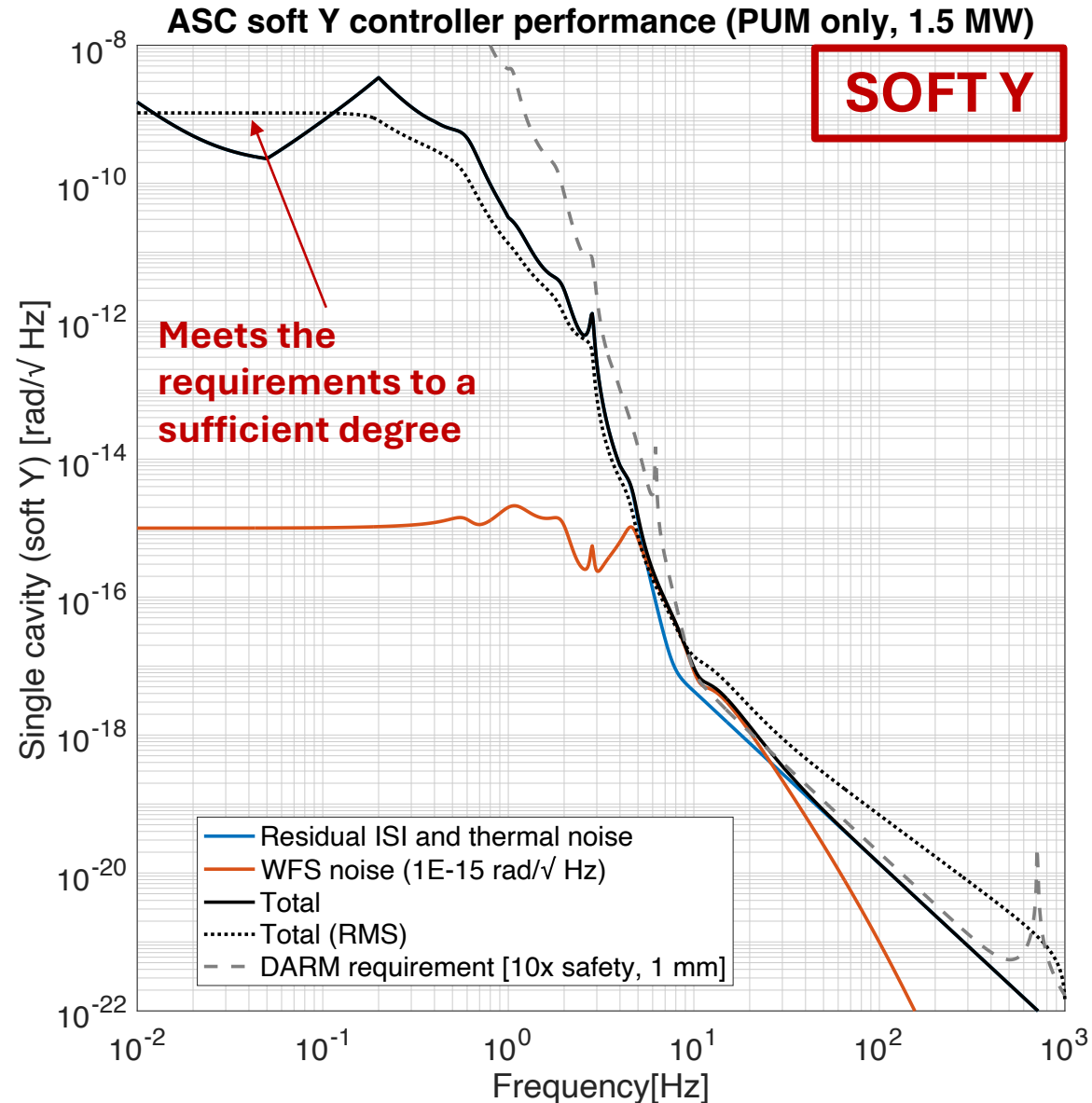


Yaw ASC (1.5 MW):

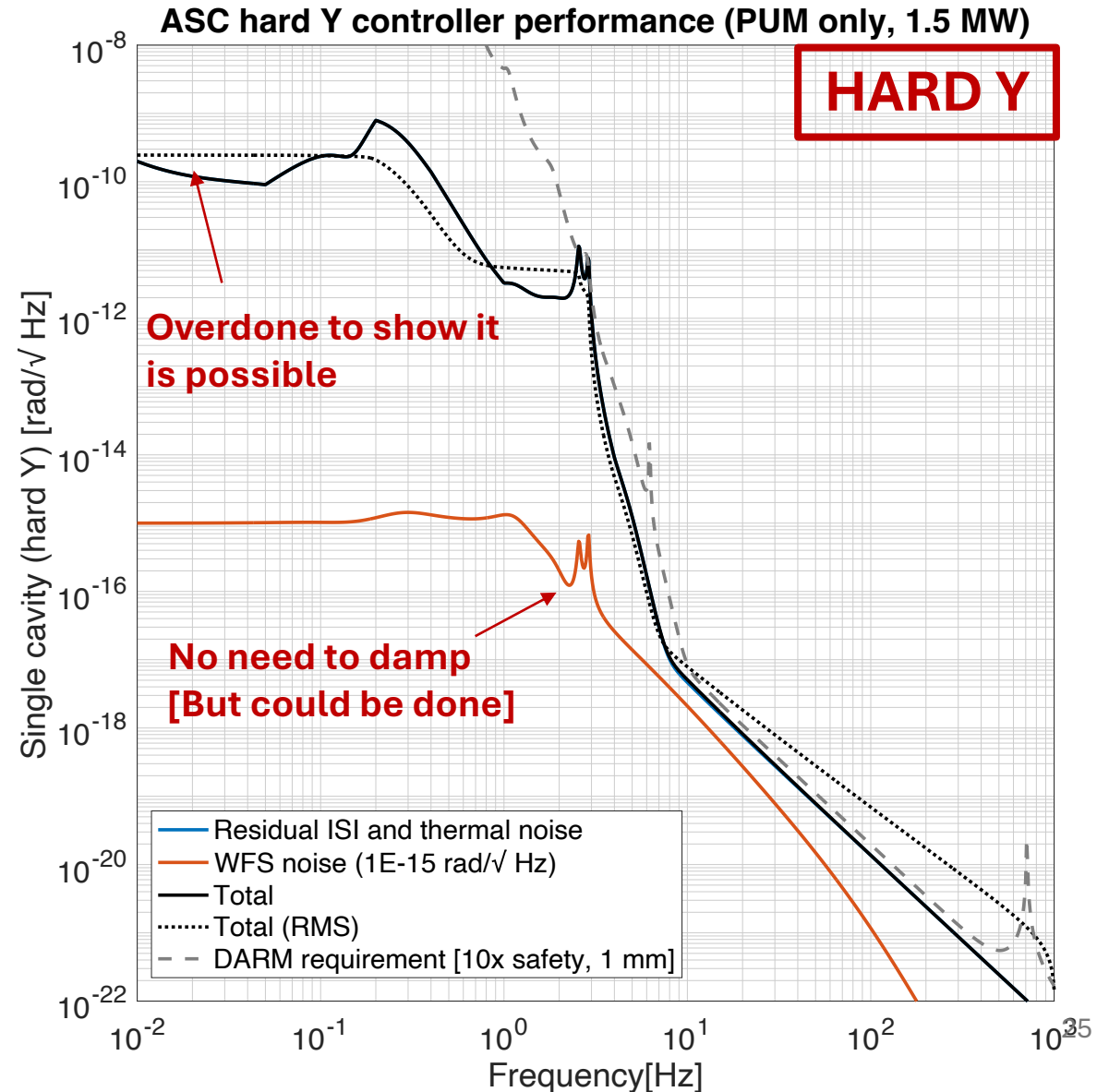
Open-Loop Gains



Yaw ASC (1.5 MW):

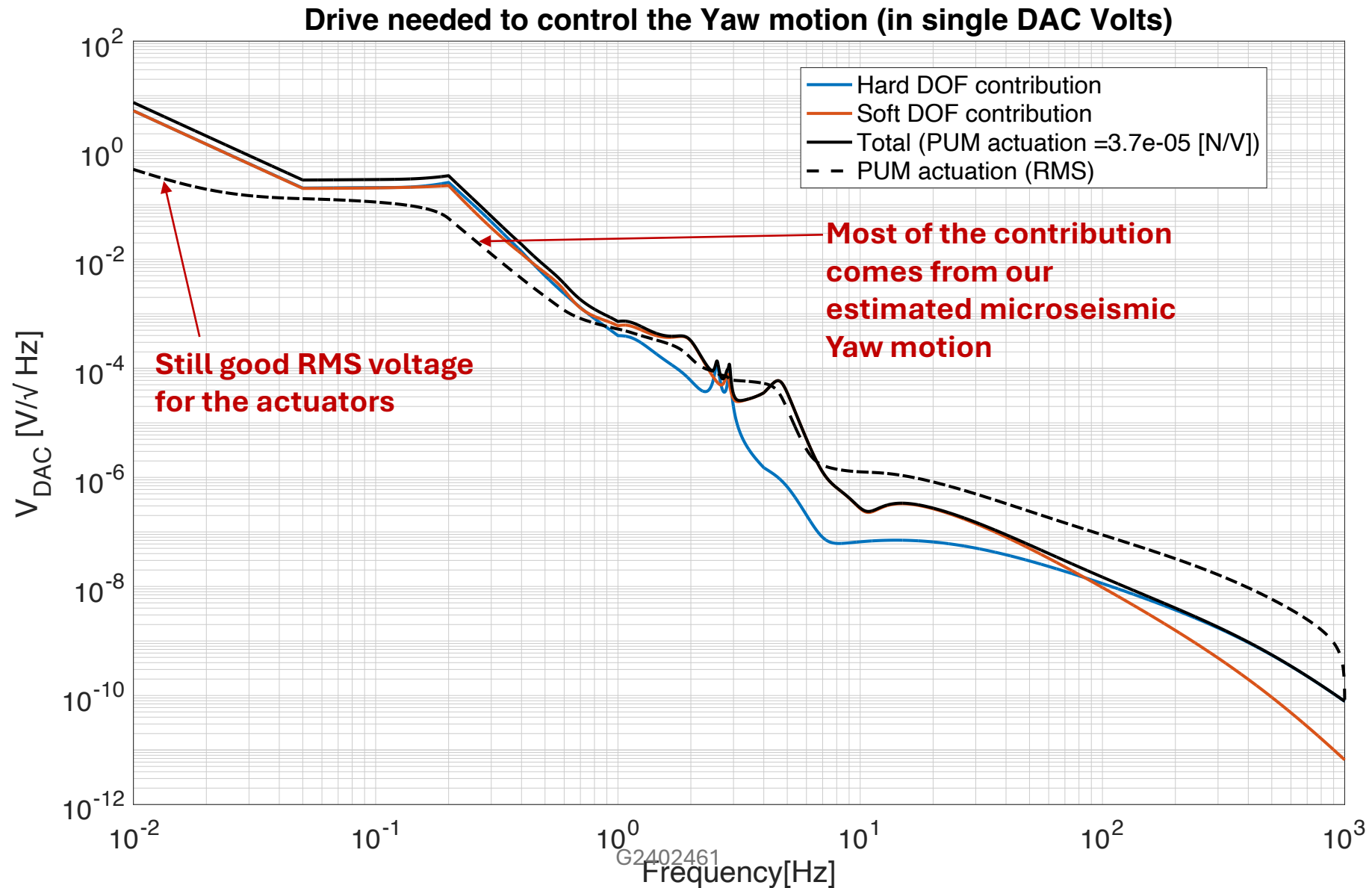


Closed-Loop Motion



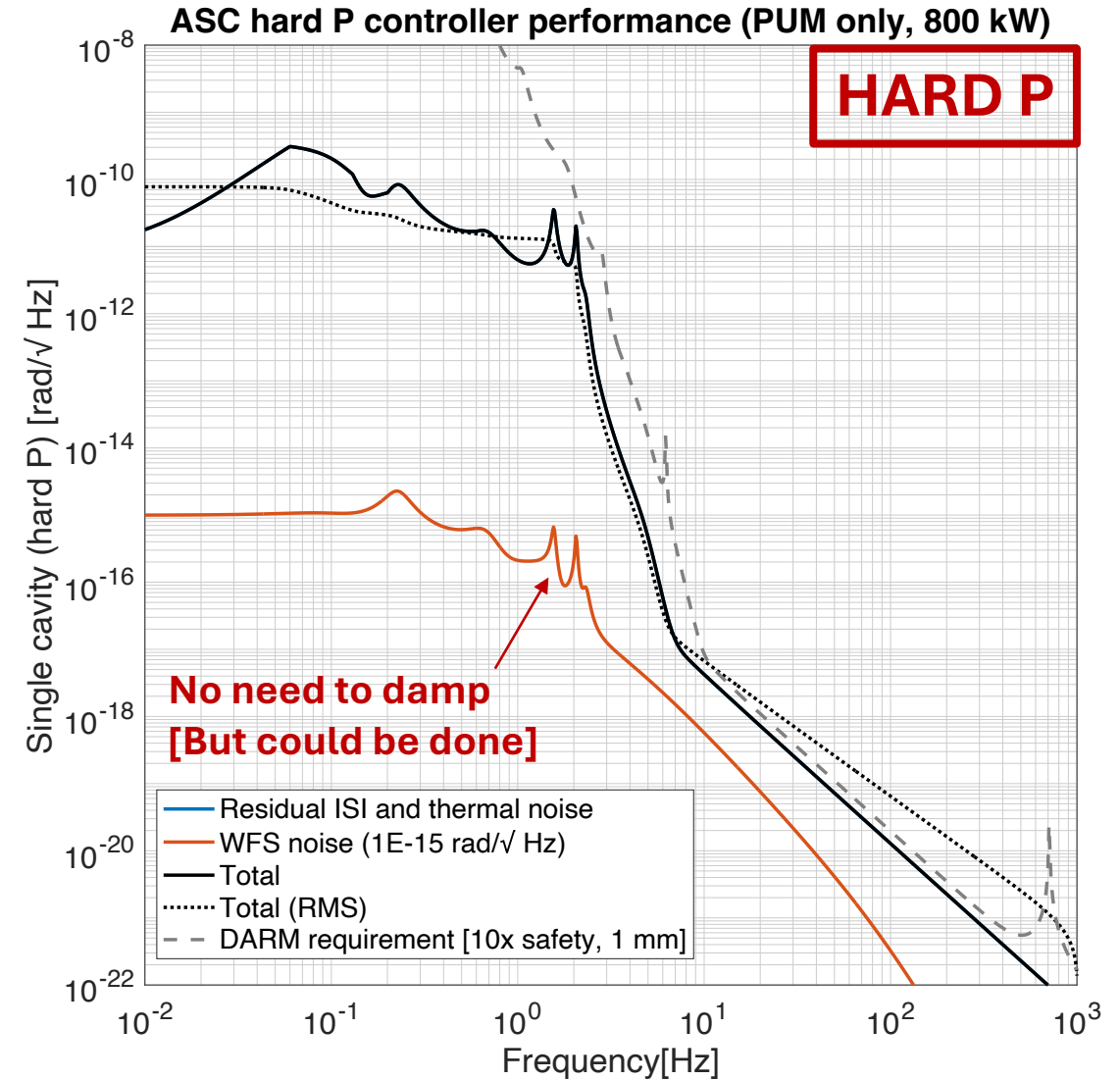
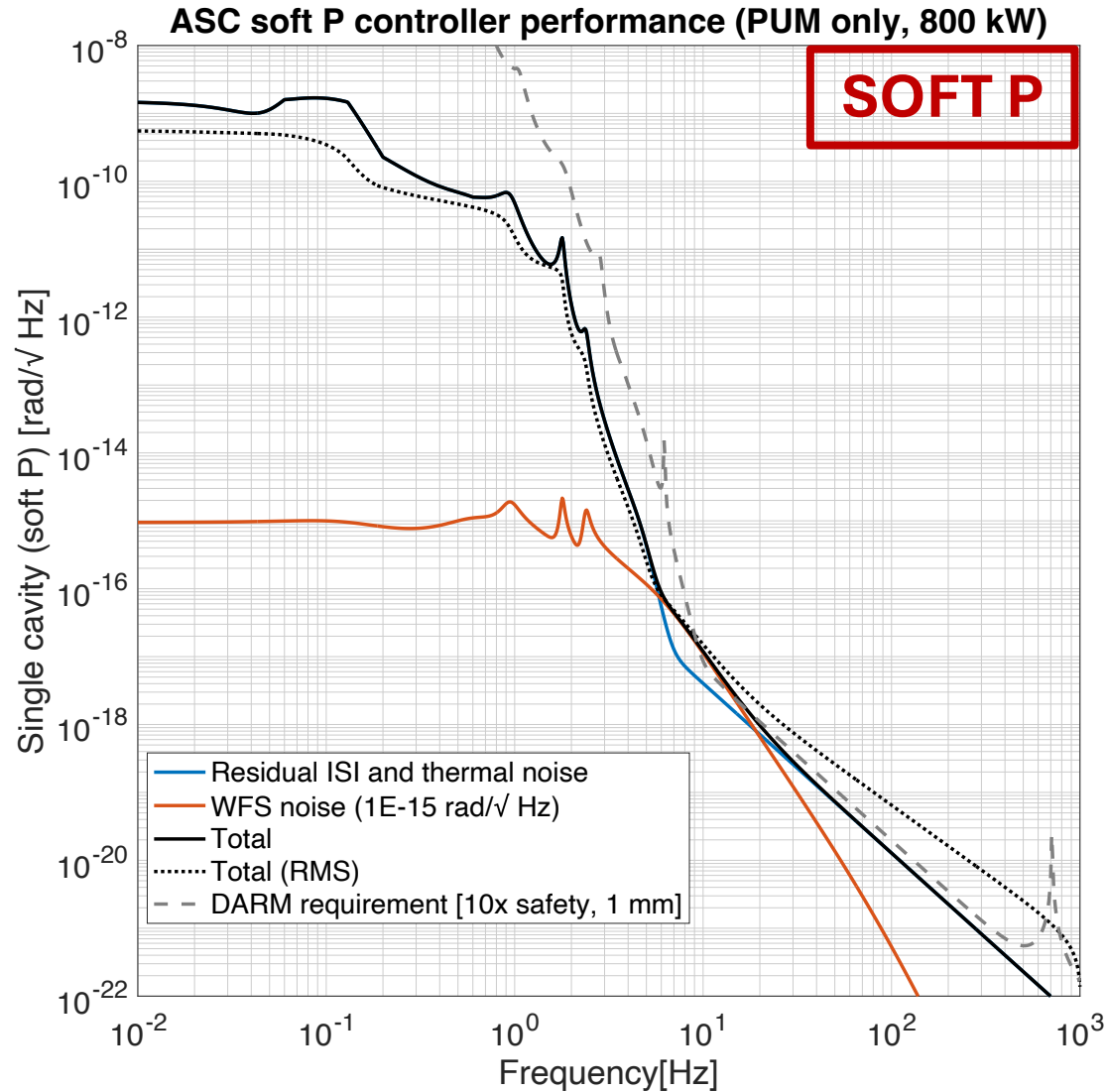
Yaw ASC (1.5 MW):

Upper-Limit DAC volts

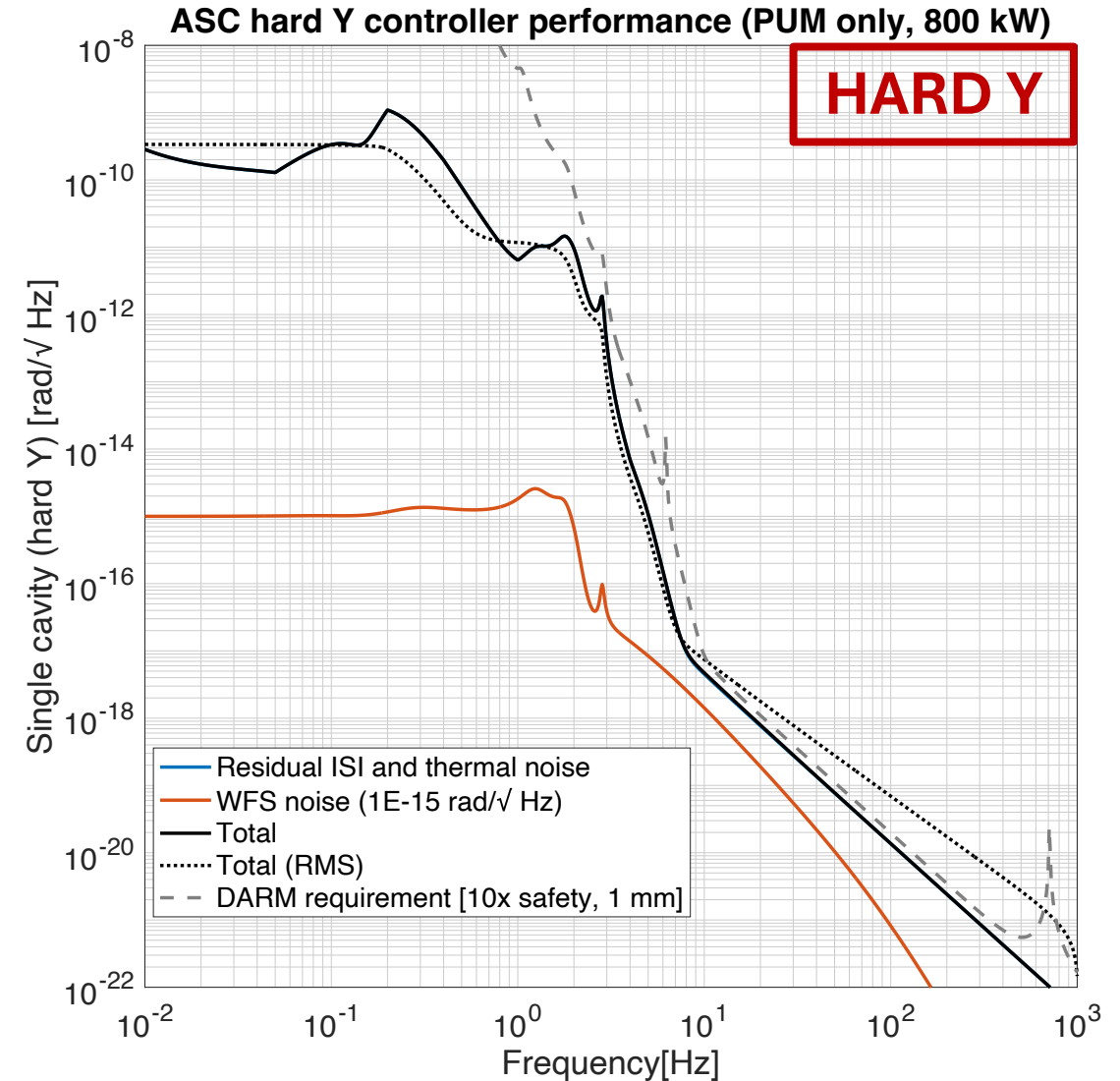
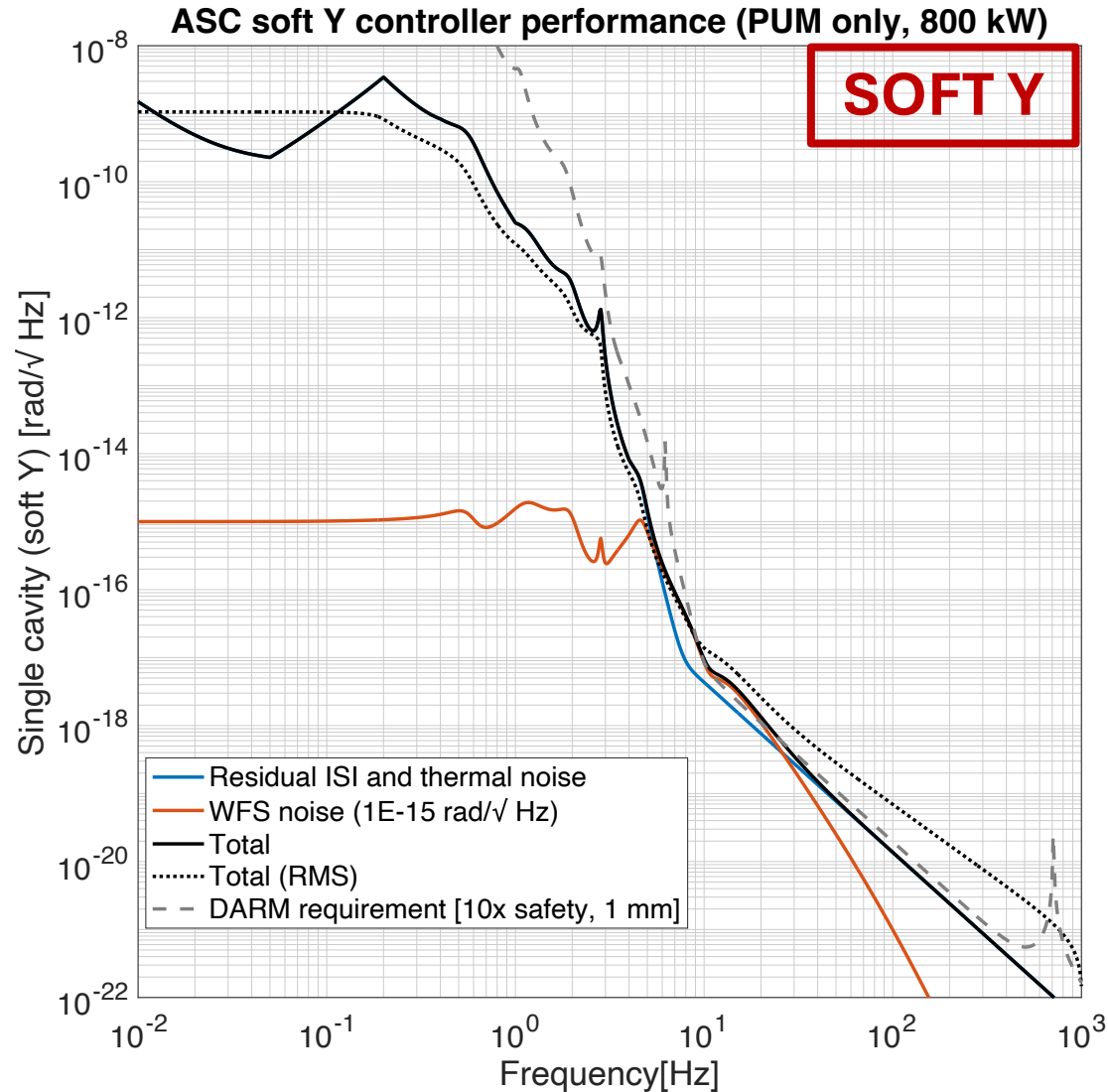


What about ASC at lower powers?

800 kW ASC performance



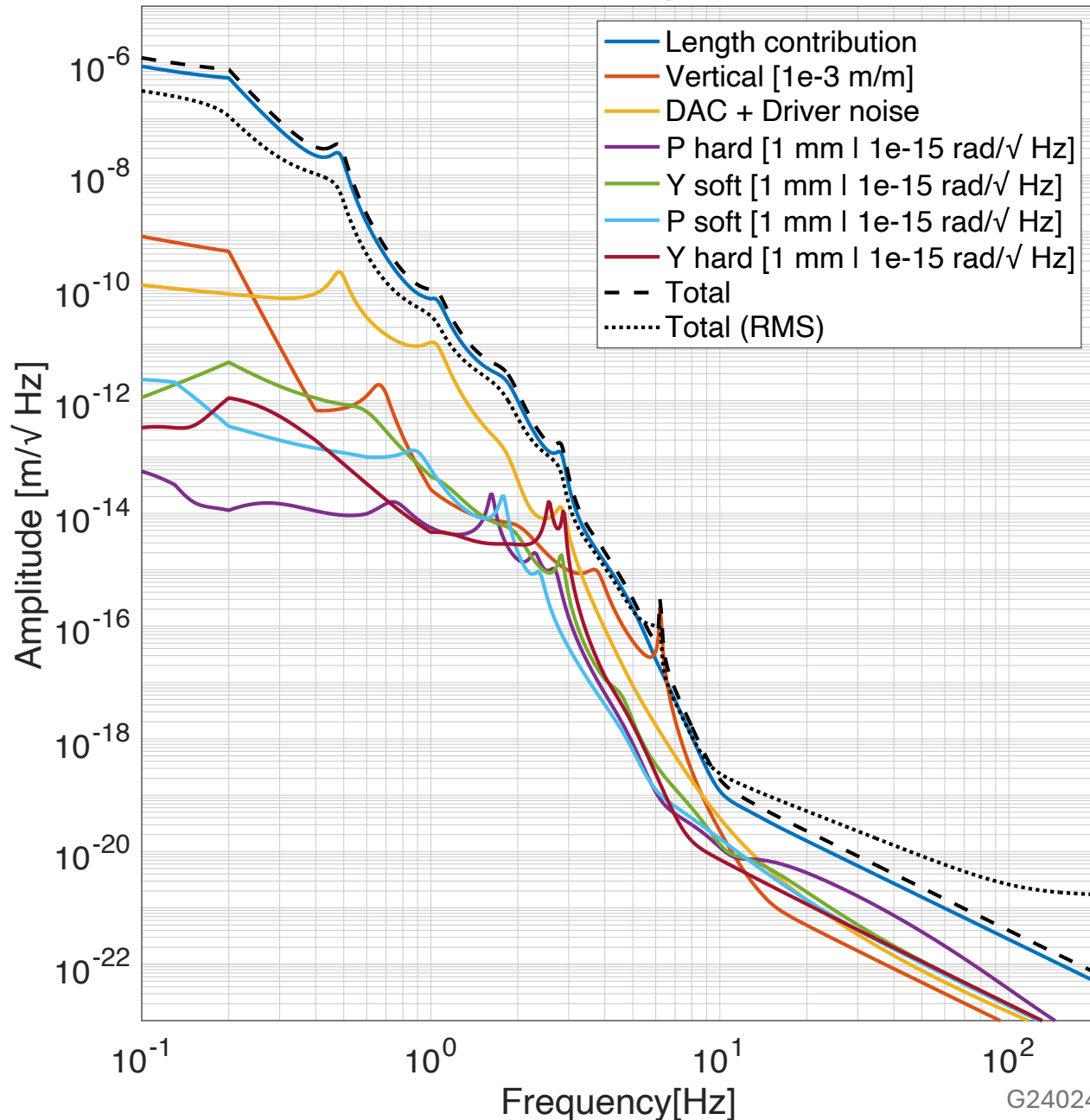
800 kW ASC performance



ASC takeaways (for now)

- At lower powers (less than 1 MW) it should be possible to damp the hard mode locally, simplifying the ASC loops.
- Building a reasonable controller for the well-damped angular plants (< 1 MW) is doable.
- At lower powers, the limiting factor is likely to be our ability to control the soft mode RMS.
- At 1.5 MW we must resort to more complicated controllers to deal with the hard Pitch degree of freedom.

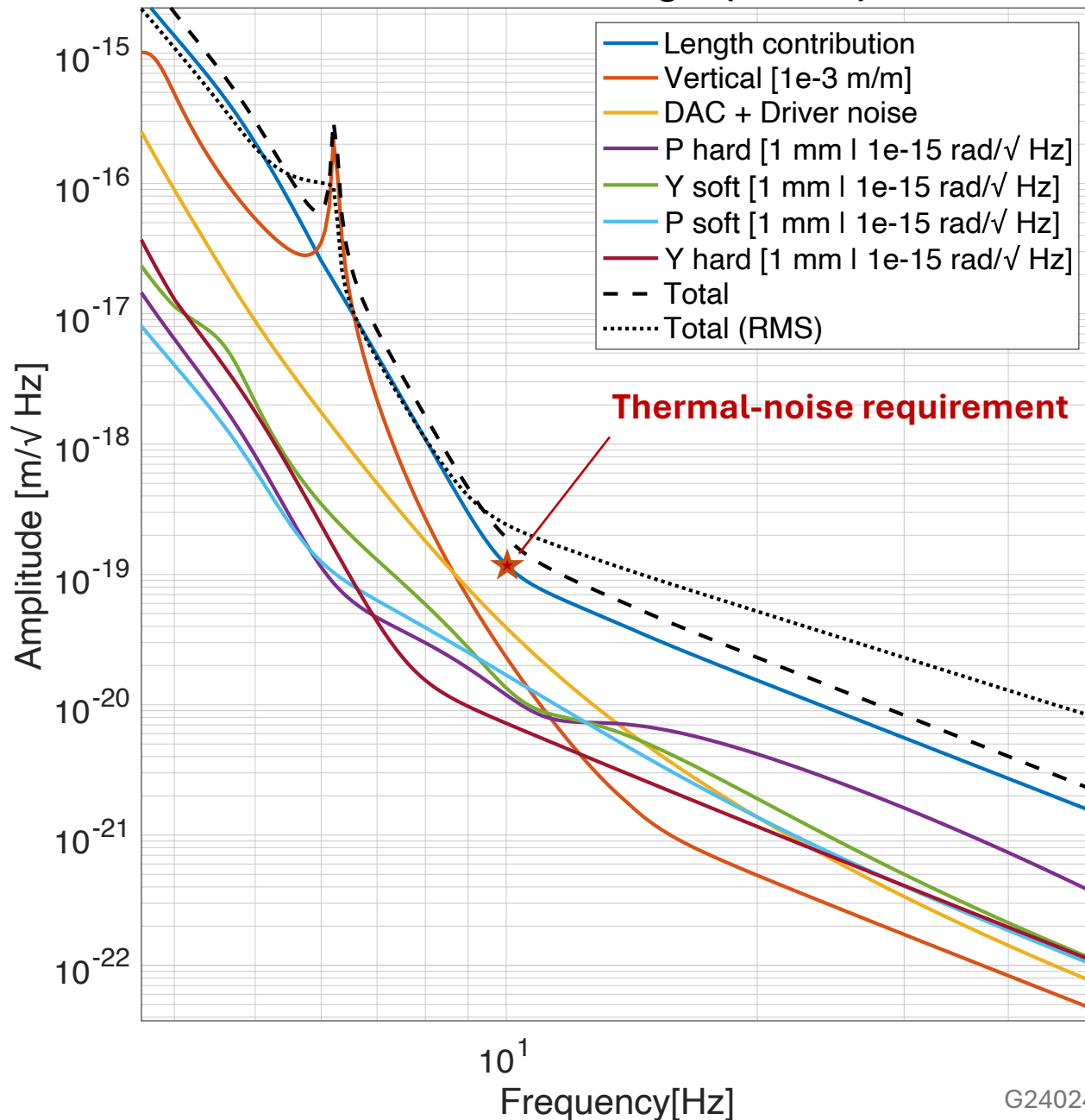
DARM noise Budget (1.5 MW)



Let's put it all together into a noise budget

- The main contributors to the noise that can be mitigated are:
 - The TST stage DAC noise
 - The P hard dof due to the undamped mode
 - The Y hard dof due to the poorly damped mode

DARM noise Budget (1.5 MW)



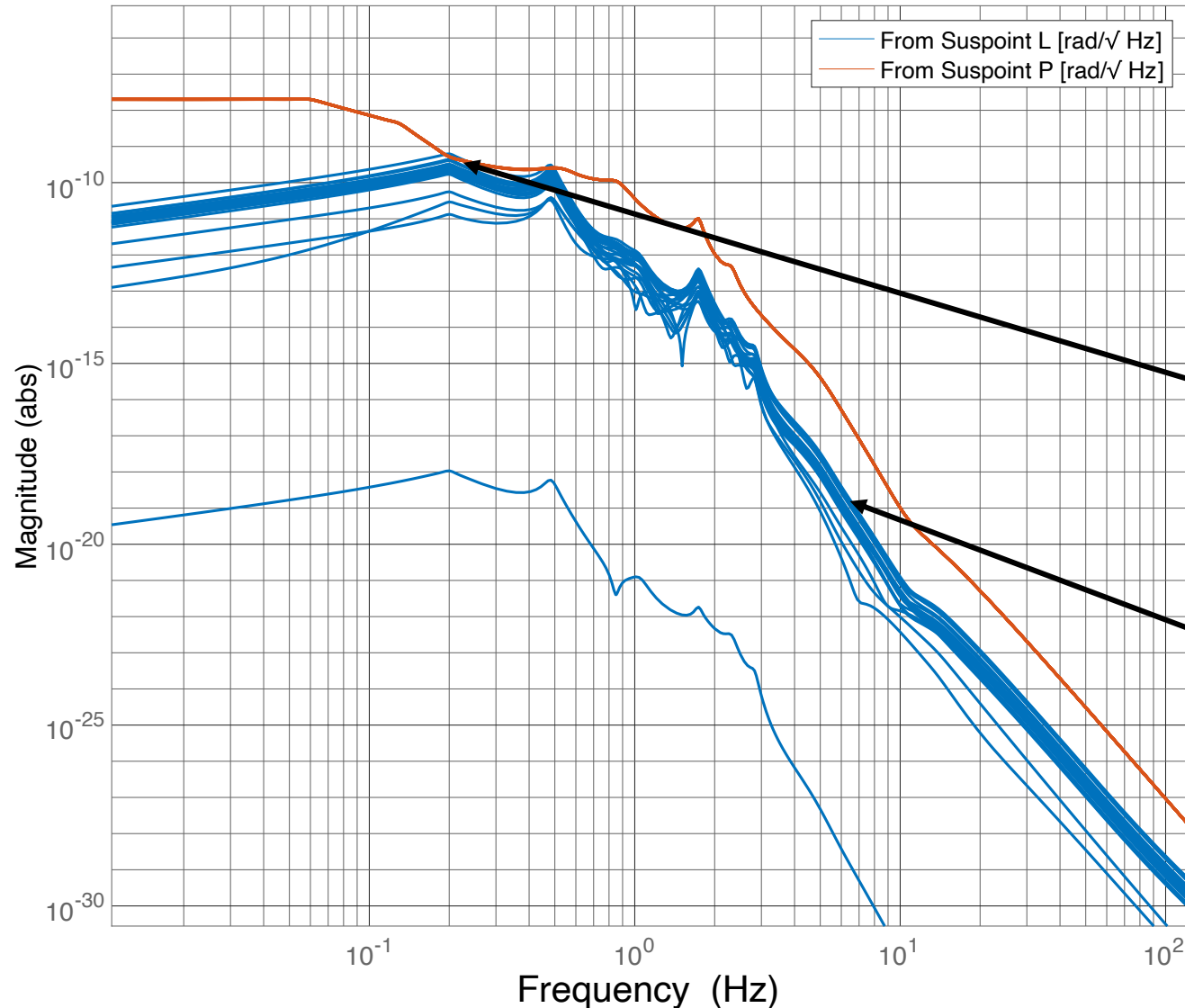
Let's put it all together into a noise budget

- The main contributors to the noise that can be mitigated are:
 - The TST stage DAC noise
 - The P hard dof due to the undamped mode
 - The Y hard dof due to the poorly damped mode
- Note:** This assumes the scenario where the WFS noise is at the $1\text{e-}15\text{ rad/Hz}^{1/2}$.
- Note:** This assumes the dofs are well damped and decoupled

Caveats

- How much uncertainty can we tolerate on this design?
- Can we reduce the actuator noise?
- How good do the sensors need to be?

Pitch of the TST stage for uncertain d-values unc=250 microns



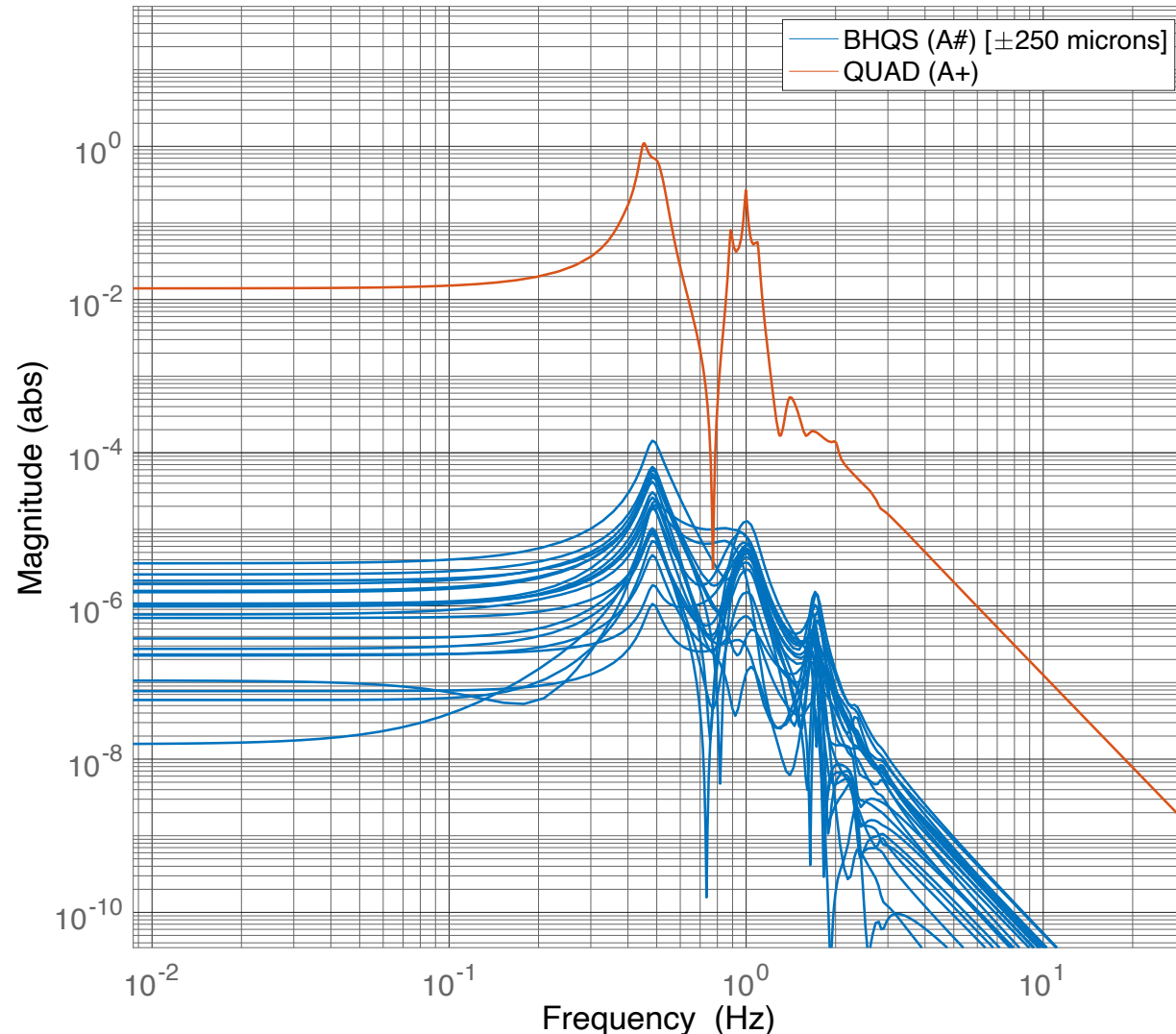
How much uncertainty?

Length-to-pitch cross-coupling From ISI

- 250 μm tolerance is enough to ensure the Length-to-Pitch coupling is lower everywhere except for the microseism.
- The Length-to-Pitch coupling in this case is 100 times lower above the resonances, even when including the Length controls

Percent change on the TST-TST L and P Open Loop Gains for uncertain d-values
unc=250 microns

From: dampedout.tst.disp.L To: dampedout.tst.disp.P



How much uncertainty?

- 250 microns keeps the loop interaction on the 0.01% level.
- 1% is the limit of what we would consider “decoupled” (about 3cm for the BHQS)

In a 2x2 Multi-input / Multi-output system

L2L	P2L
L2P	P2P

the fraction

$$\frac{(L2P)(P2L)}{(L2L)(P2P)}$$

represents the fractional interaction between two **high-gain** Single-input / Single-output loops like the ones used for interferometric controls.

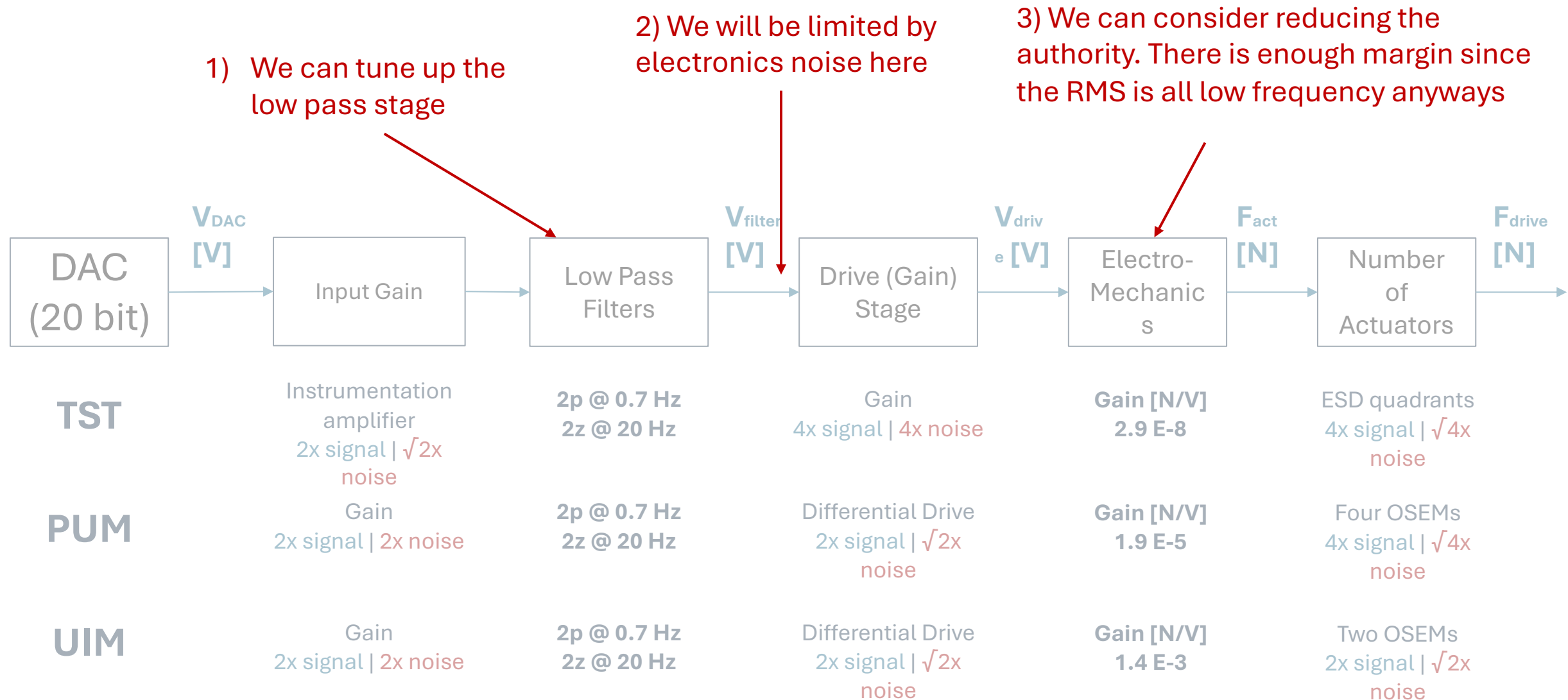
Caveats

- How much uncertainty can we tolerate on this design?

250 microns on the d-values (Limited by microseism)

- Can we reduce the actuator noise?
- How good do the sensors need to be?

About the actuator noise



Caveats

- How much uncertainty can we tolerate on this design?

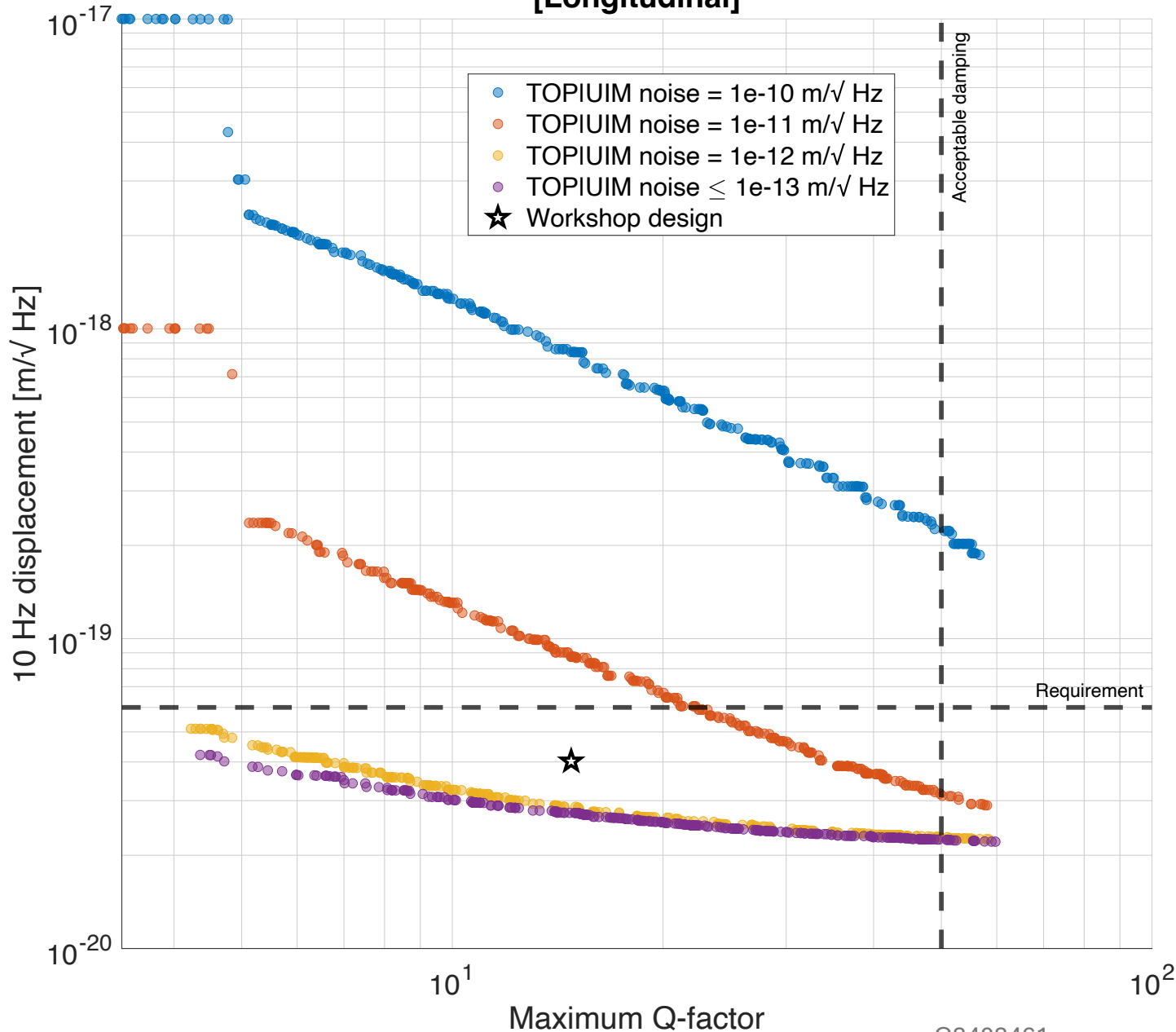
250 microns on the d-values (Limited by microseism)

- Can we reduce the actuator noise?

Yes - There is at least a factor of 3 margin to reduce the ESD's authority without saturating the DACs
(most of the actuation RMS happens at the UIM)

- How good do the sensors need to be?

Pareto front for local damping [Longitudinal]



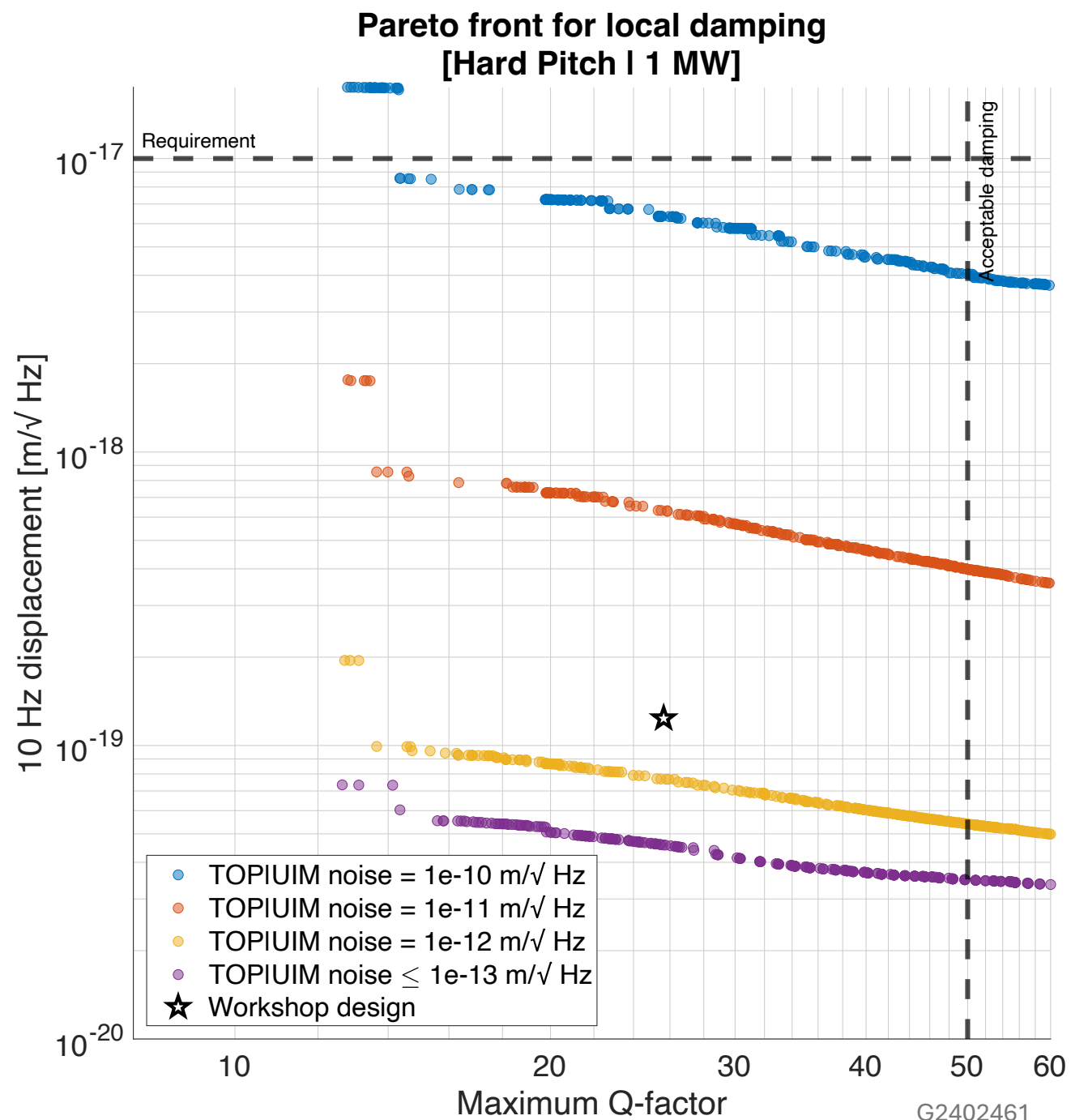
What noise for sensors?

Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Longitudinal:

- Any sensor performing better than $1 \text{ e-}13 \text{ m}/\text{Hz}^{1/2}$ will be limited by ISI noise.
- Sensors with noise above $3 \text{ e-}11 \text{ m}/\text{Hz}^{1/2}$ are unlikely to meet our requirements
- A performance better than $5 \text{ e-}12 \text{ m}/\text{Hz}^{1/2}$ is enough to rival the idealized calculations.



What noise for sensors?

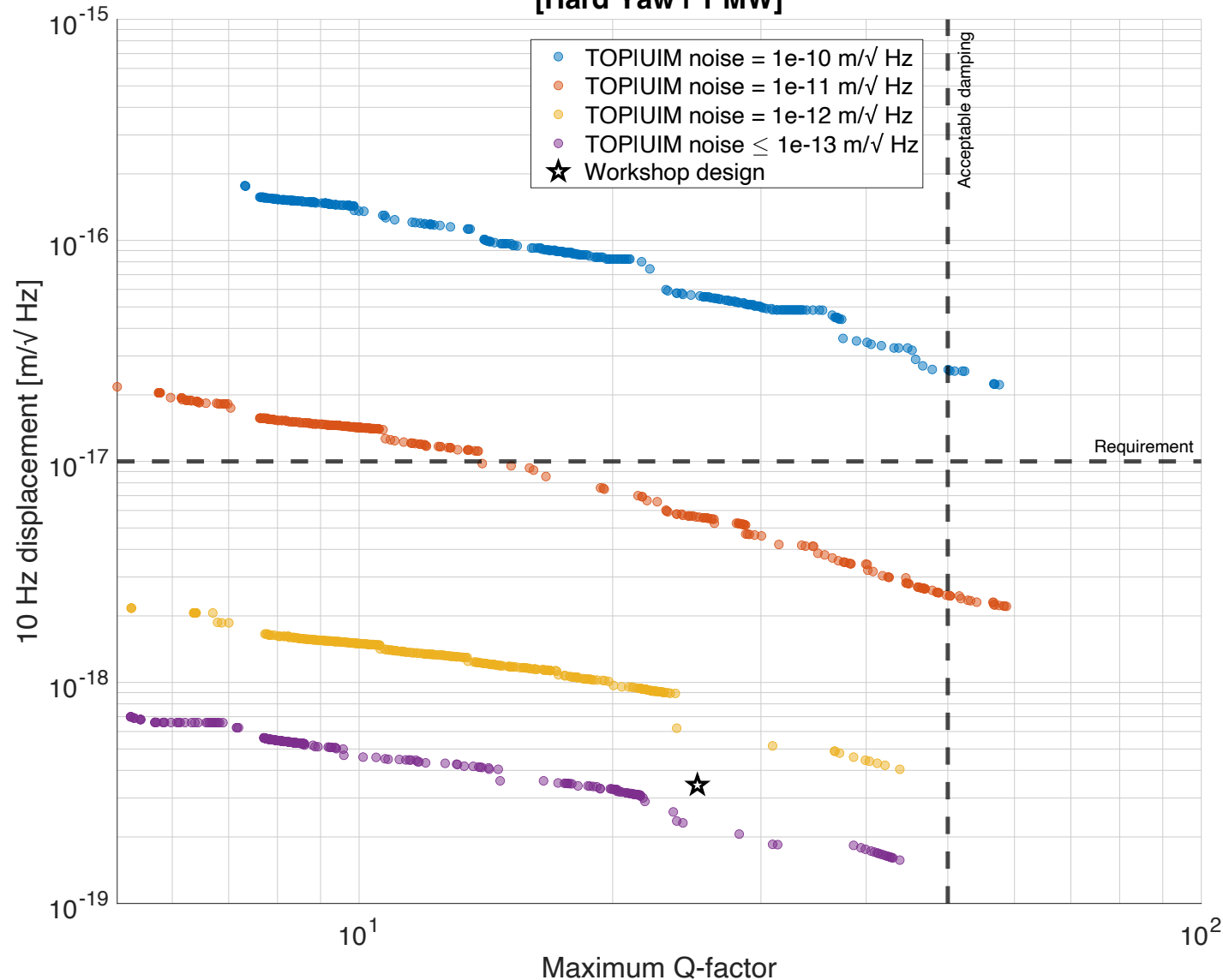
Assumed controller:

2 real zeros at 0 Hz, 2 real poles , elliptic filter for rolloff.

For Pitch:

- Up to 1 MW, we should be able to pick sensors up to $1e-10$ m/Hz^{1/2}.
- To get some margin, we would still prefer something below $1e-11$ m/Hz^{1/2}.

Pareto front for local damping
[Hard Yaw | 1 MW]



What noise for sensors?

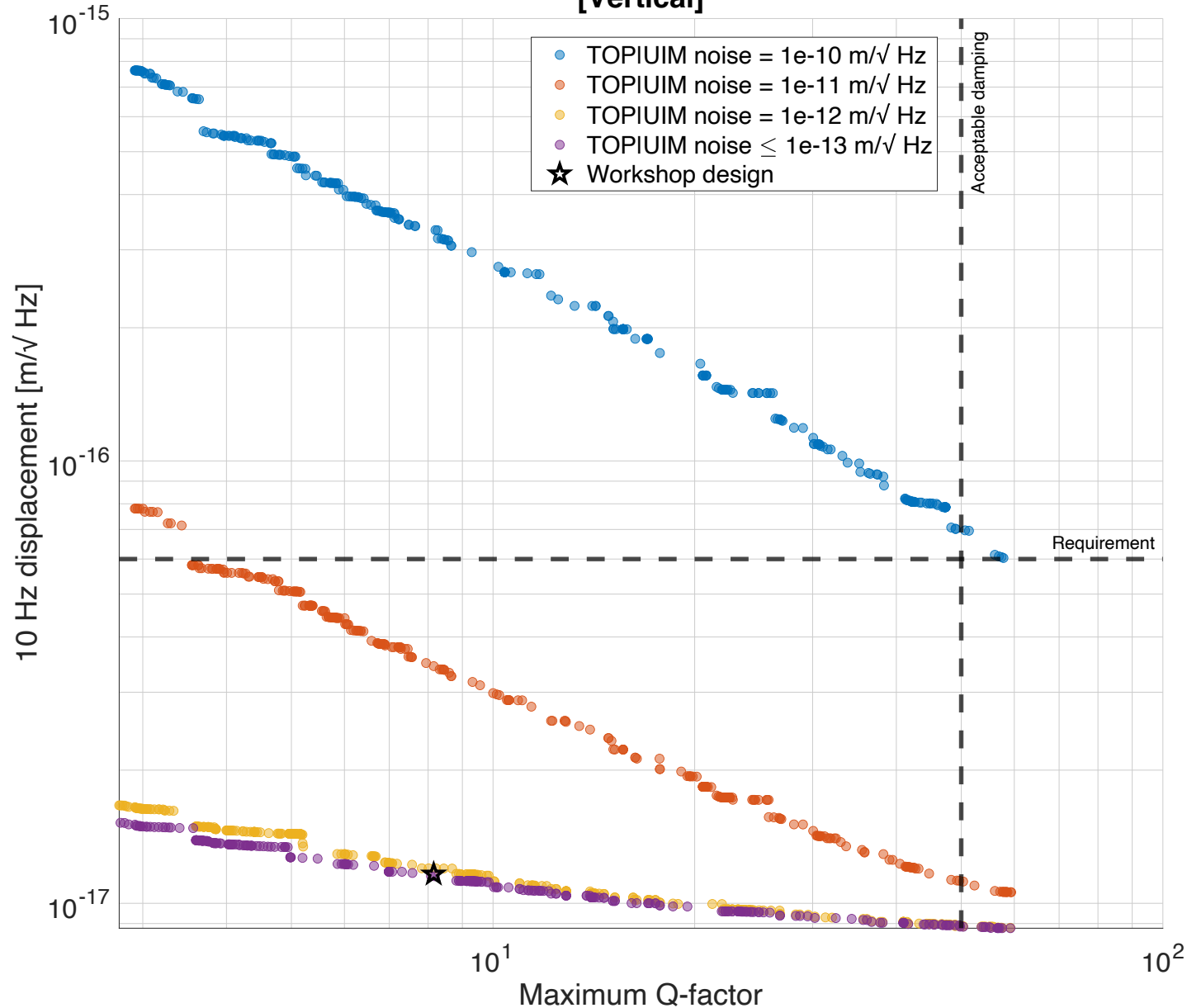
Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Yaw:

- We must use the UIM to aid with damping
- At 1 MW, we to damp the Yaw mode a sufficient amount, we want a sensor with noise below $1e-11$ m/Hz^{1/2}.

Pareto front for local damping [Vertical]



What noise for sensors?

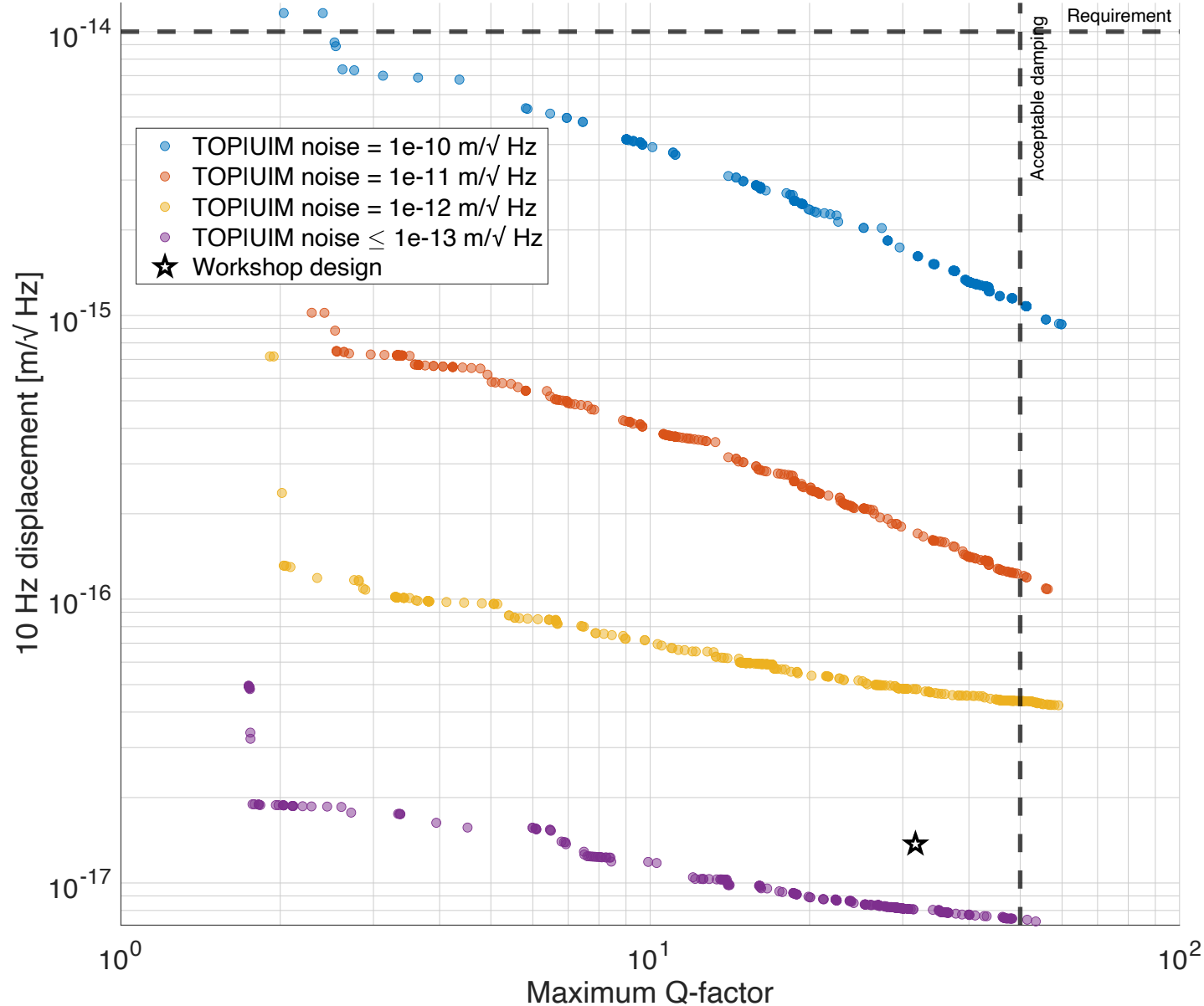
Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Vertical (excluding the bounce mode):

- Only the TOP mass is needed for good performance.
- A sensing noise lower than the $3\text{e-}11$ m/Hz^{1/2} would allow for a Q of around 20.

Pareto front for local damping [Roll]



What noise for sensors?

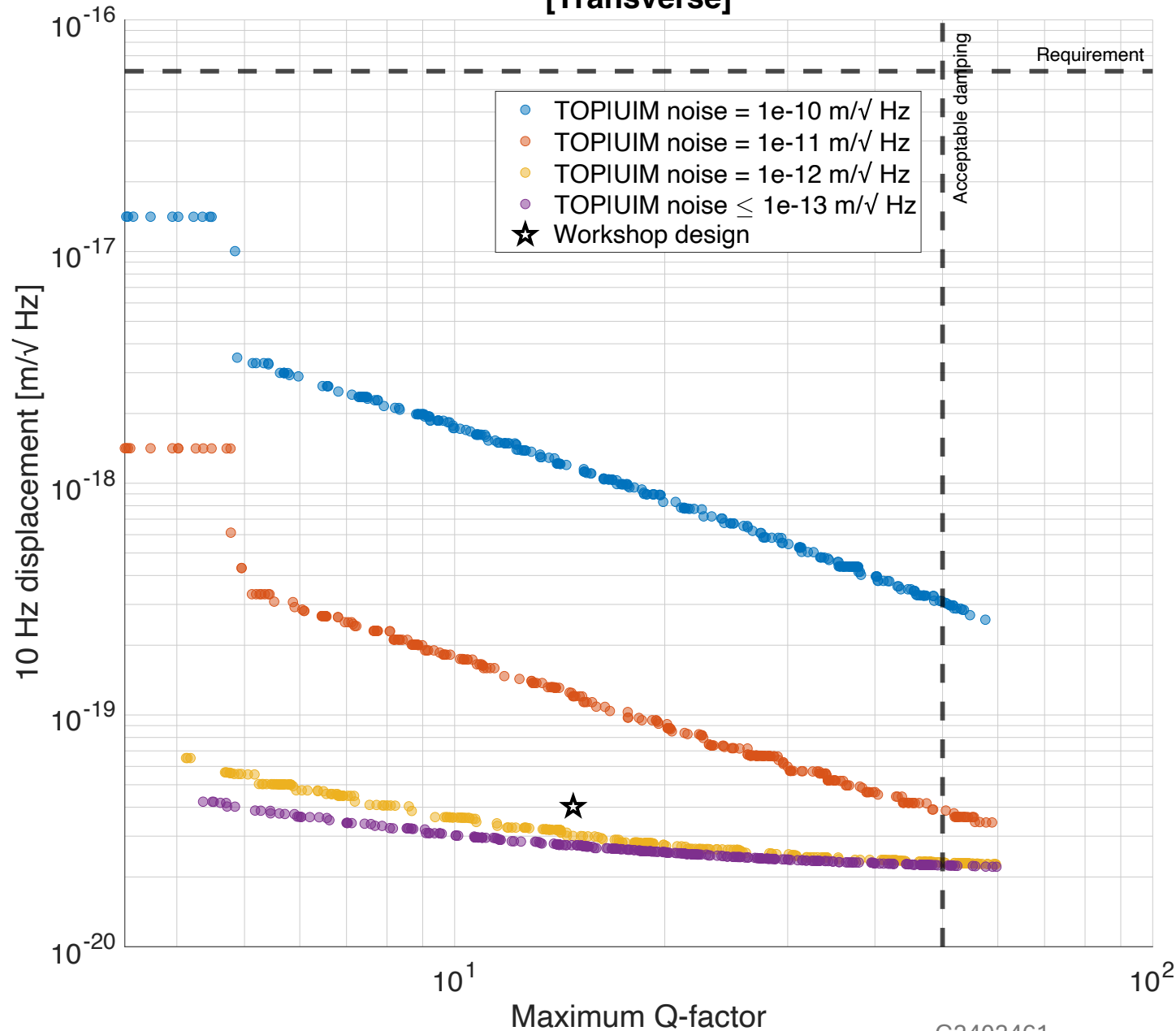
Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Roll (excluding the roll mode):

- We can piggyback from the other DOFs.
- The UIM is not required to achieve these loop performances.

Pareto front for local damping [Transverse]



What noise for sensors?

Assumed controller:

2 real zeros at 0 Hz, 2 real poles, elliptic filter for rolloff.

For Transverse (excluding the roll mode):

- We can piggyback from the other DOFs.

Caveats

- How much uncertainty can we tolerate on this design?

250 microns on the d-values (Limited by microseism)

- Can we reduce the actuator noise?

Yes - There is at least a factor of 3 margin to reduce the ESD's authority without saturating the DACs
(most of the actuation RMS happens at the UIM)

- How good do the sensors need to be?

Noise < $3\text{e-}11 \text{ m/Hz}^{1/2}$ @ 10 Hz

Bare minimum performance

Noise < $5\text{e-}12 \text{ m/Hz}^{1/2}$ @ 10 Hz

Required to meet BHQS design

Noise < $1\text{e-}12 \text{ m/Hz}^{1/2}$ @ 10 Hz

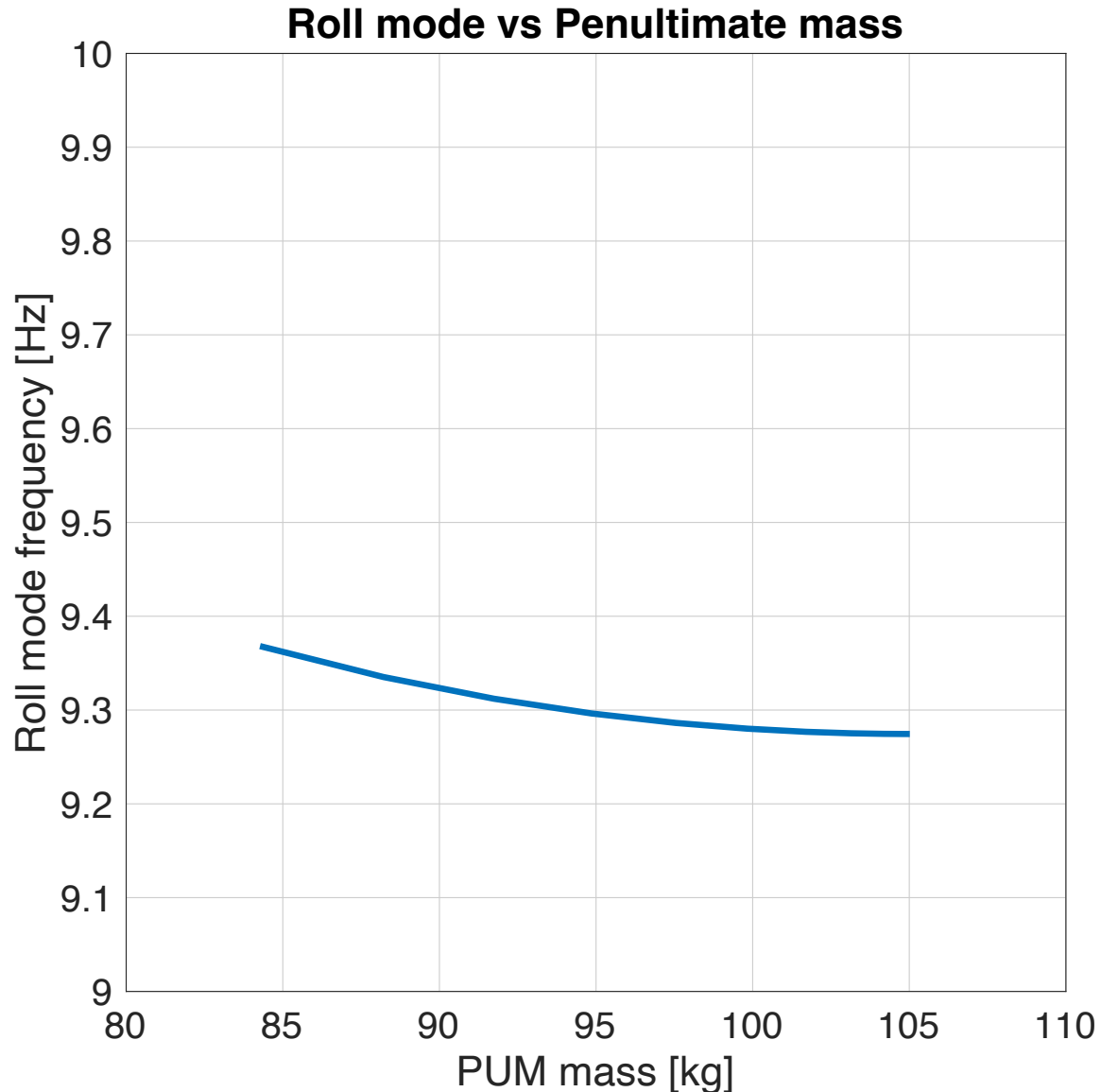
Target sensor performance

Noise < $5\text{e-}13 \text{ m/Hz}^{1/2}$ @ 10 Hz

Excellent (we should improve the ISIs now)

Last minute things that we might want to consider

- Accurate assessment of the Roll mode frequency.
- Should we trade off Roll mode for Longitudinal isolation?
- What if we increased the mass of the test mass to 105 kg?
- What about trading Pitch at low frequencies for damping the Pitch hard mode?
- Should we change the orientation of the blade springs?



Should we trade off with the roll mode?

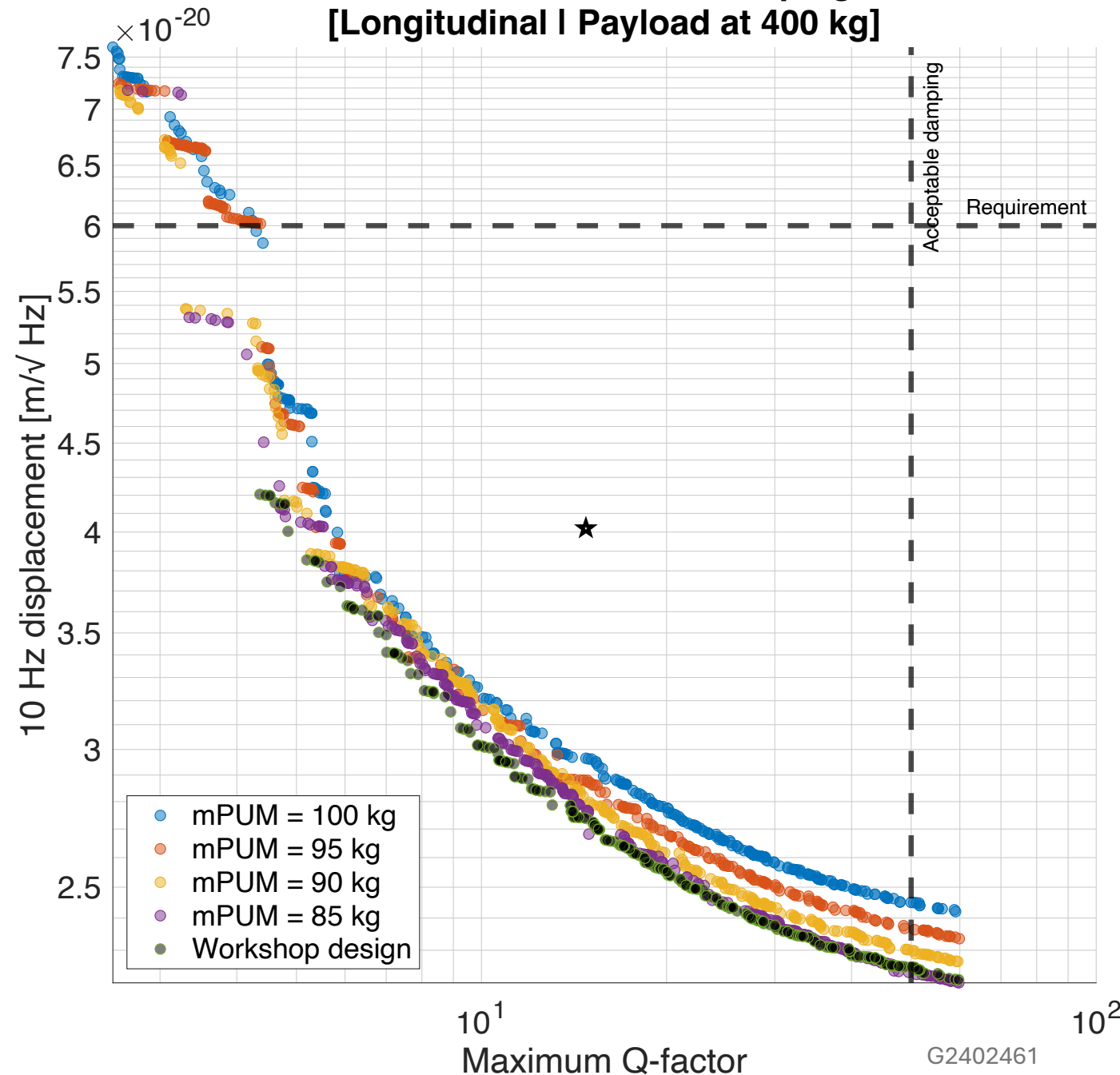
- Taking into account the effect of the nulling region for the fibers sets the roll mode at around 9.3 Hz.
- Changing the mass of the PUM in a ‘donut’ pattern has little effect on this.

Recommendation:

Only trade off if something would greatly benefit (Length | Pitch | Yaw)

Not very worth the risk since the $f_{\text{Roll}} > 9 \text{ Hz}$

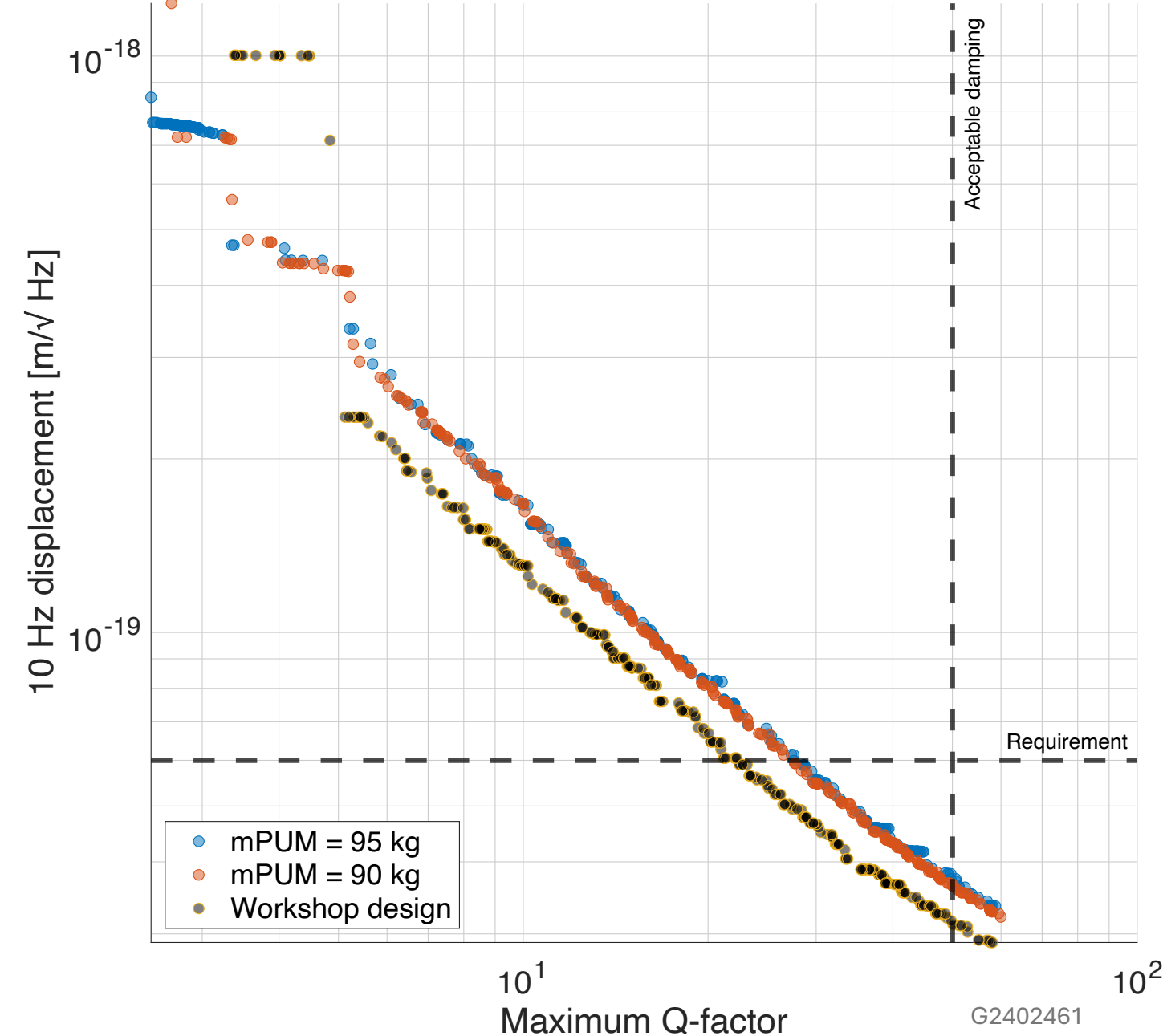
Pareto front for local damping [Longitudinal | Payload at 400 kg]



Should we increase the mass of the TST stage?

- We get marginally worse longitudinal performance unless we increase the payload proportionally.
- Payload should be 420 kg if we want to retain Longitudinal isolation.

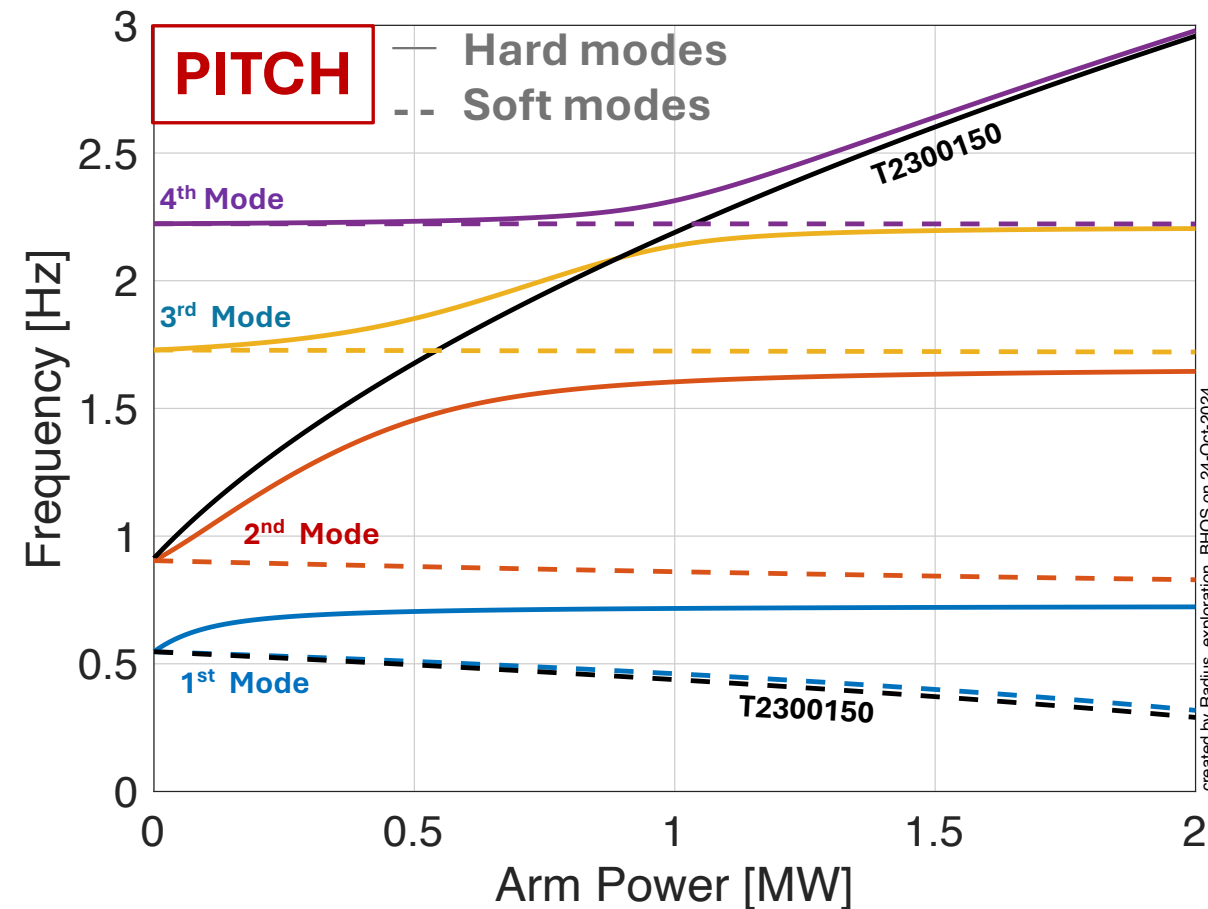
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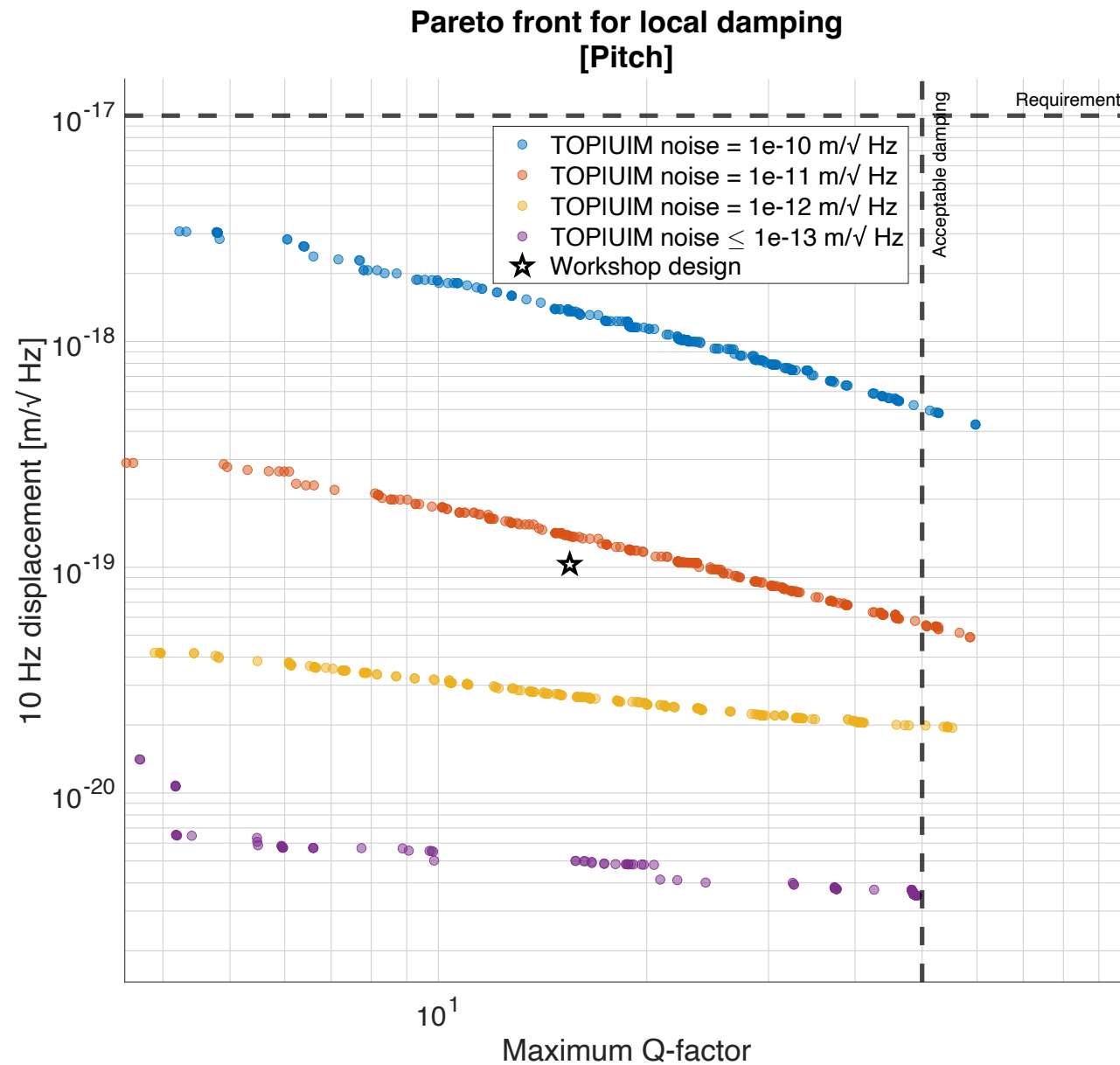


$$f_{4,\text{hard}} \approx \frac{1}{2\pi} \sqrt{\frac{k_{\text{hard}} + k_4}{I_4}}$$

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- If we added $1\text{e-}11 \text{ m/Hz}^{1/2}$ sensor noise the situation looks equally compromised.
- Payload should be 420 kg if we want to retain Longitudinal isolation.
- Moving to 105 kg results in a 2.5 % reduction in the Pitch hard mode frequency at 1.5 MW

Recommendation:

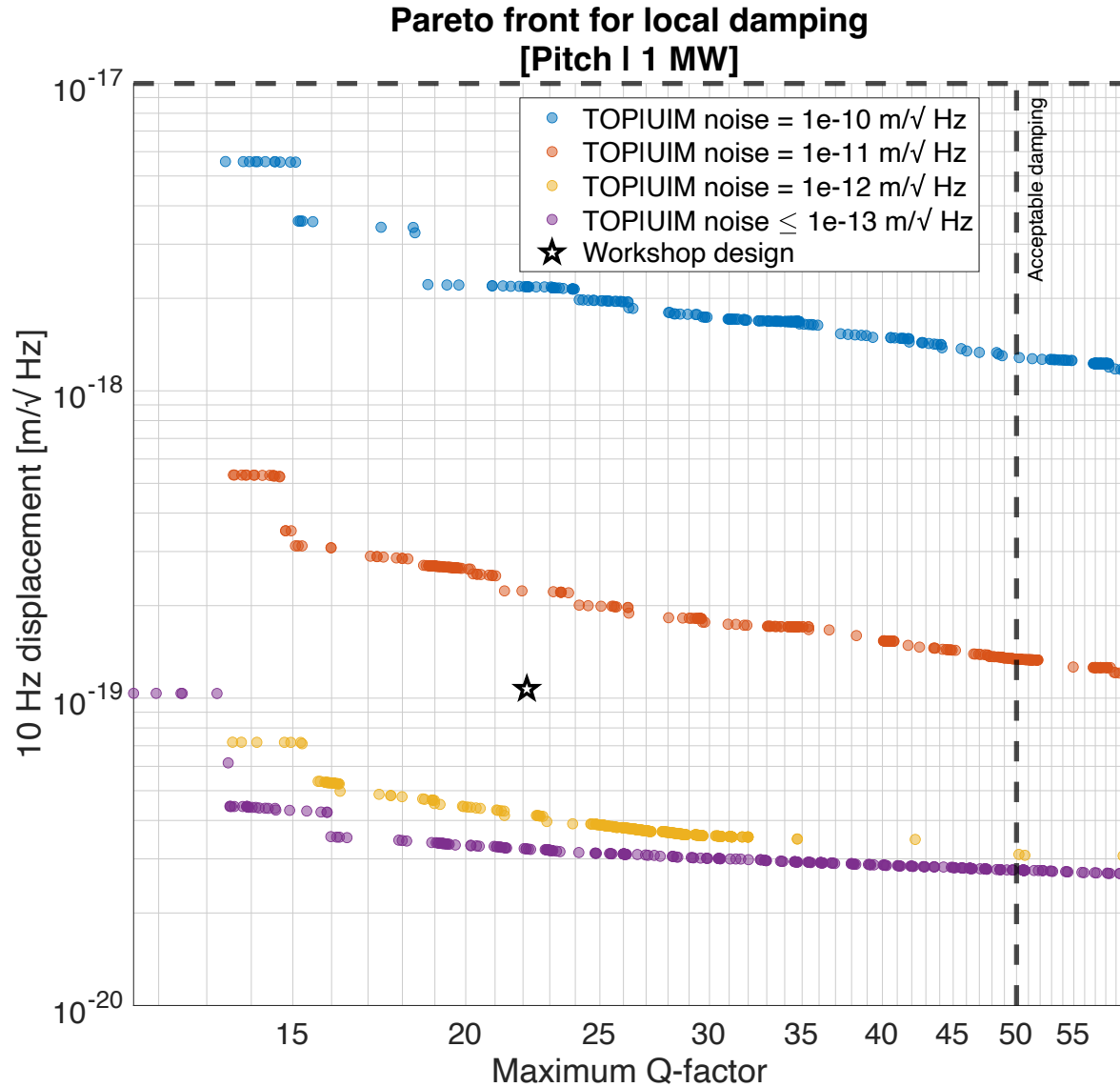
Increase proportional to the payload if possible.
Unless 2.5% change in the hard mode is worth it



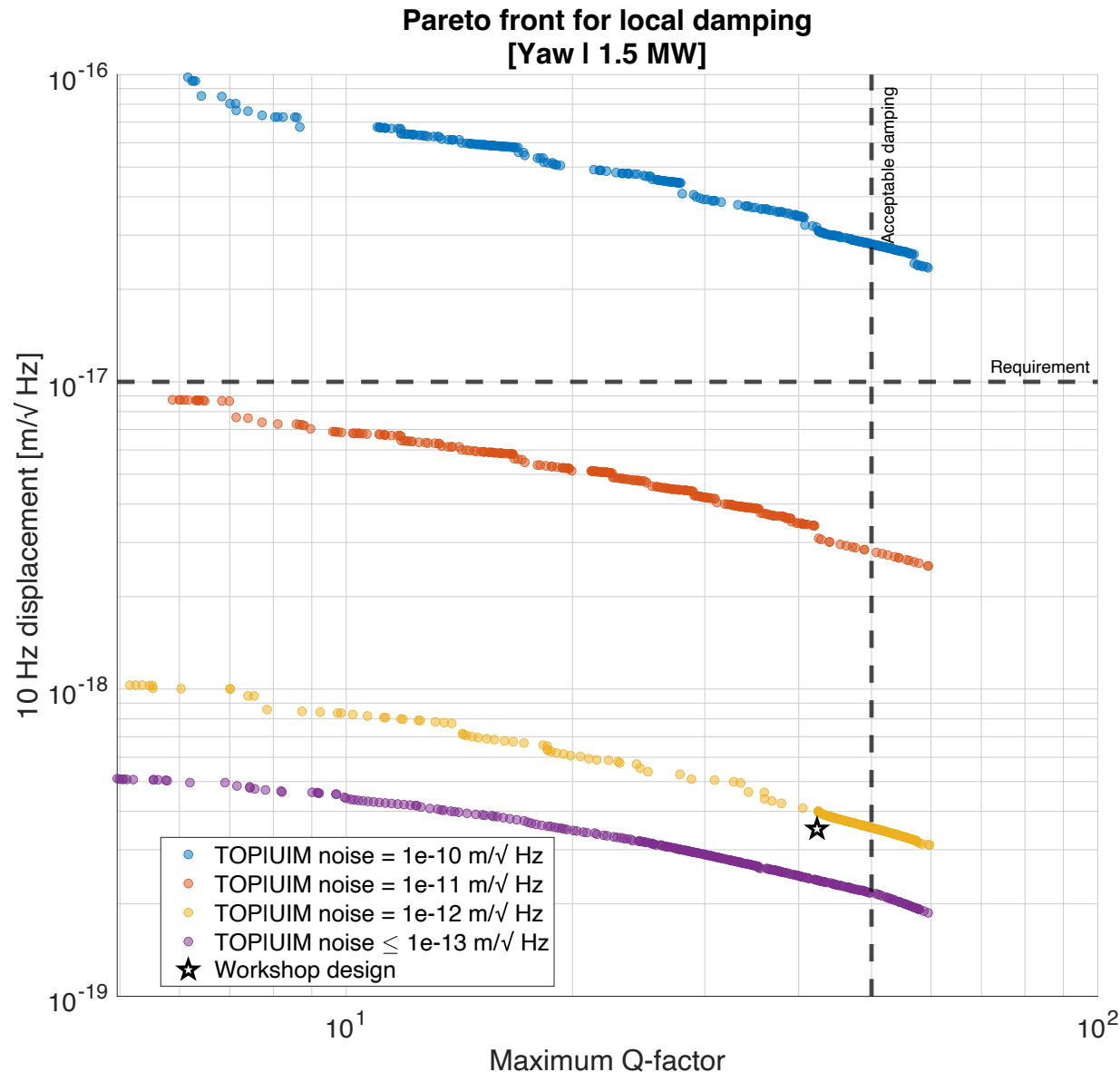
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 - By 1.2 MW it is unfeasible to keep the Q below 20 with local damping



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 - By 1.2 MW it is unfeasible to keep the Q below 20 with local damping
- In contrast, Yaw can be damped to a Q of 8 while meeting the requirements with $1e-11$ m/Hz^{1/2}

Recommendation:

Target an 'easy to operate' power over which we want low Qs.

Design with less margin to locally damp for longer

General conclusions

- The conceptual design of the BHQS is finalized.
 - Hopefully, all modes below 10 Hz.
 - It should perform without issues until 800 kW – should be easy to work at 1 MW power.
 - The ASC is challenging past that up to 1.5 MW
- We have a tool to compare (and codesign) damping with suspension designs. [15 second runtime per design]
- We established tolerances for the d values (0.25 mm)
- We established a target for the suspension sensor performance:
 - Noise < $1\text{e-}12 \text{ m/Hz}^{1/2}$ @ 10 Hz Target sensor performance